











**FUlly Solved** 

New Testing System

GUIDE

# GRE- GAT General (Local) Test With Explanatory Answers

For

Various Kinds Of Entry Tests Including Ph.D., M.Phil & National Talent Scholarship Scheme (NTSS)Etc.



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# NEWTESTINGSYSTEM GUIDE

GRE-GAT GENERAL (LOCAL) TEST

# **Plus EXPLANATORY ANSWERS**

For Various Kinds of Entry Tests Including Ph.D., M.Phil & National Talent Scholarship Scheme (NTSS) Etc.

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'' ڈوگر پبلشرز'' کا ادارہ کسی تعارف کامختاج نہیں۔ بہاشاعتی دنیا کا ایک معتبر نام تصور کیا جاتا ہے۔ تعلیمی میدان میں اس ادارے کی خدمات لاز وال ہیں۔ ہمارے ادارے کے تحت شائع ہونے والی'' ڈوگرز یونیک'' کت کواسا تذہ اورطلباء وطالبات میں جویز برائی نصب ہوئی' وہ بہت کم اداروں کا مقدر ہوتی ہے۔ خداوند کریم کے فضل و کرم ہے ہماری کتب نہ صرف ملک کے طول وعرض میں پڑھی اور پڑھائی جاتی ہیں بلکہ بیرون ملک بھی ان کی طلب میں روز افزوں اضافیہ ہور باہے ۔ شاید یمی دجہ ہے کہ طلبہ کو جب مھی کوئی دشواری پیش آتی ہے تو وہ راہنمائی کے لیے ہمارے اوارے کا رخ کرتے ہیں اور جاری پیکوشش ہوتی ہے کہا بے معزز قارئین کو بھی مایوں ندکریں۔اس مقصد کیلئے ہم نے ملک کے نامور ماہر بن تعلیم ماہر بن تعلیم نفسیات سینتر یروفیسرز'اساتذه کرام' ماہرین نصاب اورامتحانات پرششل ایک ایٹریٹوریل بورڈتشکیل دیا ہے جو کہ طلبہ کی مشکلات وشواریوں اور صروریات کو مدنظر رکھتے ہوئے مختلف عنوانات اور مضامین پر کتب مرتب کرتا ہے۔

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ہارے ملک میں جب بیرونی ممالک میں رائج ETS ک طرز پر NTS کا آغاز کیا گیا تو طلبہ کی کثیر تعداد نے راہنمائی کے لیے ہارے ادارے کارخ کیا۔ شروع شروع میں NTS کا دائرہ کارمحدود تھالیکن وقت گزرنے کے ساتھ ساتھ اس کی اہمیت اور افادیت کو مدنظر رکھتے ہوئے اس نظام کو وسعت دی گئ البذا جب ہم نے محسوں کیا کہ طلب کو گائیڈ کرنے کے لیے ایک کتاب کی اشد ضرورت ہے تو ہم نے قو می خدمت کو بدنظر رکھتے ہوئے بی تا بتح ریر نے کا ادادہ کیا۔ حد شکر ہے اس ذات باری تعالی کا جس نے مجھے ہمت اور حوصلہ عطا فرمایا کہ میں اس کا م کو پایئے تھیل تک پہنچا سکا۔ یہ آیک معاری منفرداور جامع کتاب ہے جس میں NTS کا بطوراحس احاطہ کیا گیا ہے اور کس بھی پہلوے صرف نظرنہیں کیا گیا۔ یہ کتاب NTS کے حوالے ے طلبہ کی بہترین معاون ثابت ہوگی۔اس میں غیرضروری چزوں کوشامل نہیں کیا گیا۔اس گائیڈ کو بڑھنے کے بعد جب طلبہ کمرہ امتحان میں بیٹھیں گے تو انہیں پیرے حوالے سے اجنبیت کا احساس نہیں ہوگا۔ گائیڈیس باڈل پر چہ جات ای نقطہ نظر کو مدنظر رکھ کرشا ل کئے گئے ہیں۔

NTS کے استخانات میں شرکت کرنے والے معزز طلباء و طالبات اس بات کو پین نظر رکھیں کہ یہ کتاب محص ایک گائیڈ ہے جو کہ آپ کی راہنمائی اورمشکلات کا ازالہ کرنے سے لیے تحریر کی گئے ہے۔ یک میں صورت میں احقانی پر جہ جات کا کمل احاط نہیں کرتی۔ اسخانات کی تمل تیاری سے لیے آ یکوامتحان کی نوعیت کے اعتبار سے تجویز کردہ کتب کا مطالعہ کرنا ضروری ہے۔ عام طور پر (GRE(Local) 'SAT'GAT(General) یا GMAT کی کتب جویز کی جاتی ہیں۔ بہتمام کتب بین الاقوا ی طور پر منعقد ہونے والے مخلف امتحانات کی ضروریات کو مدنظر رکھ کرتحریر کی جاتی ہیں۔ آ ب کوان عنوانات پر میثار غیر میکی کتب مارکیٹ میں وستیاب ہوسکتی ہیں۔ ہمارا ادارہ اللہ تعالیٰ کے فضل و کرم سے SAT'GMAT اور GRE پر مہلی مرتب پاکستان کے تعلیمی پس منظر کو مدنظر رکھتے ہوئے یونیک کتب شائع کررہا ہے جو کہ بہت جلد مارکیٹ میں دستیاب ہوں گی اور جمیں اُمید کال ہے کہ بی ستبالك سنك ميل البت مول كي-

معزز قار کین! ہم نے آپ کی آسانی کیلیے اس کماب کو مختلف حصول میں تقتیم کیا تاکہ آپ کو امتحانات کی تیاری میں کوئی دشواری پیش نہ آئے۔ English اور Arithmetic کے مضامین پرخصوصی توجہ مرکوز کی گئے ہے جو کہ تمام اتسام کے امتحانات میں لازی طور پرشامل ہول گے۔ آپ کی سولت کی خاطر ماؤل پیرز کا اضافہ بھی کیا گیا ہے۔ بیکتاب ایک انسانی کاوٹن ہے جو کہ یقنیا غلطیوں سے مبرانہیں ہوگا۔ اس سلسلے میں ہمیں آپ کا تعاون درکار ہوگا۔آپ اگر اس کتاب میں کوئی کی یافلطی یا کیں تو ہمیں ضرور مطلع فربائیں۔اس سے علاوہ اس کی بہتری سے لیے آپ کے پاس کوئی تجاویز ہوں تو وہ بھی ضرورارسال کریں ہم انہیں ضرور مدنظر تھیں گے۔ آخریں میں اس کتاب کی پخیل کے حوالے سے ڈوگر پبلشر زایڈ بیٹوریل بورڈ کے ارا کین کا تهددل سے شکر ریادا کرتا ہول جنہوں نے اس سلسلے میں اپنا بھر پور کر دارا دا کیا۔

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## تعارف (Introduction)

بین الاقوای طور پر NTS کئی چیزوں کے ناموں کا تخفف ہے لیکن بیالی نیاامتحانی طریقہ کار (New Testing Scheme) ہے۔ پاکستان میں اے بیشنل شیسٹنگ مروس کے نام سے موسوم کیا گیا ہے اور میٹمیٹ منعقد کروانے کے لیے تجی طور پر آیک ادارے کو ذمہ داری مونی گئی ہے۔ ابتدا میں بیڈمیٹ لی ۔ آئی ۔ ڈی اور ایکی منطح پر مختلف یو نیورسٹیوں 'کالجوں اور ایمی منطق کی جارہی ہے اور ملکی منطح پر مختلف یو نیورسٹیوں 'کالجوں اور اور اور اور کی منطق کی ذمہ داری بھی ای ادارے کو مونی جارہی ہے۔

ذور پہلٹرز نے شعبہ تعلیم کے تمام میدانوں میں خدمت سرانجام دیے گائز م کررکھا ہے ای لیے NTS کے حوالے سے طلبہ کی مشکلات کو مذظر رکھتے ہوئے ان کی مناسب دہنمائی کے لیے یہ تمال بیار کی گئی اور رہام جذبہ خدمت کو مذظر رکھ کرکیا گیا ہے۔ دنیا کے بچھ یما لک میں NTS کے بجائے ETS رائج ہے۔ ہارے بچھ ہما لک میں بھی امتحال کے بیار کا گئی اور رہام جذبہ خدمت کو مذظر رکھ کرکیا گیا ہے۔ دنیا کے بچھ یما لک میں بھی امتحال کے بیار کا نہا ہے۔ پاکستان میں اس ادارے کا قیام جولائی 2002ء میں عمل میں لایا گیا جس کا مقصد طلبہ کے منطق مطحول پر علیحہ ہ علیحہ و استفیاد ہو کہ معال میں بھی بڑا فرق ہے۔ ای وجہ سے بڑے اداروں کے طلبہ مستفید ہو جو سے اس کے مطلبہ کا علیحہ معیار معیان کرتا تمال ہونے کے میں اور پیائی ای طرح معیار تعلی میں بھی بڑا فرق ہے۔ ای وجہ سے بڑے اداروں کے طلبہ مستفید ہو جاتے ہیں اس لیے طلبہ کا علیحہ معیار معیان کرتا تمال ہے۔ میں اس کے میں اس کے کا کوشش کی گئی ہے۔

مقاصد (Objectives): جیما کداد پر بیان کیا گیا ہے NTS کا بنیادی مقصد طلبہ کی صلاحیتوں تابلیتوں اور میلانات کی بیائش کرنا ہے اور پاکستان میں معارتطیم میں بہتری لانا ہے۔اس کا مقصد بین الاقوامی اور کلی سطح پر یو بیورسٹیوں کالجوں اور اداروں میں داخلہ لینے کے خواہش مندامیدواروں کے داخلہ امتحانات منعقد معاصدوں ویل میں:
محاوانا ہے۔اس کے چھر چیرہ چیرہ مقاصدوں ویل میں:

- ادر مدم وجوده طریقید امتحانات میں پائی جانے والی خامیوں کا از الد کرنا اور طلبہ کی صلاحیتوں کا بطور احسن جائزہ لیتا اور بیائش کرنا۔
- :- ایک مناسب درست اور سائمنیفک طریقهٔ کار متعارف کروانا۔ اس مؤثر طریقهٔ کار کے ذریعے مختلف اقسام کے واخلہ مسٹ منعقد کروانا۔
- 3- بین الاتوای اور تکی سطح پر یو نیورسٹیوں کا فجز اور اداروں میں دافطہ کے متنی طلباء و طالبات کے لیے ایک معیاری اور بکساں امتحانی طریقیہ کارروشناس کروانا تاکسکی کی مق تلفی ندہو۔
  - 4- مین الاقوامی مطمی جوایجنسیان تمیست لیتی بین ان کے لیے واخلہ نیسٹوں کی تیاری کروانا تاکہ جب طلب استخانات میں بیٹسیں تو انہیں اجنبیت کا حساس نہو۔
    - من ایک مخصوص مضمون میں طلب کوند مر کھنا بلکسان کی کما حقد اور بنیادی صلاحیتوں کو پر کھنا۔ طلبہ میں پائی جانے والی خامیوں کا از الد کرتا۔
    - بشمول ملازمت بیشراور بیرودگاراً میدوارول کے علم اور مهارتوں کی بنیاد پر بیائش کرنے اور صلاحیوں کے جائز و لینے کے لیے مؤثر اور قابل جروسراتهام مها کرنا۔
- 7- تغلیمی تیاری اورمعاشرے میں عملی طور پر ضرورت کے اعتبار کے درمیان موجود خلاکو پُر کرنا مینی استے ہی بیشہ درافراد تیار کیے جا کمیں جن کی مادکیٹ بٹن کھیت ہوسکے۔ NTS ایک غیرمنافع بخش خود مخار ادارہ ہے جو کہ پوری محنت مگن اور جانفشانی ہے اپنے مقاصد کو بردیے کا رلانے میں مصروف پیٹل ہے۔ طلبہ کے حوالے ہے
  - ورج ذیل چند بنیا دی امور پر اس کی خصوصی توجہ ہے: نیا درج پیانے پر اعلی معیار تعلیم کوفر درخ ویا۔

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- الله المراكثون المتحانات أوريائش كودرست مناسب اورمؤثر بنانا ..
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  - المعتقب السام كيسسول اوردا فطے كے امتحانات كا انعقاد ـ
- القواى الرمكي سطير تعليم اور بيشدوارانه شعبول كم اين ايك را يطيكاكام كرنا-
- - فسدداری سونی ہے اور وقت گزرنے کے ساتھ ساتھ ان کی تعداد میں مزیدا ضافہ ہونے کا امکان بھٹی ہے۔

Nea		,
Testing	Con	tents
50 50	INTRODUCTION ABOUT NTS	SECTION - II
2 2	Introduction	ANALYTICAL REASONING
avide faide	Objectives of NTS7	Preposition
	NTS Commitment	Symbols Used in Logic
1 1	NTS - Services8	Explanation226
2 1 2	Test Format 10	Conjunction227
50 00	Test Schedule for GAT Subject 2007 13	Disjunction227
2 2	NTS - Test Centers14	Implication or Conditional227
2 2	Schedule and Information	Biconditional
Gaide Gaide	Original Advertisement16	Model Examples227  Multiple Choice Questions (MCQs)229
New	SECTION - I	Explanatory Answers231
esting .	QUANTITATIVE ABILITY	SECTION - III
System	Sauk A	VERBAL ABILITY
	Pow Arithmetic	
Garide	, , , , , , , , , , , , , , , , , , ,	Pour Sentence Completion
	1. Numbers	Hamita Amania Completion
1 1	2. Multiplication & Division	How to Answer Sentence Completion  Ouestions235
12 6	3. Highest Common Factor & Least	Examples with Explanatory Answers235
2 4	Common Multiple	Kinds of Sentence Completion236
System System	4. Square Root	Multiple Choice Questions Tests (1-12)236
2 2	6. Percentage	<i>P</i> <b>▲</b> <i>P P P P P P P P P P</i>
di si	7. Ratio and Proportion	Pow Analogy Questions
2 3	8. Average	Multiple Choice Questions Tests (1-2).268
	re-	Synonym/Antonym Tests274
State Later	₽®₩ <b>₩</b> Algebra	MA 1 Costs
30 30	<b>*</b>	Pour Critical Reading
stan	1. Polynomials	· •
Gaide	2. Equation	Comprehension279
2 8	3. Inequality103	Long Passages with Explanatory Answers.279
New	4. Word Problems108	Short Passages with Explanatory Answers 284
1 1 1		GRE-GAT GENERAL TESTS WITH
Testing Testing	Pour Geometry	EXPLANATORY ANSWERS
System	•	GRE-GAT Test No. 1295
tien	1. Lines and Angles 111	GRE-GAT Test No. 2311
Gaide	2. Triangles	GRE-GAT Test No. 3325
, ,	3. Quadrilaterals & Polygons 153	GRE-GAT Test No. 4339
New 1	4. Circles	NTS TESTS WITH
13 27	5. Area	EXPLANATORY ANSWERS
4. 4.	6 Solid Geometry 191	NTS Test No. 1353
39.00	7. Coordinate Geometry	NTS Test No. 2360
8 12	8. Counting & Probability	NTS Test No. 3366

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New Testing Lotter Gaide New Testing Service لستان کے علیمی پس منظر میں نیار کی گئی ڈوگر پبلشرز کی چندشاہ کار کتابیں درج ذیل کتب کی ضرورت عرصہ دراز سے محسول کی جارہی تھی کیونکہ یہ غیرمکی کتب ہمارے لوکل ٹمیٹ سسم سے مطابقت نہیں رکھتی تھیں اور ہارے ملک میں تیار کیے جانے والے ٹیسٹوں میں ان میں سے %30 سے زیادہ سوالات نہیں آتے New تھے۔اب ہم نے ان کتب کوا سے مرتب کیا ہے کہ انشاء الله 100% سوالات ہماری کتب میں سے یوچھے جا کیں گے۔ Dogar's Unique GRE With Explanatory Answers Dogar's Unique SAT With Explanatory Answers Dogar's Unique GAT With Explanatory Answers Dogar's Unique GMAT With Explanatory Answers Carde غیر ملکی SAT 'GAT 'GRE اور GMAT وغیرہ زیادہ تر غیر حل شدہ ہوتی تھیں کیکن ہم نے تمام New Testing سوالات کوحل کرکے اپنی کتابوں میں شامل کیا ہے تا کہ طلباء وطالبات کوکوئی دشواری در پیش نہآ ئے۔ Some Important Features: 🖈 تکمل وضاحت اورحل ☆ Fully Explained With Explanatory Answers ↑ 55 سے زائد غیر ملکی کتابوں کا نیوژ ☆ An Extract of Variety of Books Men Testing 🖈 سابقه برجه جات کے سوالات کا مجموعه ☆ Questions Collected from Previous Papers 🏠 برمضمون اورعنوان كى عليحده وضاحت اورتعارف ☆ Topic by Topic Explanation and Introduction 🖈 رياضي يرخصوصي توجه ☆ Special Stress Upon Mathematics Carile ☆ Guidance from Paper-Setting Authorities مختلف اقسام کے پرچہ جات بنانے والے ماہرین کی خدمات حاصل کر کے ایسے سوالات کتابوں میں شامل کیے گئے ہیں جو کہ سوفیصد متوقع ہوں۔اپنی نوعیت' افادیت اورمواد کے اعتبار سے آپ ان کت کوغیرملکی کتب سے کہیں زیادہ منفر ذُجامع اور آسان یا کیں گے۔ (Be Pakistani and Buy Pakistani) دُوگرز بونیک بکس 17- أردوبازارلا بور فن 7313957 دُوكُوز بيونسك يكس ميني عرك راولينزي ون:5533165 دوگرز يونيك بكس اكبرازار شخويره فن: 3782738 36-ارددباذار كلهور فول: 7120060-7230332-7313957 **ڏوگرز يونيڪ بکس**'ارووبازار کراچي فون: 2766700 ال تاكون 731397 اليكان dogar publishers@yahoo.com ال دُوكُورُ يونيك بكس وصروالى بازارُيثاور ولا: 2590061 New Testing System Goide New Testing System Golde. New Testing System Golde. New Testing System Golde. New Testing System Golde

#### Introduction

"NTS" is a new testing system introduced by the government of Pakistan for the search of national talent. For this purpose, NTS was established in July 2002. An experience of decades brought it to the forefront that a large number of scholarships were restricted to certain pockets of the country and many areas remained unrepresentative. In the light of this, the new scheme of testing system was launched. The fundamental aim of NTS is to evaluate the knowledge level of the students. It also aims at to provide a single standard for quality evaluation of the educated human resource. There is no single syllabus in our educational institutions right from basic to the advanced level. There is also a big variation in syllabit taught in various schools, colleges and universities. A huge gap is also found in the standard of education and institutions. It is a vital issue to evaluate the knowledge of students on the prevailing system of examinations. NTS was established to solve this issue by evaluating the skills and knowledge of the individuals on a standardized measure.

NTS is providing training and testing programs for individual students. Efficiency, transparency, reliability and consistency are few prominent features of the NTS which are the main causes of its popularity. Most of the educational institutions and organizations are attracting towards it. In the beginning, NTS was conducting test only for Ph.D and M.Phil scholarships, but not it is also conducting Entry Test for admission to different educational institutions. With the passage of time, it is gaining a prestigious position in the testing system. It has become a reliable name in the field of testing. It has gained this position in a very short span of time.

#### Objectives of NTS

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NTS was established for the achievement of certain objectives and goals, so we can call it a national talent search scheme. It is a novel testing system introduced for the first time in Pakistan. Within the overall premise of contributing to the improvement of the quality of education in Pakistan, the important objectives of NTS are as under:

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- 1. The main objective of NTS is to improve upon the shortcomings in our prevailing performance evaluation system of candidates through establishing a credible, technically appropriate and accurate system of performance evaluation for students of different educational institutions at various levels in the country.
- Another important objective is to provide a standardized and uniform criterion for selecting candidates seeking admission to various universities in the country and abroad and also to provide a basis on which students, individuals and institutions can assess performance for preparation of various types of tests conducted by different international testing agencies.
- 3. To enable assessment and ranking not only in a particular subject on a general competency level but also help in identification of areas of strengths and weaknesses in its sub-contents on a disaggregated basis.
- To provide a reliable and efficient system for evaluating the knowledge base and
  skills of candidates including professionals employed and unemployed.
- 5. To establish a credible and reliable measure of assessing the students' knowledge in commonly taught programs for relative ranking.
- 6. To bridge up the gap between academic preparation and the practical market needs in a highly dynamic and competitive environment.

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#### NTS Commitment

#### Promoting Overall Quality of Education

Based on a vision aimed at providing quality <u>services</u> in educational testing and assessment mechanisms for various stakeholders, NTS is committed to promoting the overall quality of education as a value-added adjunct.

#### Performance Evaluation

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NTS undertakes programs that are aimed at establishing a credible, technically appropriate and accurate system of performance evaluation of students/candidates of various educational institutions at different levels.

#### Assessing Knowledge, Skills & Professional Abilities

It also extends services for the employed and unemployed professionals to get satisfactory jobs in their relevant area through an assessment of their knowledge base, skills, and professional abilities.

#### A Rapidly Growing & Credible Entity

NTS is a rapidly growing and credible entity of national repute. Its context and potential coincides with the expressed need of the Government for the establishment of a National Accreditation Council and Testing Service.

#### Conducting Various Types of Tests

While the beginnings were made by conducting <u>General Tests</u> through an IT-focused thrust, NTS has expanded its services to other disciplines of education testing. It now provides services for conducting <u>Subject Tests</u> by providing facilities both for individual candidates and institutions. These tests are prepared and assessed by experts and professionals from relevant fields.

#### Linkages & Networks

NTS now has growing linkages and associations with educational and professional organizations & institutions, including those engaged in talent search and career & educational promotion activities, at the national and international levels. (Courtesy to NTS)

#### NTS - SERVICES

NTS provides its services in vast areas:

#### National Aptitude/General Testing:

NTS conducts General Tests so as to evaluate the critical thinking skills of analytical reasoning and also performance assessment of candidates with regard to quantitative & verbal ability. General Tests also called National Aptitude Tests, help establishing a reliable and credible measure of judging the knowledge base of students in commonly taught program.

#### Services – Measuring Knowledge Base and Skill Levels:

The NTS Subject Tests are prepared and designed with a view to assess the qualifications, knowledge base, competency and skill level of the candidates in a specific area of study.

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#### Services for Test Preparation:

NTS provides complete guidelines with regard to Test Preparation. A guide for users is available on our website as well as in the market in printed form. Model Questions and Sample Tests are also available on the website for helping the candidates to practice and be well prepared for the test. Furthermore, Reference Books are also recommended by NTS to be an additional source of help for the test takers for Computer Science Subject Tests.

#### Administrative Services:

NTS provides an administrative service for not only the candidates but also the institutions. All administrative arrangements regarding registration, test center selection, test execution, result preparation and then its reporting etc. are taken as a responsibility by NTS.

#### Admission Test Services for Institutions:

NTS conducts Admission Tests for various institutes and organizations, all services like the arrangements of test registration, paper generation, test execution, paper marking, result declaration etc. are provided by NTS for these entities.

#### Services for Online Testing:

NTS also conducts Online Tests for the candidates' efficient and credible evaluation of their knowledge and skills. Arrangements like the availability of labs, content development for the assessment, online paper generation, test execution and online result formation immediately after the test, are made by NTS.

#### Establishing Performance Ranking:

NTS also assists in carrying out an estimated ranking of students as well as professionals. This ranking is not only in a particular subject on a general competency level but also helps in the identification of areas of strengths and weaknesses in its sub-contents on a disaggregated basis.

#### Services for Score Reporting:

For General Tests, NTS declares its results electronically within seven days of the test being conducted, the results of each candidate are sent to their homes through a fast and reliable courier service. The result of Online Subject Tests is displayed online immediately after the candidate completes his/her test. The score of candidates is also reported in the form of a certificate at their respective addresses.

#### Services to Facilitate Employment:

NTS extends its services for employed and unemployed candidates to get satisfactory jobs in their relevant areas through a very estimated and careful judgement of their knowledge base and skills. It facilitates access to job opportunities for various professionals and candidates both within the country and abroad on the basis of their scores in NTS Subject Tests.

#### Statistical Analysis and Reports:

NTS by virtue of its flexible and user friendly solution can better help the institutions and organizations to have statistical analysis and report for administrative tasks and it will ultimately lead to true decision making and managerial tasks.

#### • Survey:

NTS has very robust and accurate system for processing forms and surveys. In addition to the educational and professional testing services, NTS has the survey facility for different organizations, government data collection and other methods to get feedback from people. (Courtesy to NTS)

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#### **Test Format**

#### **General Tests**

#### Type & Design of Questions:

The General Test is generally divided into three sections, i.e., The Verbal Section, Quantitative Section and the section of Analytical Reasoning. All the questions are based on Multiple-Choice Question format.

The test of Verbal Section is based on completing sentences with the appropriate words, pointing out the errors in the sentences, comprehension exercises to assess the basic knowledge about the vocabulary and grammar of the language. Questions are basically about sentence completion, analogy and critical reading.

In the Quantitative Section, the NTS tries to measure your basic mathematical skills and check your understanding of the elementary level mathematics. The MCQs in this section are based on three areas, i.e., Arithmetic, Algebra and Geometry.

In the Analytical Section, various objective type questions are asked to analyze the capability of every student with regard to their problem solving aptitude in the daily life activities and also the academic interests. Questions asked are basically on the analytical reasoning and logical reasoning.

A few Model Questions in the website can help you in being familiarized with the nature of questions.

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#### **Duration of the Test:**

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The duration of NAT(S) is 120 minutes. The Verbal Section is given 20 minutes in which the candidates are asked to solve 20 questions. The Quantitative Section has been given 55 minutes for the solution of 35 questions. In the last section, i.e., the Analytical Section, 45 minutes are provided to the candidates to answer 35 questions.

The duration of NAT(G) is also 120 minutes. The time suggested for Verbal Section is 35 minutes. 28 and 57 minutes time is recommended for the Quantitative and Analytical Reasoning Section respectively.

The following time table is prepared which describes the number of questions, its time and marks distribution more clearly:

	Scier	ice (NAT-S)		
Test Sections	No. of Questions	Suggested Time	Marks	
Verbal	20	20	20	
Quantitative	35	55	35	
Analytical	35	45	35	
	Scien	ce (NAT-S)		
Test Sections	No. of Questions	Suggested Time	Marks	
Verbal	35	. 35	35	
Quantitative	15	28	15	
Analytical	40	57	40	

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#### **Subject Tests**

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#### Type & Design of Questions:

The test consists of 120 Multiple Choice Questions (MCQs) that range in difficulty level (easy, moderate and hard). The Questions have been selected from a standardized curriculum that has been designed by experts and professionals and is updated from time to time.

#### **General Test (NAT)**

The National Aptitude Test program (NAT) aims to assess the verbal, quantitative and analytical abilities that have been attained over a period of time and that are not necessarily related to any specific field of study.

The Verbal Section measures the ability to analyze and evaluate written material and synthesize information obtained from it; to analyze relationships among component parts of sentences and recognize relationships between words and concepts. There is a balance of different subject matters, i.e., humanities, social sciences, and natural sciences.

The Quantitative Section measures your basic mathematical skills, understanding of elementary mathematical concepts, and the ability to reason quantitatively and solve problems in a quantitative setting. There is a balance of questions requiring basic knowledge of arithmetic, algebra, geometry, and data analysis. These are essential content areas usually studied at the high school level.

The Analytical Reasoning tests your critical thinking and analytical writing skills. It assesses your ability to articulate and support complex ideas, analyze an argument, and sustain a focused and coherent discussion. It does not assess any specific content knowledge.

Present NAT programs have an IT & CS-focused thrust and have different levels that includes;

#### NAT-IS NAT-IIS NAT-IIG NAT-IIG

NAT-IS & NAT-IIS programs are meant for candidates who hold a degree in Science discipline and wish to pursue further education in graduate or post graduate courses, respectively.

NAT-IG and NAT-IIG programs are designed for candidates who hold a degree in Humanities discipline and wish to pursue further education in graduate or post graduate courses, respectively.

Note: It may be noted that in case of the 2nd Masters in Development Studies Program (MDS-2) being offered in Fall-2005, candidates may indicate their preference to take the test in NAT-IIG or NAT-IIS, irrespective of their previous academic background being in Science or Humanities. The MDS Program is presently being offered by CIIT Abbottabad only by the Department of Development Studies. A specific Test Format, Test Scores and Test Fee are designed for the General Tests.

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New Testing Series Gaide New Testing System Gaide New Testing Series Gaide New Testing Series Gaide New Testing Series Gaide New Testing System **Subject Tests** NTS Subject Tests have their own special attributes: These tests help in comprehen we evaluation of a candidate emphasizing any one required area of study or specialization. Garde The scores of NTS Subject Tests interpret the acquired knowledge base of candidates and predict their abilities regarding their specific knowledge, skills New Testing System Gaide and abilities in a number of different ways. These also help in the overall Testing ranking of students. The NTS Subject Test focuses on evaluating the knowledge base and skills of the candidates in a specific area of study. These Subject Tests are extremely helpful in measuring the potentials, capabilities and knowledge of candidates in specific fields. New Testing System The NTS Subject Tests enable assessment and ranking not only in the particular subject on a general competency level but also help in identification of areas of strengths and weaknesses in sub-contents on a disaggregated basis in that particular subject. NTS offers Subject Tests in various disciplines: Computer Science (CS) Biology Physics Mathematics Chemistry Psychology English Graduate Assessment Test (GAT) - Subject Coule These tests are designed for those who have extensive background in that specific subject/discipline. New Testing System Gaide These tests help cvaluate students' ability to analyze and solve problems, understand relationships, and interpret material in their particular field. These are prepared on national level, i.e., to assess students' capability and existing knowledge in their specific/major area of study. Presently, these tests are being offered in Computer Sciences and Management Sciences, only. The tests will be held biannually. The scores of this New Testing System Guide test remain valid for ONE WHOLE YEAR from the test date. A few of the other study areas are under process and are being considered for Subject Tests. Test Format of GAT Subject Total Questions (MCOs) = 100Total Test Time = 120 Minutes (2 Hours) Test Type: Paper Based Test Contents General Section = 30% of the Total Test Subject Section = 70% of the Total Test New Teating System Goods New Teating System Goods New Teating System Goods

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Areas of General Section 30%

English (Verbal) = 15%

Analytical Reasoning = 15%

#### Core Areas of Computer Sciences 70%

Sr. No.	Core Areas of Computer Sciences	Area Percentage (100% of the 70%)
1.	Discrete Structures	10%
2.	Algorithm & Complexity	12%
3.	Architecture & Organization	12%
4.	Operating System	12%
5.	Programming Fundamentals	09%
6.	Programming Languages	10%
7.	Information Management	12%
8.	Net-centric Computing	09%
9.	Software Engineering	10%
10.	Computational Science	04%

Core Areas of Management Sciences 70%

Sr. No.	Core Areas of Management Sciences	Area Percentage (100% of the 70%)
1.	Finance	33%
2.	Marketing	33%
3.	Management	20%
4.	Economic Analysis	14%

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#### Test Schedule for GAT Subject 2007

The Subject Test dates for Computer Sciences and Managements Sciences in the year 2007 is as follows

1. First test

**April**, 2007

2. Second test

October, 2007

The schedule of these tests in detail is as under:

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Sr.#	Advertisement Date	Last Date for Application Submission	Test Date	Result Date	Result Card Issue Date
First Test	February, 2007 & will be repeated on February, 2007	March, 2007	April, 2007	April, 2007	Before April, 2007
Second Test	August, 2007 & will be repeated on September, 2007	September, 2007	October, 2007	October, 2007	October, 2007

NTS website at least 7 days prior to test date.

Any queries will be received through e-mail latest by 4 days prior to the test date.

#### Registration & Test Fee

Applicants will be charged Rs. 600/- as test fee, in shape of Bank Draft in favor of NT Abbottabad (Bank Draft will be received along with Application Forms) as a matter of processing for registration.

Note: Candidates with more than 40 years of age are not eligible to apply.

#### Result Announcement and validity

- Results will be declared within seven days from the test date. 1.
- The candidates will be issued the result card through authorized courier 2. service/ Pakistan postal service (registered mail) within 14 days from test date.
- The results of GAT Subject remains valid for One Year (1 Year) from the test 3.
- The candidates intending to improve there NTS test score will be eligible to 4: reappear in the next test by applying afresh.
- NTS will verify the test score of the candidate on written demand of the HEC 5. within 48 hours.
- NTS will conduct these tests biannually and will issue NTS GAT Subject 6. Score Card to the individual candidate.
- Any candidate intending to improve his NTS GAT Subject Score can reappear 7. in the next test.

#### NTS – TEST CENTERS

Test will be conducted in maximum 20 cities of Pakistan depending on the number of candidates applied for test. (Sr. No. 1-5 cities are compulsory test centers and Sr. No. 6-20 are optional test centers depending on number of candidates applied for the said center a Minimum of 100 candidates per center)

- 1. Islamabad
- 2. Lahore
- 3. Karachi
- 4. Peshawar

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- 5. Quetta
- 6. Multan
- 7. Faisalabad
- 8. Guirat

- 9. Sargodha
- 10. Bahawalpur
- 11. D.I. Khan
- 12. D.G. Khan

- 13. Sukkur
- 14. Larkana

- 15. Nawabshah
- 16. Hyderabad

- 17. Bannu
- 18. Abbottabad
- 19. Muzaffarabad
- 20. Gilgit

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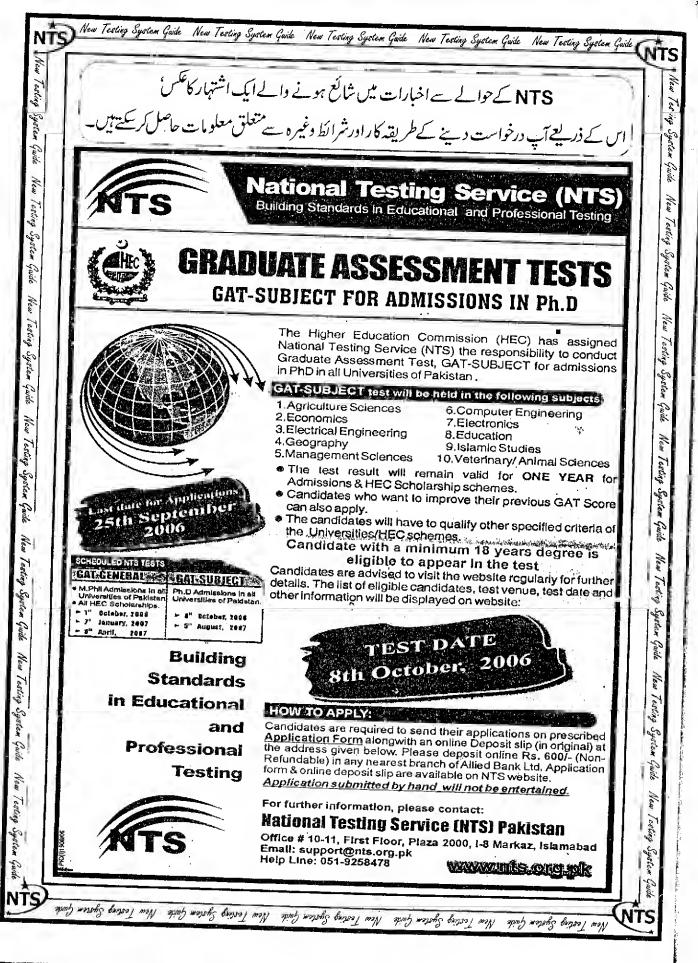
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# Quantitative Ability

The basic mathematical skills, understanding of elementary mathematical concepts, and the ability to reason quantitatively and solve problems in a quantitative setting are measured in the quantitative part of the test. The knowledge of arithmetic, algebra, geometry and data analysis, which are usually essential area of study of the high school level are measured in balanced questions. The questions about quantitative ability can also be asked from:

- → Discrete Quantitative Questions
- Quantitative Comparison Questions
- Data Interpretation Questions etc.

This section is discussed and explained in detail in this book. Topic by topic explanation is given to facilitate the candidates. Explanatory answers are also given to avoid complications.





#### Chapter-1:

#### Numbers:

In decimal number system, we use ten symbols 0, 1, 2, 3, 4, 5, 6, 7, 8, 9 called digits, to represent any number.

NUMBERS

Note: A group of figures, denoting a number is called numeral.

#### Types of Numbers

#### Natural Numbers:

Numbers which we use for counting the objects are known as natural numbers. It is denoted by 'N'...

$$N = \{1, 2, 3, 4, \dots \}$$

#### Whole Numbers:

All Natural Numbers together with zero form the set of all whole numbers. It is denoted by 'W'.

$$W = \{0, 1, 2, 3, \dots \}$$

#### Integers:

The set of numbers which consists of whole numbers and negative numbers is known as integers. It is denoted by Z.

$$Z = \{...... -3, -2, -1, 0, 1, 2, 3, .....\}$$

#### Positive Integers:

The set  $Z^+ = \{1, 2, 3, 4, \dots\}$  is the set of all positive integers. It is clear that positive integers and natural numbers are synonyms.

#### **Negative Integers:**

The set  $Z = \{-1, -2, -3, \dots\}$  is the set of all negative integers.

Remember: "0" is neither positive nor negative.

Non-Negative Integers:

The set  $\{0, 1, 2, 3, \ldots\}$  is a set of non-negative integers.

Non-Positive Integers:

The set  $\{0, -1, -2, -3, \ldots\}$  is the set of non-positive integers.

**Even Numbers:** 

The numbers which are divisible by 2 are called Even Numbers.

$$E = \{2, 4, 6, \ldots \}$$

Odd Numbers:

The numbers which are not divisible by 2 are called Odd Numbers.

$$O = \{3, 9, 11, 17, 19, \ldots\}$$

Properties of zero:

- 0 is neither positive nor negative.
- 2. 0 is an even integer.
- 3. 0 is smaller than every positive number.
- 4. 0 is greater than every negative number.
- 5. For any integer p;  $p \times 0 = 0$ .
- 6. For any integer p (including 0):  $p \div 0 = 0$ .
- 7. For any positive integer p;  $0 \div p$ ;  $\frac{0}{p}$  = undefined.
- 8. For every integer p; p + 0 and p 0 = p.
- 9. If the product of two or more numbers is 0, then at least one of them is 0.

Properties of one:

- 1. For any number  $p: p \times 1 = p$  and  $\frac{p}{1} = p$ .
- 2. 1 is the divisor of every integer.
- -3. 1 is an odd integer.
- 4. 1 is not a prime number, because prime numbers should be greater than 1.
- 5. I is the smallest positive integer.
- 6. For any number  $n: 1^n = 1$ .

Factors and Multiples:

A number which divides a given number exactly is called a factor of the given number.

Example 1: Find the factors of (i) 64 and (ii) 75.

Solution: (i) 
$$64 = 1 \times 64$$

$$= 2 \times 32$$

$$= 4 \times 16$$

$$= 8 \times 8$$

The factors of 64 are 1, 2, 4, 8, 16, 32 and 64.

(ii) 
$$75 = 1 \times 75$$

$$= 3 \times 25$$

$$= 5 \times 15$$

The factors of 75 are 1, 3, 5, 15, 25 and 75.

Division Algorithm:

Let a and b be two given integers such that  $b \neq 0$ . On dividing a by b, let q be the quotient and r the remainder, then a = bq + r,

Clearly, 0 < r < b

In general, we have

$$Dividend = (Divisor \times Quotient) + Remainder$$

Multiple of a Number:

A multiple of any natural number is a number obtained by multiplying that number by any natural number. Example: Find the multiples of:

(i) 4 less than 30

(ii) 9 less than 60

Solution: (i)	$4 \times 1 = 4$
	$4 \times 2 = 8$
	$4 \times 3 = 12$
	$4 \times 4 = 16$
	$4 \times 5 = 20$
	$4 \times 6 = 24$
	$4 \times 7 = 28$ etc.
: The mult	tiples of 4 less tha

- an 30 are 4, 8, 12, 16, 20, 24 and 28.
  - (ii)  $9 \times 1 = 9$

 $9 \times 2 = 18$ 

 $9 \times 3 = 27$ 

 $9 \times 4 = 36$ 

 $9 \times 5 = 45$ 

 $9 \times 6 = 54$  etc.

The multiples of 9 less than 60 are 9, 18, 27, 36, 45 and 54.

#### Divisible of a Number:

If a number divides a second number without leaving any remainder, then we say that the second number is divisible by the first number. For example, since the number 2 divides 14 without leaving any remainder, we say that 14 is divisible by 2.

Q1. How many numbers between 200 and 500 are divisible by 13? 23 (A) 17 **(B)** (C) 15 32 **(D)** Q2. The first five multiples of 17 are: 0, 1, 17, 34, 51 (A) (B) 17, 34, 51, 68, 85 (C) 38, 57, 76, 95, 114  $(\mathbf{D})$ None of these Q3. The number which is divisible by 7 but not by 14 is: (A) 21 (B) 12 (C) 71 -**(D)** None of these Q4. The total number of even prime numbers is: (A) **(B)** (C) None of these **(D)** Q5. The least prime number is: (A.) 0 **(B)** 1 (C) 2 3 (D) Q6. The smallest member of set W is: (A) 0 **(B)** 

(C) 2

3. **(D)** 

**(D)** 

- Q7. The smallest even number of three digits is:
  - (A) 98

(C)

102 **(B)** 

100

Q8. The smallest 4-digit number using 7, 0, 8 and 9 is:

998

(A) 0879

0789 **(B)** 

(C) 0978

7890 **(D)** 

- Q9. The cube of \(\frac{1}{2}\) is:
  - (A)

**(B)**  $\frac{-}{8}$ 

(C)

**(D)** 

der,

- Q10. 3 - 7 =

(B)

(C)

- (D)
- If 1 is added to the denominator of a fraction, it becomes  $(\frac{1}{2})$  and if 1 is added to the numerator, Q11. the fraction becomes 1. The fraction is:
  - (A)

**(B)** 

(C)

- **(D)**
- How many two-digit numbers are there which are divisible by 6? Q12.
  - (A) 17

(B) 18

(C) 16

- 15 **(D)**
- Q13. A number whose fifth part increased by 5 is equal to its fourth part diminished by 5, is:
  - (A) 160

**(B)** 180

(C) 200

- 220 (D)
- Q14. If  $(5^a)(5^b) = \frac{5^c}{5^d}$ , what is d in terms of a, b and c?

**(B)** 

- **(D)**
- Which of the following is equal to  $(3^8 \times 3^9)^{10}$ ?

  (A)  $3^{720}$ Q15.
  - (A)

3170 **(B)** 

(C)

- 3<sup>98</sup> (D)
- Q16. If 0 , which of the following lists the numbers are in increasing order?
  - $p, \sqrt{p}, p^2$   $\sqrt{p}, p, p^2$

- $p, p^2, \sqrt{p}$  $p^2, p, \sqrt{p}$ **(D)**
- The value of x satisfying  $\sqrt{5+3}\sqrt{x} = 3$  is:
  - (A)

**(B)** 

125 **(C)** 

27 **(D)** 

- If,  $x^x \sqrt{x} = (x\sqrt{x})^x$ , then x =Q18.

**(B)** 

(C)

**(D)** 

- $(16)^{7/4}$  is equal to: Q19.
  - (A)

128 **(B)** 

- None of these (D)
- Q20.  $\frac{4}{5}$  of a number exceeds its  $\frac{2}{3}$  by 8. The number is:
  - (A) 30

**(B)** 

**(C)** 75

- (D)
- Q1.(A) Number of numbers up to 200 which are divisible by 13

$$=\frac{200}{13}=15+\frac{5}{13}, i.e., 15$$

Number of numbers up to 500 which are divisible by 13

$$= \frac{500}{13} = 38 + \frac{6}{13} \text{ i.e., } 38$$

The required numbers = 38 - 15 = 23



ŀ۲,

Hence, the correct answer is choice A.

The first five multiples of 17 are Q2.(B)

$$17 \times 1 = 17$$
  
 $17 \times 2 = 34$   
 $17 \times 3 = 51$   
 $17 \times 4 = 68$   
 $17 \times 5 = 85$ 

First five multiples of 17 are 17, 34, 51, 68 and 85.

The number which is divisible by 7 but not by 14 is 21. Hence, the correct answer is choice A. Q3.(A)

There is only one even prime number, namely 2. Hence, the correct answer is choice C. Q4.(B)

Q5.(C) The least prime number is 2. Hence, the correct answer is choice C.

Q6.(A) 0 is the smallest member of the set W. Hence, the correct choice is A.

Q7.(D) The smallest even number of three digits is 100. The correct choice is choice D.

Q8.(B) Using 0, 7, 8, 9, the smallest number is 0789. Hence, the correct answer is choice B.

Q9.(B) 
$$\left(\frac{1}{2}\right)^3 = \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2}$$
  
=  $\frac{1 \times 1 \times 1}{2 \times 2 \times 2} = \frac{1}{8}$ 

Correct answer is choice B.

Q10.(C) 
$$3 + (-7) = 3 - 7 = -4$$

Correct answer is choice C.

Q11.(C) Let the fraction be  $\frac{x}{y}$ . Then  $\frac{x}{y+1} = \frac{1}{2}$  and  $\frac{x+1}{y} = 1$ 

Let the fraction be 
$$\frac{x}{y}$$
. Then  $\frac{x}{y+1} = \frac{1}{2}$  and  $\frac{x+1}{y} = 1$   
First we solve  $\frac{x}{y+1} = \frac{1}{2}$   $\Rightarrow y+1 = 2x$   $\Rightarrow 2x-y=1$  ...(i)  
Similarly  $\frac{x+1}{y} = 1$   $\Rightarrow x+1=y$   $\Rightarrow x-y=-1$  ...(ii)  
Subtracting (ii) from (i), we have

Similarly 
$$\frac{x+1}{y} = 1$$
  $\Rightarrow x+1=y$ 

$$\Rightarrow x - y = -1$$
 ...(ii

Subtracting (ii) from (i), we have

$$2x - y = 1$$

$$x - y = -1$$

$$x = 2$$

$$x = 2$$
,  $\Rightarrow x - y = -1 \Rightarrow 2 - y = -1 \Rightarrow y = 3$ 

Hence, the required fraction is  $\frac{2}{3}$ .

The correct answer is choice C.

Q12.(D) Required numbers are 12, 18, 24, ..... 96 Here, a = 12 and d = 6

Tn = 96 
$$\Rightarrow a + (n-1)d = 96$$
  
 $\Rightarrow 12 + (n-1)6 = 96$   
 $\Rightarrow 12 + 6n - 6 = 96$   
 $\Rightarrow 6(n+1) = 96$   
 $\Rightarrow n+1 = \frac{96}{6} = 16$   
 $\Rightarrow n = 15$   
Hence, the correct answer is choice D.

Q13.(C) 
$$\frac{x}{5} + 5 = \frac{x}{4} - 5 \implies \frac{x}{4} - \frac{x}{5} = 10$$
  
 $\Rightarrow 5x - 4x = 200$   
 $\Rightarrow x = 200$ 

Hence, the correct answer is choice C.

Q14.(D) 
$$(5^a)(5^b) = \frac{5^c}{5^d}$$
  
 $5^{a+b} = 5^{c-d}$  (By power rule)  
 $\Rightarrow a+b=c-d$   
 $\Rightarrow d=c-a-b$ 

Hence, the correct answer is choice D.

Q15.(B) Given that, 
$$(3^8 \times 3^9)^{10}$$
  
=  $(3^{8+9})^{10}$  (By power rule)  
=  $(3^{17})^{10}$   
=  $3^{17 \times 10}$   
=  $3^{170}$ 

Hence, the correct answer is choice B.

Q16.(D) For any number p, between 0 and 1

Hence, the correct answer is choice D. 
$$p^2 < p$$
 and  $p < \sqrt{p}$ 

Q17.(A) 
$$\sqrt{5 + \sqrt[3]{x}} = 3$$
  
 $5 + \sqrt[3]{x} = 9$  (Squaring both sides)  
 $\sqrt[3]{x} = 9 - 5$   
 $\sqrt[3]{x} = 4$   
 $((x)^{1/3})^3 = (4)^3$   
 $x^{1/3 \times 3} = 4 \times 4 \times 4$   
 $x = 64$ 

Hence, the correct answer is choice A.

Q18.(B) 
$$x^{x}\sqrt{x} = (x\sqrt{x})^{x}$$
$$x^{x}\sqrt{x} = (x \cdot x^{1/2})^{x}$$
$$\Rightarrow x^{x}\sqrt{x} = (x^{3/2})^{x}$$
$$\Rightarrow x^{x}\sqrt{x} = (x^{3x/2})$$
$$\Rightarrow x\sqrt{x} = \frac{3x}{2}$$
$$\Rightarrow \sqrt{x} = \frac{3}{2}$$
$$\Rightarrow \sqrt{x} = \frac{9}{4}$$

Hence, the correct answer is choice B.

Q19.(B) 
$$(16)^{7/4}$$
  
=  $(2^4)^{7/4}$   
=  $2^4 \times 7/4$   
=  $2^7$   
= 128

Hence, the correct answer is choice B.

Q20.(B) 
$$\frac{4}{5}x - \frac{2}{3}x = 8$$

$$\Rightarrow 12x - 10x = 120$$

$$\Rightarrow 2x = 120$$

$$\Rightarrow x = 60$$

Hence, the correct answer is choice B.



Chapter 2

#### MULTIPLICATION AND DIVISION

#### MULTIPLICATION

Multiplication is a short method of adding the same number repeatedly.

#### PROPERTIES OF MULTIPLICATION

1. Multiplication is commutative for rational numbers. Example:

$$\frac{a}{b} \times \frac{c}{d} = \frac{ac}{bd} = \frac{c}{d} \times \frac{a}{b}$$
$$\frac{2}{3} \times \frac{5}{7} = \frac{10}{21} = \frac{5}{7} \times \frac{2}{3}$$

2. Multiplication is associative for rational numbers.

Example:

$$\frac{a}{b} \times \left(\frac{c}{d} \times \frac{e}{f}\right) = \frac{ace}{bdf} = \left(\frac{a}{b} \times \frac{c}{d}\right) \times \frac{e}{f}$$
$$\frac{2}{3} \times \left(\frac{5}{7} \times \frac{11}{13}\right) = \frac{110}{273} = \left(\frac{2}{3} \times \frac{5}{7}\right) \times \frac{11}{13}$$

3. Multiplication is distributive over addition and subtraction for rational numbers. Example:

$$\frac{a}{b} \times \left(\frac{c}{d} \pm \frac{e}{f}\right) = \frac{a}{b} \times \frac{c}{d} \pm \frac{a}{b} \times \frac{e}{f}$$

$$\frac{2}{3} \times \left(\frac{5}{7} \pm \frac{11}{13}\right) = \frac{2}{3} \times \frac{5}{7} \pm \frac{2}{3} \times \frac{11}{13}$$

- 4. For any rational number  $\frac{x}{y}$ ,  $\frac{x}{y} \times 1 = \frac{x}{y} = 1 \times \frac{x}{y}$ , one is called multiplicative identity.
- 5. Two rational numbers  $\frac{a}{b}$  and  $\frac{b}{a}$  are the multiplicative inverses of each other.

$$\frac{\mathbf{a}}{\mathbf{b}} \times \frac{\mathbf{b}}{\mathbf{a}} = 1 = \frac{\mathbf{b}}{\mathbf{a}} \times \frac{\mathbf{a}}{\mathbf{b}}$$

Note: The sign of the product is +ive, if there are an even number of negative factors or there are no negative factors. The sign of the product is -ive, if there are an odd number of negative factors

#### DIVISION

The process of subtraction of the same number form a given number for a few times is called division (+), i.e.,  $6 \div 2 = 3$ 

(2 can be subtracted 3 times from 6)

#### IMPORTANT POINTS

1. Division is the inverse operation of multiplication. For example  $6 \div 2 = 3$  means to find the number by which 2 should be multiplied so as to obtain 6.

Because 
$$3 \times 2 = 6$$
  
Therefore,  $6 \div 2 = 3$ 

- 2. When a number is divided by another number, the first number *i.e.* the number which is being divided is called the *dividend*, the second number which divides is called the *divisor* and the number obtained as a result of division is called the *quotient*. In the above example, 6 is the dividend, 2 is the divisor and 3 is the quotient.
- 3. The operation of division starts from the left whereas the operations of addition, subtraction and multiplication start from the right.

Divisibility:

The following table gives the rules to test the divisibility from 2 to 19.

Divisibility by	If	Example
2	Any number in the unit's place which is either even or zero.	12, 10, 26, 32, 38, 567992, 11110234
3	The sum of digits is divisible by 3.	321:3+2+1=6 is divisible by 3.
4	The last two digits of a number is divisible by 4.	725324 : 24 is divisible by 4.
5	The number ends with 5 or zero.	4112370, 5321095, 3331210, etc.
6	A number is divisible by 2 and the sum of the digits of the number is multiple of 3.	342, 63924, 154, 261 etc.
8 /	The last three digits of a number is divisible by 8. or The last three digits of a number are zero.	2125000, 135923120, 7792320, 1256, etc.
	The sum of all the digits of a number is divisible by 9.	33456735 : 3 + 3 + 4 + 5 + 6 + 7 + 3 + 5 = 36 divisible by 9.
10	Any number which ends with zero.	70, 789790, 7111130, 5773313570, 112300100 etc.
— II — — — — — — — — — — — — — — — — —	The sum of digits at odd and even places are respectively equal or differ by a number divisible by 11.	4235682 : Sum $1 = 4 + 3 + 6 + 2 = 15$ Sum $2 = 2 + 5 + 8 = 15$ Sum $1 = \text{Sum } 2$ , the number is divisible by 11. or 283712 : Sum $1 = 2 + 3 + 1 = 6$ and Sum $2 = 8 + 7 + 2 = 17$ , their differ $17 - 6 = 11$ is divisible by 1.
12	The number which is divisible by both 4 and 3.	135792 etc.
1. 14	The number which is divisible by both 2 and 7.	98, 504 etc.
15	The number which is divisible by 3 and 5.	360, 733352215 etc.
16	The number whose last 4 digit number is divisible by 16.	253421020, 27954204 etc.
18	Any number which is divisible by 9 and has its last digit even (or zero).	2709360, 252630 etc.
25	The number formed by the last two digits of the number is divisible by 25.	257275, 25277750 etc.

#### Model Examples:

Q1. Multiply 63987 by 91763 is not more than 3 lines. Solution:

Q2. Find the number, one-sixth of which exceeds its one-ninth by 654. **Solution:** Let the number be x

$$\frac{x}{6} - \frac{x}{9} = 654$$

$$\frac{x}{18} = 654$$

 $\Rightarrow x = 654 \times 18 = 11772 \qquad \text{Ans.}$ 

Q3. Find the quotient and remainder when  $x^2 + bx - 5$  is divided by x + 1. For what value of 'b' will the remainder be zero?



Solution:

$$x + 1)x^{2} + bx - 5(x + (b - 1))$$

$$x^{2} + x$$

$$- (b - 1)x - 5$$

$$(b - 1)x - 1 + b$$

$$- (4 - b)$$
ent =  $x + b - 1$  Ans.

So Quotient = x + b - 1 Ans.

Remainder  $\approx -(b+4)$ 

For remainder = 0

$$-b - 4 = 0$$

$$\Rightarrow b = -4$$

 $\Rightarrow b = -4$ Q4. The speed of mail train is 1,370 meters per minute. Express it in miles per hour correct to three significant figures, given that 1 metre = 39.37 inches.

Solution: Speed of mail train = 1,370 metres per minute

$$= \frac{1370 \times 60 \times 39.37}{12 \times 3 \times 1760}$$
 miles per hour

51.077 miles per hour Ans.

Q5. A boy when asked to multiply a number by 7/8, divided this instead, by 7/8 and found the answer  $1\frac{1}{14}$  too great. Find the number and the correct answer.

Solution: Let the number be 'x'

$$(x \div \frac{7}{8}) - \left(x \times \frac{7}{8}\right) = \frac{15}{14}$$

$$\frac{8x}{7} - \frac{7x}{8} = \frac{15}{14}$$

$$\frac{64x - 49x}{56} = \frac{15}{14}$$
or
$$\frac{15x}{56} = \frac{15}{14}$$

$$\therefore \qquad x = \frac{56 \times 15}{14 \times 15} = 4 \quad \text{Ans.}$$

Correct answer =  $4 \times \frac{7}{8} = 3\frac{1}{2}$ Ans.

Q6. The sum of the squares of two consecutive integers is 1105. Find the integers and check your answer. Solution: Let the two consecutive positive numbers be:

$$x, x + 1$$

Then sum of the squares of these consecutive numbers = 1.105

$$x^{2} + (x+1)^{2}. = 1105$$

$$x^{2} + x^{2} + 2x + 1 = 1105$$

$$2x^{2} + 2x - 1104 = 0$$

$$x^{2} + x - 552 = 0$$
or
$$x^{2} + 24x - 23x - 552 = 0$$

$$x(x+24) - 23(x+24) = 0$$

$$(x-23)(x+24) = 0$$

$$\Rightarrow x = 23 \text{ or } x = -24$$

As the two consecutive numbers are +ve integers, therefore, we neglect the -ve number. Thus the two consecutive numbers are 23 and 24. Ans.

#### Chapter 3

#### HIGHEST COMMON FACTOR & LEAST COMMON MULTIPLE

The highest common factor of two or more numbers is the greatest number which divides each of them exactly.

#### Methods of finding H.C.F.

#### (i) By Prime Factors.

Resolve the given number into their prime factors. The product of all prime common factors is known as H.C.F.

#### Model Example

Find the H.C.F. of 630, 1050 and 1260.

Solution:

$$630 = 2.3.3.5.7$$

$$1050 = 2.3.5.5.7$$

$$1260 = 2.2.3.3.5.7$$

$$\therefore$$
 H.C.F. is 2.3.5.7 = 210. Ans.

#### (ii) By Division:

Find the H.C.F. of 5133 and 3953

#### Various Steps:

Step I. Dividing the greatest number by the lesser, we get the remainder 1180.

Step II. Dividing the previous divisor 3953 by 1180, we get the remainder 413.

Step III. Dividing the previous divisor 1180 by 413 we get the remainder 354.

Step IV. Dividing the previous divisor 413 by 354 we get the remainder 59.

Step V. Dividing the previous divisor 354 by 59 we get no remainder.

The last divisor 59 is the H.C.F.

H.C.F. is also known as Greatest Common Measure (G.C.M.)

#### LEAST COMMON MULTIPLE (L.C.M)

The Least Common Multiple of two or more given numbers is the least number which is exactly divisible by each of them.

#### Methods of Finding L.C.M.

(i) By Factors. Resolve the given numbers into prime factors, and find the product of the highest powers of all the factors that occur in the given number. The product will be the required L.C.M.

#### Model Example

Q1. Find the L.C.M. of 70, 80, 90.

Solution:

$$70 = 2 \times 5 \times 7$$

$$80 = 2^4 \times 5$$

$$90 = 2 \times 3^2 \times 5$$

L.C.M. = 
$$2^4.3^2.5.7 = 5040$$
 Ans.

- (ii) With the help of H.C.F. The product of two numbers is equal to the product of their L.C.M. and H.C.F.
  - .. L.C.M. of two numbers
    - = Product of numbers

H.C.F.



#### L.C.M. and H.C.F. of Factions.

L.C.M. of two or more fractions

L.C.M. of numerators H.C.F. of denominators

H.C.F. of two or more fractions

L.C.M. of numerators
H.C.F. of denominators

#### Model Examples

Q1. The H.C.F. of two numbers is 34 and their L.C.M. is 4284. If one of the numbers is 204, find the other.

Solution:

As product of 2 numbers

= their H.C.F. × L.C.M.

The other number is = 
$$\frac{34 \times 4284}{204}$$

=714 Ans.

Q2. What is the highest number of four digits which will leave a remainder of 1 when divided by any of numbers 6, 9, 12, 15, or 18?

Solution:

f

F.

L.C.M. of 6, 9, 12, 15, 
$$18 = 180$$

Greatest no. of 4 digits = 9999

Greatest no. of 4 digits divisible by

$$180 = 9999 - 99 = 9900$$

Read. No. = 
$$9900 + 1 = 9901$$

Q3. Three men A, B and C go walking round a circle one mile in circumference at the rates of 160, 120 and 105 yards per minute, respectively. If they all start together and walk in the same direction, when will they first be together again?

Ans.

Solution: Circumference of the circle

= 1 mile or 1760 yds.

A will complete the circle in

$$=\frac{1760}{160}=11\,\mathrm{min}.$$

B will complete the circle in

$$=\frac{1760}{120}=\frac{44}{3}$$
 min.

C will complete the circle in

$$=\frac{1760}{105}=\frac{352}{21}\,\mathrm{min}.$$

L.C.M. of 11, 
$$\frac{44}{3}$$
,  $\frac{352}{21}$  = 352 minutes.

i.e., they will be together again first after 352 min. or 5 hrs. 52 min. Ans.

## Multiple Choice Questions (MCQs)-

- Q1. A neon sign flashes every 3 seconds, another sign flashes every 5 seconds, and a third flashes every 7 seconds. If they all flash together, how many seconds will pass before they all flash simultaneously again?
  - (A) 15 seconds

(B) 35 seconds

(C) 105 seconds

(D) 21 seconds

5

Q2. The greatest number which exactly divides 1155 and 735 is:

(A) 2

3)

(D)

**(B)** 

The chairs in the school hall can be set out in 35 equal rows or in 45 equal rows or in 105 equal

0.16

400

**(C)** 

(A)

rows are:

Q15.

0.48m

600

**(D)** 

Three bells toll after intervals of 6, 9 and 15 minutes, respectively. If they toll together at 5 p.m., Q16. when will they toll together next?

(A) 6:30 **(B)** 5:30

(C) 6:45

(D.) 5:45

Q1. (C) The L.C.M of 3,5 and 7 will give the answer

 $=3\times5\times7=105$ 

Q2. (D) The required number is the H.C.F of 1155 and 735

The greatest number required is 105.

The least number which is completely divided by 35, 45 and 55, is their L.C.M. which is 3465. Q3. We want to find the least number which on dividing by 35, 45 and 55 leave remainders 25, 35 and 45 respectively i.e., 10 less than the quotient in each case. Hence such a number is 3465 -10 = 3455

Q4. (C)

2	12-20 - 24-32
2	6 - 10 - 12 - 16
2	3 - 5 - 6 - 8
2	3 - 5 - 3 - 4
2	3 - 5-3 - 2
3	3 - 5 - 3 - 1
5	1-5-1-1
,	1 - 1 - 1 - 1

The L.C.M. of 12, 20, 24 and 32 is

$$2^5 \times 3 \times 5 = 32 \times 3 \times 5 = 480$$

Q5. One edge of the minimum cube must be 24 cms, the least common multiple of 6, 12 and 24. Thus, it will have a volume of  $24 \times 24 \times 24$  cubic centimeters which is equal to 8 bricks

$$i.e., \qquad \frac{24 \times 24 \times 24}{6 \times 12 \times 24} = 8$$

Q6. (A) Product of two numbers  $= L.C.M \times H.C.F$ 

$$18 \times 2 \text{nd number} = 150 \times 30$$

$$2 \text{nd number} = \frac{150 \times 30}{18}$$

$$= 250$$

Q7. (A)Product of two numbers =  $L.C.M \times H.C.F$ 

2500 = 
$$125 \times \text{H.C.F}$$
  
H.C.F =  $\frac{2500}{100}$ 

Q8. (C) The question asks for the first time they will finish at the same time. So, we must find least common multiple

 $6 \times 5 \times 5 = 150 \text{ minutes}$ 

= 2:30 hours So they will finish marking at 1:30 PM.

Q9. (D) The HCF of 153 and 204 gives the wanted length

_3_	153
_3	51
17	17
	1

2	204
2	102
3 .	51
17	17
	1

$$153 = 3 \times (3) \times \boxed{17}$$

$$204 = 2 \times 2 \times \cancel{3} \times \cancel{17}$$

$$HCF = 17 \times 3 = 51$$

Greatest length = 51cm

Q10. (B) The HCF of 477, 2412 and 639 gives the wanted length.

_3	477	
_3	159	
	53	
		•

2	2412		3	639
_2	1206		3	213
3	603			71
3	201	•		
	67			

$$477 = 3 \times 3 \times 53$$

$$2412 = 2 \times 2 \times 3 \times 3 \times 3 \times 67$$

$$639 = 3 \times 3 \times 71$$

H.C.F = 
$$3 \times 3 = 9$$

Q11. (D) The number which is divisible by 18, 24, 30 and 36 is divisible by their L.C.M

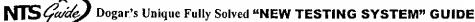
L.C.M = 
$$2 \times 2 \times 2 \times 3 \times 3 \times 5 = 360$$

The greatest number of 4-digits is 9999. Now we find the greatest multiple of 360 less than 9999.

Thus 9999 - 639 = 9360 is exactly divisible by 360. But the required number leaves a remainder of 17 in each case. Hence, the number is

$$9360 + 17 = 9377$$

**Q12.** (C) Required number = L.C.M of 12, 15, 18



 $L.C.M = 2 \times 2 \times 3 \times 3 \times 5 = 180$ 

The required least number = 180 + 5 = 185

Q13. (D). As 48 and 60 remainders when 2400 and 3600 are divided by the numbers 2400 - 48 = 2352

3600 - 60 = 3540 must be exactly divisible by the number.

The H.C.F of 2352 and 3540 is the required number.

- The H.C.F of 2350 and 3540 is 10.
- The required greatest number is 10.

Q14. (C)

$$0.96 \div 2 = 0.48$$
m

Q15.

$$= 5 \times 5 \times 8 \times 3 = 600$$
 chairs

Q16. (A)

L.C.M of 6, 9 and 15 = 
$$3 \times 2 \times 3 \times 5$$
  
= 90

The bells will toll after 90 minutes, it mean at 6:30.

#### Chapter 4

#### **SQUARE ROOT**

Methods of Finding Square Root:

- (i) By Factors. Resolve the number into its prime factors. The square root is the product of the prime factors taken half as many times as they occur in the number.
- (ii) By Division.

Model Example

Find the square root of 2480625.

Solution:

1	2480625	(1575
	1	
25	148	
	125	
307	2306	
	2149	
3145	15725	•
	15725	
	×	

Ans. 1575

Q2. Find the square root of 43.45 to four decimal places.

Solution:

6	43.45	(6:5916
t-	36	
125	7.45	
	6.25	
1309	12000	
•	1178	81
13181	21900	
	131	.81
131826	871900	
	79	0956
		80944

As remainder is more than half 6.5917

Ans.

Q3. Find the value of  $\sqrt{\frac{2+\sqrt{3}}{2-\sqrt{3}}}$  correct to three decimal places.

etion: 
$$\sqrt{\frac{2+\sqrt{3}}{2-\sqrt{3}}} = \sqrt{\frac{(2+\sqrt{3})(2+\sqrt{3})}{(2-\sqrt{3})(2-\sqrt{3})}}$$
 (Rationalization)
$$= \sqrt{\frac{(2+\sqrt{3})^2}{(2)^2-(\sqrt{3})^2}}$$
$$= \sqrt{\frac{(2+\sqrt{3})^2}{4-3}} = 2+\sqrt{3} = 2+1.732$$

#### Unitary Method and Chain Rule

#### IMPORTANCE:

The unitary method and chain rule have quite an importance in our daily life. It is explained by the following model examples.

#### Model Examples:

Q1. In a kilometer race A can beat B by 40 metres and B can beat C by 50 metres. How many metres can A beat C in a 500 metres race?

Solution:

When A covers 1000 m.

B covers 1000 - 40 = 960 m.

and

When B covers 1000 m.

C covers 1000 - 50 = 950 m.

.. When B covers 960 m.

C covers 
$$\frac{950}{1000} \times 960 \,\text{m} = 912 \,\text{m}.$$

i.e., when A covers 1000 m. C covers  $\frac{912}{2}$ 

$$=456 \text{ m}$$

or when A covers 500 m. race, A will beat C by = 500 - 456 = 44 m.

Q2. Divide Rs. 510 between A, B and C so that A gets 2/3 of what B gets and B gets ¼ of what C gets. Find the share of each.

Solution: Let C's share be Rs. x

: B's // // = 
$$\frac{x}{4}$$
  
A's // // =  $\frac{2}{3} \times \frac{x}{4} = \text{Rs.} \frac{x}{6}$ 

Total amount = Rs. 510

$$\therefore \qquad x + \frac{x}{4} + \frac{x}{6} = 510$$

$$\frac{12x + 3x + 2x}{12} = 510$$

$$x = \frac{12 \times 510}{17} = 360$$

Q3. Divide Rs. 600 among A, B, and C so that Rs. 40 more than 2/5 of A's share, Rs. 20 more than 2/7 of B's share, Rs. 10 more than  $\frac{9}{17}$  of C's share may be equal.

Solution: Let  $\frac{2}{5}$  of A's share + Rs.  $40 = \frac{2}{7}$  of B's share + Rs.  $20 = \frac{9}{17}$  of C's share + Rs. 10 be = x.

$$\therefore \frac{2}{5} \text{ of A's share} = x - 40$$

or A's share = 
$$\frac{5}{2}(x-40)$$

Similarly B's share = 
$$\frac{7}{2}(x-20)$$

C's share = 
$$\frac{17}{9}(x-10)$$

As total amount = Rs. 600

$$\frac{5x-200}{2} + \frac{7x-140}{2} + \frac{17x-170}{9} = 600$$

$$\frac{45x - 1800 + 63x - 1260 + 34x + 340}{100} = 600$$

or 
$$142x - 3400 = 600 \times 18 = 10800$$

$$142x = 10800 + 3400 = 14200$$

$$x = \frac{14200}{142} = 100$$

A's share 
$$=\frac{5}{2}(100-40) = \text{Rs. } 150$$

B's share = 
$$\frac{7}{2}(100-20)$$
 = Rs. 280 Ans.

C's share = 
$$\frac{17}{9}(100-10) = \text{Rs. } 170$$

Q4. A garrison has enough provision for 52 days. After 20 days, a reinforcement of 400 men arrives and the food would then last for 24 days only. How many men were there in the garrison originally?

Solution: Let there be x men in the garrison originally. After 20 days no. of men = x + 400. If these men had not joined, the provision would have lasted for 50 - 20 = 32 days more.

For x men the provision can last for 32 days

11 32r 11

For (x + 400) men of provision can last for  $\frac{32x}{x + 400}$  days

But provision lasted for 24 days

$$\therefore \frac{32x}{x+400} = 24$$

$$32x = 24x + 9600$$

$$8x = 9600$$

x = 1200 men. Ans.

# Multiple Choice Questions (MCQs)

- Q1. What is the least positive integer which is to be added to 57592910 so that the sum may be a perfect square?
  - (A) 7588

(B) '

(C)

- (D) 15166
- Q2. A rectangular field which is twice as long as it is broad, has an area of 14450 m<sup>2</sup>, what is its perimeter?
  - (A) 85 m

(B) 510 m

(C) 165 m

- **(D)** 170 m
- Q3. The cost of the planting sugarcane at the rate of 6 paisa per square meter is Rs. 5840.64. What is the length of side of this square field:
  - (A) 312 m

(B) 622 m

(C) 97344 m

- **(D)** 459 m
- Q4. What is the smallest number which when subtracted from 1.00060219 gives a perfect square number?
  - (A) 0.00210

(B) 210

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# Explanatory Answers

Q1. (C) 57592910 is greater than the square of 7588 (using calculator). The next squared is the square of 7589.  $(7589)^2 = 57592921$ .

Now 57592921 - 57592910 = 11, which is the required integer to be added.

Q2. (B) As the length is twice as long as width and so its rectangle can be divided into 2 square regions

The area of each square region 
$$=\frac{14450}{2} = 7225 \text{m}^2$$

Now length of each region = Width of the field  $\times 2$ 

$$= \sqrt{7225}$$
= 85 m
= 85 × 2 = 170m
Perimeter = 2(170 + 85)
= 2(255)

$$= 2(255)$$
  
= 510m

Q3. (A) Cost = Rs. 5840.64 = 584064 paisas

Area = 
$$\frac{584064}{6}$$
 = 97344

Side = 
$$\sqrt{97344}$$
  
= 312 m

Q4. (C)

There are eight places after the decimal in the given number, so after subtracting .0000021 from the given number the remainder would be zero. So .0000021 is the required number.

**Q5.** (A) 
$$313 \times 313 = 97969$$

Q6. (D) Side length 
$$= 6 \text{cm}$$

Sides of 256 square shapes =  $\sqrt{256} = 16$ 

Size of the square is  $= 16 \times 6 = 96$ 

Number of students in front row =  $\sqrt{9224 - 8}$ =  $\sqrt{9216}$ = 96

Q8. (B) The first two integers those square end with 9 are 3 and 7.

The difference between there is

$$49 - 9 = 40$$

**Q9.** (C) Suppose breadth 
$$= x$$

Length = 
$$10x$$

Area = 
$$(10x) \times (x) = 75690$$

$$10x^2 = 75690$$

$$x^2 = 7569$$

$$\Rightarrow$$
  $x = 87 = breadth$ 

$$10x \approx 870 = \text{length}$$

Perimeter = 
$$2(Length + breadth)$$

$$=2(87 + 870)$$

$$= 1914 \text{ m}$$

Q10. (C) Side of each square = 
$$\sqrt{0.25} = 0.5$$
km

Length of the railings = 
$$(.5 + .5)2 = 2km$$

$$= 2 \times 1000 = 2000 \text{ m}$$

Cost of railing = 
$$2000 \times 101 = \text{Rs.} 202000$$

**Q11.** (B) Size of the square sheet = 
$$2.1 \text{m} = 2.1 \times 100 = 210 \text{cm}$$

Area of square root 
$$= 210 \times 210$$

$$= 44100 \text{ cm}^2$$

So, No. of 1cm square pieces will be  $= 1 \times 44100 = 44100$ 

Q12. (C)

Let the width = b, then length = 2b

Area = 
$$b \times 2b = 2b^2$$

$$2b^2 = 1152 \text{ (given)} \implies b^2 = 576$$

$$b = \sqrt{576} = 24$$

length = 
$$2b \Rightarrow \text{length} = 2 \times 24 = 48$$

Perimeter of the field 
$$= 2(24 + 48)$$

$$=2(72)=144m$$

Q13. (D) There is no way to simplify 
$$\sqrt{x^2 + y^2}$$
.

Q14. (C) 
$$\sqrt{\frac{a^2}{16} + \frac{a^2}{25}} = \sqrt{\frac{25a^2 + 16a^2}{400}} = \sqrt{\frac{41a^2}{400}} = \frac{a\sqrt{41}}{20}$$

Q15. (A) 
$$\sqrt{24a} \times \sqrt{6a}$$

$$=\sqrt{144a^2}$$

n the

# Chapter 5

# FRACTIONS AND DECIMALS

# FRACTIONS:

If any unit be divided into any number of equal parts, one or more of these parts is called a fraction of the unit.

**Example:** The fractions one-fourth, two-third and three-fourth are respectively written as  $\frac{1}{4}$ ,  $\frac{2}{3}$  and  $\frac{3}{4}$ 

# NUMERATOR AND DENOMINATOR:

The upper number, which shows the number of parts taken to form the fraction, is called numerator.

The lower number, which indicates the number of equal parts in which the unit is divided, is called denominator.

# Terms of The Fraction:

The numerator and the denominator of a fractions are called its terms.

Note: A fraction is also called a rational number.

# Lowest Terms of a Fraction:

When the numerator and the denominators of a fraction have no common factor, the fraction is said to be is its lowest terms:

Example: 
$$= \frac{6}{10} = \frac{3 \times 2}{5 \times 2}$$

In the above example denominator and the numberator have a common factor, thus  $\frac{6}{10}$  is not is its lowest

terms. If we cancel out 2 by dividing numerator and denominator by 2 we find  $\frac{3}{5}$ , which has no common factor.

hence  $\frac{3}{5}$  is in its lowest terms.

# **Proper Fraction:**

A proper fraction is one whose numerator is less than the denominator.

Example: 
$$\frac{2}{3}$$
,  $\frac{5}{7}$ ,  $\frac{23}{46}$  are proper fractions.

Note: The value of proper fractions is always less than 1

# IMPROPER FRACTION:

A fraction whose numerator is equal to or greater than the denominator is called improper fraction.

Example: 
$$\frac{15}{13}$$
,  $\frac{13}{5}$ , and  $\frac{21}{14}$  are improper fractions.

Note: The value of an improper fractions is always more than as equal to I

# Mixed Fraction:

When an improper fraction is changed to consist of a whole number and a fraction, it is called a mixed fraction.

**Example:** The improper fraction  $\frac{15}{13}$  can be written as  $\frac{2}{13}$ , which is a mixed fraction.

# Compound Fraction:

A fractions of a fraction is called a compound fraction.

Example:  $\frac{1}{3}$  of  $\frac{3}{5}$  is a compound fraction.

Thus 
$$\frac{1}{3}$$
 of  $\frac{3}{5} = \frac{1}{3} \times \frac{3}{5} = \frac{1}{5}$ 

# Complex Fractions:

A complex fraction is one in which the numerator or denominator or both are fractions.

**Example:**  $\frac{3/2}{5}$ ,  $\frac{3}{2/5}$ ,  $\frac{2/5}{3/7}$  and  $\frac{1/3 + 1/2}{2/3 - 1/5}$  are complex fractions.

Example 1: One third of one-seventh of a plot is sold Rs. 45000. What is the value of six-twnety fifth of the plot.

**Solution:** One third of one seventh  $=\frac{1}{3} \times \frac{1}{7} = \frac{1}{21}$ 

Now,  $\frac{1}{21}$  of a plot costs = Rs. 45000.

$$\frac{6}{25} \text{ of the plot will cost} = \frac{45000}{1/2} \times \frac{6}{25}$$

$$45000 \times 21 \times 6$$

Example 2: A sum of money increased by its sixth part amount to Rs. 56. Find the sum.

Solution: Let x be the amount of money, thus

$$x + \frac{x}{6} = 56 \implies \frac{6x + x}{6} = 56$$

$$\Rightarrow \frac{7x}{6} = 56$$

$$\Rightarrow 7x = 56 \times 6$$

$$\Rightarrow x = \frac{56 \times 6}{7} = 48$$

# **VULGAR FRACTIONS**

In questions of fractions signs +, -,  $\times$ , +, "of" ('of' signifies multiplication) and brackets are often involved. In simplifying these questions the following order must be followed:

# IMPORTANT POINTS

- (i) Remove the brackets.
- (ii) Then quantities which are connected by 'of' should be simplified.
- (iii) Then division and multiplication are carried out.
- (iv) Operation of addition and subtraction are performed at last.

Note: The above rules can be easily remembered by the word 'BODISA' of which 'B' stands for brackets, O for 'of', D for division, I for into, S for subtraction and A for addition.

Model Examples:

Example 3: 
$$7\frac{1}{2} - \frac{1}{9} \left[ 3\frac{3}{4} + \left\{ \frac{5}{6} \text{ of } \frac{2}{3} \left( \frac{1}{3} - \frac{1}{4} - \frac{1}{6} \right) \right\} \right]$$

Solution:

$$= 7\frac{1}{2} - \frac{1}{9} \left[ \frac{15}{4} \div \left\{ \frac{5}{6} \text{ of } \frac{2}{3} \left( \frac{1}{3} - \frac{3 - 2}{12} \right) \right\} \right]$$

$$= 7\frac{1}{2} - \frac{1}{9} \left[ \frac{15}{4} \div \left\{ \frac{5}{6} \text{ of } \frac{2}{3} \left( \frac{1}{3} - \frac{1}{12} \right) \right\} \right]$$

$$= 7\frac{1}{2} - \frac{1}{9} \left[ \frac{15}{4} \div \left\{ \frac{5}{6} \text{ of } \frac{2}{3} \left( \frac{3}{12} \right) \right\} \right]$$

$$= 7\frac{1}{2} - \frac{1}{9} \left[ \frac{15}{4} \div \left\{ \frac{5}{6} \text{ of } \frac{1}{6} \right\} \right]$$

$$= 7\frac{1}{2} - \frac{1}{9} \left[ \frac{15}{4} \div \frac{5}{36} \right]$$

$$= 7\frac{1}{2} - \frac{1}{9} \left[ \frac{15}{4} \times \frac{36}{5} \right]$$
$$= 7\frac{1}{2} - \frac{1}{9} \times 3 \times 9 = 7\frac{1}{2} - 3 = 4\frac{1}{2} \text{ Ans.}$$

Example 4: Simplify

$$\frac{\frac{1}{6} + \frac{5}{12} \times \left(\frac{4}{5} - \frac{5}{7}\right)}{\frac{3}{4}if1\frac{2}{3} - \frac{3}{5}of1\frac{4}{7}} \div \frac{\frac{1}{3} + \frac{1}{7} - \frac{2}{5}}{\frac{1}{5} + \frac{1}{9} - \frac{2}{7}}$$

Solution:

$$= \frac{\frac{1}{6} + \frac{5}{12} \times \left(\frac{4}{5} - \frac{5}{7}\right)}{\frac{3}{4} \times \frac{5}{3} - \frac{3}{5} \times \frac{11}{7}} \cdot \frac{\frac{1}{3} + \frac{1}{7} - \frac{2}{5}}{\frac{1}{5} + \frac{1}{9} - \frac{2}{7}}$$

$$= \frac{\frac{1}{6} + \frac{5}{12} \times \left(\frac{28 - 25}{35}\right)}{\frac{5}{4} - \frac{33}{35}} \cdot \frac{\frac{35 + 15 - 42}{105}}{\frac{63 + 35 - 90}{315}}$$

$$= \frac{\frac{1}{6} + \frac{1}{28}}{\frac{5}{4} - \frac{33}{35}} \cdot \frac{8}{105} \times \frac{315}{8}$$

$$= \frac{\frac{1}{6} + \frac{1}{28}}{\frac{5}{4} - \frac{33}{35}} \cdot \frac{8}{105} \times \frac{315}{8}$$

$$= \frac{14 + 3}{\frac{175 - 132}{140}} \div 3 = \frac{17}{84} \times \frac{140}{43} \times \frac{1}{3}$$

$$= \frac{85}{387} \text{ Ans.}$$

# Continued Fraction:

The fractions of the form 
$$a + \frac{b}{c + \frac{d}{e + \frac{f}{a}}}$$

etc. are known as continued fractions where a, b, c, ...... etc., are any numbers.

Note: In order to simplify such fractions, we begin with the lowest part and proceed step by step, upwards.

# Model Examples:

Example 5: Simplify:

$$\left\{1 + \frac{1}{2 + \frac{2}{3 + \frac{3}{4}}}\right\} \div \left\{\frac{4}{4 + \frac{4}{3 + \frac{3}{2}}}\right\}$$



Solution:

$$\left\{1 + \frac{1}{2 + \frac{2}{15}}\right\} \div \left\{\frac{4}{4 + \frac{4}{9}}\right\}$$

$$= \left\{1 + \frac{1}{2 + \frac{8}{15}}\right\} \div \left\{\frac{4}{4 + \frac{8}{9}}\right\}$$

$$= 1 + \left\{\frac{1}{\frac{38}{15}}\right\} \div \left\{\frac{4}{\frac{44}{9}}\right\}$$

$$= \left\{1 + \frac{15}{38}\right\} \div \left\{\frac{36}{44}\right\}$$

$$= \frac{53}{38} \times \frac{44}{36} = \frac{583}{342} \qquad \text{Ans.}$$

# DECIMAL FRACTION

A fraction involving decimal point is called decimal fraction.

# Conversion of a decimal fraction into vulgar fraction:

Rule. Write down the given number in the numerator omitting the decimal point and for the denominator write I followed by as many zeroes as there are figures on the right of the decimal point.

As 
$$46.76 = \frac{4676}{100}$$
 and 
$$199.0083 = \frac{1990083}{10000}$$

Model Example

Q1. Simplify

$$\frac{0.1 \times 0.1 \times 0.1 + 0.01 + 0.01 \times 0.01}{0.2 \times 0.2 \times 0.2 + 0.08 + 0.04 \times 0.02}$$

Solution:

$$= \frac{\frac{1}{10} \times \frac{1}{10} \times \frac{1}{10} + \frac{1}{100} + \frac{1}{100} \times \frac{1}{100}}{\frac{2}{10} \times \frac{2}{10} \times \frac{2}{10} + \frac{8}{100} + \frac{4}{100} \times \frac{2}{100}}$$
$$= \frac{\frac{1}{1000} + \frac{1}{100} + \frac{1}{10000}}{\frac{8}{1000} + \frac{8}{1000} + \frac{8}{10000}}$$

$$= \frac{\left(\frac{1}{1000} + \frac{1}{100} + \frac{1}{10000}\right)}{8\left(\frac{1}{1000} + \frac{1}{100} + \frac{1}{10000}\right)}$$
$$= \frac{1}{8} \quad \text{Ans.}$$

# Multiple Choice Questions (MCQs)

Q1.	If $\frac{5}{x}$ , $\frac{8}{x}$ , and $\frac{13}{x}$	are all in lowest terms. Then how many integers, x, between 30	and 40?
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(A) 5

**(B)** 

**(D)** 

Q2. 
$$\frac{6}{6} \times \frac{6}{12} \times \frac{6}{18} \times \frac{6}{24} \times \frac{6}{30}$$
 equals:

(A)  $\frac{1}{120}$ 

**(B)** 

(C)  $\frac{1}{30}$ 

**(D)** 

(D) None of these

Q3. If 
$$\frac{4}{13}$$
 of a number is 39, what is  $\frac{8}{13}$  of that number?

(A)  $\frac{39}{4}$ 

**(B)** 

(C) 16

<u>39</u> 8 **(D)** 

# Q4. $\frac{3}{4}$ of 28 is equal to $\frac{30}{7}$ of what number?

(A)

**(B)** 

(C) 30

56 **(D)** 

(D) None of these

# Q5. Which of the following is less than $\frac{5}{11}$ ?

(A)  $\frac{3}{2}$ 

(C)

**(D)** 

**(D)** None of these

### Q6. There are 20 boys in a class. Five of them are left-handed. What fraction of the class is left handed?

(A)

(B)

(C)

**(D)** 

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Q7.	A chemic solution?	al solution contains 8%	of acid. If there is 15	5ml of acid, what is the	volume of th
	(A)	125.5 mL	(B)	187.5 mL	
	(C)	225.5 mL	(D)	171.5 mL	
Q8.	What frac	ctional part of a week is 9	98 hours?		
	(A)	$\frac{7}{98}$	(B)	712	
	(C)	$\frac{1}{20}$	(D)	$\frac{1}{2}$	
Q9.				1	
ue.	candidate to win?	must gain at least 50% (	m 7% usually forget to f the remaining votes.	to vote. In order to win How many votes does he	an election, a need in orde
	(A)	2725	(B)	410	
	(C)	5450	(D)	None of these	
Q10.	What frae	tion is exactly midway be	4		
		_	3 4	7	
	(A)	$\frac{7}{12}$	(B)	$\frac{7}{24}$	
	(0)	<u>29</u> 11		1	
	(C)	, - "	(D)	$\frac{1}{2}$	
ົລ11.	$\frac{4}{9}$ of a num	ber is 12. What is the nu	mber?		
	(A)	27	(B)	36	
	(C)	18	(D)	16	
212,	Ali purelia	sed some goldfish. Durin		bem died, and during the	والمحادد المحاد
	$\frac{3}{9}$ of those s	still alive at the end of th	e first week died. What	t is the fraction of the orig	sccond week,
	still alive a	fter two weeks?		y man it worken of the drift	inai golulian
			•	3	
	(A)	$\frac{1}{2}$	(B)	$\frac{3}{2}$	
				-	
	(C)	$\frac{5}{2}$	(D)	$\frac{4}{3}$	
113	3 of a numl	ber is 10. What is the num		3	
, 1 G.			aber?		
	(A)	91	(B)	81	
		23	(D)	27	
14.	$\frac{5}{8}$ of 24 is eq	qual to $\frac{15}{7}$ of what numbe	r?		
	(A)	15	(B)	105	
	(C)	35	(D)	7 .	
15.	A German	elass has 12 boys and 18 p	girls. What is the fracti	ion of the class boys?	
	(A)				
	(A)	$\frac{1}{6}$	(B)	$\frac{3}{5}$	
	(C)	$\frac{2}{3}$	(D)	4/15	
		J		15	

# Explanatory Answers

Q1. (D) If x is even, then  $\frac{8}{x}$  will not be in lowest term. This is because, both x and 8 are divisible by 2.

Now we take the odd number between 30 and 40, these are; 31, 33, 35, 37, 39. In these numbers, we see that 35 and 39 are divisible by 5 and 13, respectively. Thus only 31, 33 and 37 are required numbers.

Q2. (A) Simplifying  $\frac{6}{6} \times \frac{6}{12} \times \frac{6}{18} \times \frac{6}{24} \times \frac{6}{30}$ 

$$\frac{1}{1} \times \frac{1}{2} \times \frac{1}{3} \times \frac{1}{4} \times \frac{1}{5} = \frac{1}{20}$$

Q3. (B) As  $\frac{4}{13}$  of a number is 39. Therefore the  $\frac{8}{13}$  of that number will be 78

Because  $\frac{8}{13} = \frac{4}{13} \times 2$ , and  $\frac{4}{13}$  of a number is 39, therefore double of  $\frac{4}{13} \left( \frac{4}{13} \times 2 = \frac{8}{13} \right)$  should be equal to  $39 \times 2 = 78$ 

Q4. (A) Let x be the required number, then by given condition

$$28 \div \frac{4}{3} = x \div \frac{30}{7}$$

$$28 \times \frac{3}{4} = x \times \frac{7}{30}$$

21 · = 
$$x \times \frac{7}{30}$$

$$\frac{21 \times 30}{7} = x$$

$$\Rightarrow x = 90$$

Q6. (C) Left handed = 5

So, fraction = 
$$\frac{5}{20} = \frac{1}{4}$$

Q7. (B) 8mL acid in solution = 100mL

1mL acid in solution 
$$=\frac{100}{8}$$
 = 12.5 mL

15mL acid in solution = 
$$12.5 \times 15$$

$$= 187.5 \, \text{mL}$$

Q8. (B) There are 7 days in a week, and each day has 24 hours. Therefore, Hours in a week =  $24 \times 7 = 168$ 

The required fraction is:  $\frac{98}{168} = \frac{7}{12}$ 

**Q9.** (A) People does not give vote  $=\frac{7}{100} \times 5860$ 

$$= 7 \times 58.6$$

People does not give vote  $\cong 410$  people

Candidate must gain vote = 
$$5450 \times \frac{50}{100}$$
  
= 2725 vote

Q10. (B) The midway fraction of the fractions 
$$\frac{1}{3}$$
 and  $\frac{1}{4} = \frac{1}{2} \left( \frac{1}{3} + \frac{1}{4} \right) = \frac{1}{2} \left( \frac{7}{12} \right) = \frac{7}{24}$ 

Q11. (A) Let the required number be "x", then according to given condition 
$$\frac{4}{9} \times x = 12 \Rightarrow x = \frac{12}{\frac{4}{9}}$$

$$= 12 \times \frac{9}{4} = 27$$

Q12. (A) Let the number of fish purchased =

During first week (died fish) = 
$$\frac{1}{5} \times x = \frac{x}{5}$$

Still alive =  $x - \frac{1}{5}x = \frac{4}{5}x$ 

During second week (died fish) = 
$$\frac{4}{5}x \times \frac{3}{8} = \frac{3}{10}x$$

Fish at the end of two weeks = 
$$\frac{4x}{5} - \frac{3x}{10} = \frac{8x - 3x}{10} = \frac{5x}{10} = \frac{1}{2}x$$

So fraction 
$$=\frac{\frac{1}{2}x}{x} = \frac{1}{2}$$

Q13. (D) Let the number 
$$= x$$

Then 
$$\frac{3}{8} \times x = 10$$

$$\Rightarrow x = \frac{80}{3}$$

$$\Rightarrow x = 26.67 = \boxed{27}$$
**Q14.** (D) Let the number = x

Then 
$$\frac{15}{7} \times x = \frac{5}{8} \times 24$$

$$\Rightarrow \frac{15 \times x}{7} = 15$$

$$\Rightarrow x = \frac{7 \times 15}{15} = \boxed{7}$$

**Q15. (D)** No. of boys = 
$$12$$

No. of girls = 
$$18$$
  
Total =  $12 + 18 = 30$ 

Required fraction 
$$=\frac{12}{30} = \boxed{\frac{4}{15}}$$

# Chapter 6

# **PERCENTAGE**

# Percentage:

The term 'percent' is a short form of the Latin word 'per centum' meaning 'out of hundred'. It can best be defined as:

"A fraction whose denominator is 100 is called a percentage and the numerator of the fraction is called the rate percent."

A rate percent is reduced to an equivalent fraction dividing it by 100.

# Change of percentage into Fraction or Decimal:

To convert a percentage to a fraction, mixed number or decimal, divide it by 100, and reduce, if possible. If necessary, the relating fraction may then be changed to a decimal.

# Example:

- (i) Express  $2\frac{1}{7}\%$  to a fraction
- (ii) Change  $\frac{3}{4}\%$  to a decimal.

# Solution:

(i) 
$$2\frac{1}{7}\% = \frac{15}{7}\%$$
  
=  $\frac{15}{7} \times \frac{1}{100} \left( \text{Replace \% by } \frac{1}{100} \right)$   
=  $\frac{3}{140}$   
=  $\frac{3}{140}$ 

(ii) 
$$\frac{3}{4}\% = \frac{3}{4} \times \frac{1}{100} \left( \text{Replace \% by } \frac{1}{100} \right)$$
  
=  $\frac{3}{400} = .0075$ 

# Change of Fraction into Percentage:

To change a fraction or a mixed numbers to a percent.

- a. Multiply the fraction or mixed number by 100%.
- b. Reduce, if possible
- c. Affix a % sign.

# Example 2:

- (i) Change  $\frac{1}{80}$  to a percent.
- (ii) Change 0.05 to a percent

# Solution:

(i) 
$$\frac{1}{80} = \frac{1}{80} \times 100\%$$
  
= 1.25%

(ii) 
$$0.05 = 0.05 \times 100\%$$

$$= \frac{5}{100} \times 100\%$$
$$= 5\%$$

# Expressing One Quantity as a Percentage of Another:

To express one quantity "p" as a percentage of another quantity "q".

- Write p as a fraction of q.
- Multiply the fraction  $\frac{p}{q}$  by 100% to convert it to a percentage. b.

# Example 3:

There are 56 boys in a class of 140 students. What is the percentage of the boys?

# Solution:

Total students 
$$= q = 140$$
Boys  $= p = 56$ 
Fraction  $= \frac{p}{q}$ 
 $= \frac{56}{140}$ 

Percentage 
$$= \frac{56}{140} \times 100\%$$
$$= 40\%$$

# Important Tip:

If a salary of a man is first increased by x% and then it has decreased x%, the change in its initial salary is less by x% of x or  $\frac{x^2}{100}$ 

# Note:

If two values are respectively a\% and b\% more than a third value, then the first is  $\frac{100 + a}{100 + b} \times 100$ 's of the second.

# Example 4:

Two numbers are respectively 20% and 50% more than a third, what percentage is the first to the second? Solution:

Following the above, we have the value

$$= \frac{100 + 20}{100 + 50} \times 100\%$$
$$= \frac{120}{150} \times 100\%$$
$$= 80\%$$

# Important Tip:

If the first value is r\% more than the second value, then the second is  $\left[\frac{r}{100+r} \times 100\right]$ \% less than the first value.

# Example 5:

If Hamza's salary is 35% more than that of Osama, then how much percent is Osama's salary less than that of Hamza?

# Solution:

Following the above theorem, we have the value

$$= \left[\frac{35}{100+35} \times 100\right]\%$$
$$= \left[\frac{35}{135} \times 100\right]$$

# Important Tip:

If the first value is r\% less than the second value, then the second is  $\left[\frac{r}{100-r} \times 100\right]$ \% more than the first value.

# Example 6:

If Maryam's salary is 25% less than that of Fatima, then how much percent is Fatima's salary more than that of Maria?

# Solution:

Following the above theorem, we have

$$\left[\frac{25}{100 - 25} \times 100\right] \%$$
$$= 33\frac{1}{3}\%$$

# Important Tip:

a% of a quantity is taken by the first, b% of the remaining is taken by the second and c% of the remaining is taken by the third person. Now if X is left then there was

$$\frac{X \times 100 \times 100 \times 100}{(100 - x)(100 - y)(100 - z)}$$

# in the beginning.

## Example 7:

After deduction 20% from a certain sum, and then 30% from the remainder, there is 3500 left. Find the original sum.

## Solution:

Following the above theorem, we have

$$= \frac{3500 \times 100 \times 100}{(100 - 20)(100 - 30)}$$
$$= \frac{3500 \times 100 \times 100}{80 \times 70}$$
$$= 6250$$

# Model Examples

# Example 8:

In an examination paper of 5 questions, 5 percent of the eandidates answered all of them and 5 percent none of the rest, 25 percent answered only one question, and 20 percent answered only 4. If  $24\frac{1}{2}$  percent of the entire candidates answered only 2 questions and 200 candidates answered only 3, how many candidates appeared at the examination?

Solution: Let the total no. of candidates be x

$$\frac{5x}{100}$$
 answered all the questions and  $\frac{5x}{100}$  answered none.

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The remaining candidates 
$$= x - \left(\frac{5x}{100} + \frac{5x}{100}\right)$$

$$= \frac{9x}{10}$$
No. of candidates answering only one question 
$$= \frac{25}{100} \times \frac{9x}{10} = \frac{9x}{40}$$
No. of candidates answering four questions 
$$= \frac{20}{100} \times \frac{9x}{10} = \frac{9x}{50}$$

No. of candidates answering two questions = 
$$\frac{49}{200} \times x$$

No. of candidates who answered three questions

$$= x - \left(\frac{5x}{100} + \frac{5x}{100} + \frac{9x}{40} + \frac{9x}{50} + \frac{49x}{200}\right) = 200$$

$$\Rightarrow x - \left(\frac{10x + 10x + 45x + 36x + 49x}{200}\right) = 200$$

$$\Rightarrow \frac{(200 - 50)x}{200} = 200$$

$$\Rightarrow 50x = 40000$$

$$x = 800 \text{ Ans.}$$

# Example 9:

The following table gives the number of the candidates (boys and girls) who appeared an examination. To complete the missing figure, find the number of candidates and their passing percentage.

Candidates	Appeared	Passed	Passing percentage (correct to one decimal place)
Boys	6720	3528	
Girls	4750		62.4
Total	11470		

Solution: Passing percentage of boys 
$$= \frac{3528}{6720} \times 100$$

$$= 52.5\% \text{ Ans.}$$
No. of girls passed 
$$= \frac{62.4}{100} \times 4750$$

$$= 2964 \text{ Ans.}$$
Total no. of candidates passed 
$$= 3528 + 2964$$

$$= 6492 \text{ Ans.}$$
Total pass percentage 
$$= \frac{6492}{11470} \times 100$$

$$= 56.6\% \text{ Ans.}$$

# Example 10:

In 1990, the population of a town is given below:

Men	7640
Women	6675
Boys	5628

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Girls	4872
Total	24815

In 1992, men increased by 5 percent, women by 8 percent and total population by 20 percent, and for every 7 boys there are 6 girls. Find the number of boy in 1992.

Solution: Increase in the no. of men in 1992. 
$$=\frac{5}{100} \times 7640 = 382$$

Total no. of men in 1992 
$$= 7640 + 382 = 8022$$

Increase in the no. of women in 1992 = 
$$\frac{8}{100} \times 6675 = 534$$

Total no. of women in 1992 
$$= 6675 + 534 = 7209$$

Increase in the total population in 1992 
$$=\frac{20}{100} \times 24815 = 4963$$

Total population in 1992 
$$= 24815 + 4963 = 29778$$

Total no. of boys and girls in 1992 
$$= 29778 - (8022 + 7209)$$
  
= 29778 - 15231

No. of boys = 
$$\frac{7}{13} \times 14547$$

# = 7833 Ans.

# Example 11:

Complete the following table which gives the enrolment in professional courses of one country in (1990-91) and (1995-96) and calculate the percentage increase in the first three totals of 1995-96 over those of 1990-91.

# Solution:

Categories	1990-91				
	Boy	Girls	Total 67,187		
Higher Secondary stage	57,676	9,511			
Undergraduate stage	169,259	15,715	184,974		
Postgraduate & Research	12,052	898	12,950		
Total of all stages	238,987	26,124	265,111		

Categories	1995-96				
	Boy	Girls	Total		
Higher Secondary stage	93,760	14,585	108,34		
Undergraduate stage	256,040	33,415	289,455		
Postgraduate & Research	20,200	2,000	22,200		
Total of all stages	370,000	50,000	420,000		

Solution: Increase in no. of boys

$$=370,000-238987=131013$$

\% increase = 
$$\frac{131013}{238987} \times 100$$

$$= 54.8 \%$$
 Ans.

Increase in no. of Girls

$$= 50,000 - 26124 = 23876$$

% increase 
$$=\frac{23876}{26124} \times 100$$



Total increase = 
$$91.39 \%$$
 Ans.  
=  $420,000 - 265,111$   
=  $154889$   
% increase =  $\frac{154,889}{265,111} \times 100$   
=  $58.42 \%$  Ans.

# Example 12:

The civilian industrial products of a country are given below in million dollars. Complete the columns of 'increase over the preceding year' and 'percentage increase'.

## Solution:

		Increase over the preceding year		Percentag	e increase
1951	27,003		,		
1952	29,314	2,311		."	8.60
1953	32,439	3,125			10.68
1954	36,335	3,896		•	12.00
1955	40,033	3,698			10.18

# Example 13:

In an examination, 75% of candidates passed in English and 65% in mathematics while 15% failed both in English as well as mathematics. If 495 candidates passed in both the subjects, find the total number of candidates who took the examination.

Solution: Let the total number of students be 100

25 failed in English

35 failed in Mathematics

15 failed in both

No. of failed students = 25 + 35 - 15 = 45

No. of passed in both subjects = 100 - 45 = 55

If no. of passed students is 55, then total no. of students = 100

If no. of passed students is 495, total no. of students =  $\frac{100}{55} \times 495$ 

$$= 900 \text{ Ans.}$$

# Example 14:

A candidate who gets 30 percent marks in an examination fails by 30 marks, but another candidate who gets 42 percent marks gets 42 marks more than that necessary for passing. Find the maximum number of marks and the percentage necessary for passing.

**Solution:**Let the passing marks = x

Now the candidate gets 30% marks and by this he gets 30 marks less than passing marks.

It means, he gets (x-30) marks

If he gets 30 marks, it means, maximum marks = 100

If he gets 
$$(x-30)$$
 marks, maximum marks  $=\frac{100}{30}(x-30)$  ...(i)

In the second case the candidate gets 42% marks such that he gets 42 marks above the passing marks.

It means, he gets (x + 42) marks.

If he gets 42 marks, then maximum marks  $= 100^{\circ}$ 

If he gets 
$$(x + 42)$$
 marks, maximum marks  $= \frac{100}{42}(x + 42)...(ii)$ 

As (i) and (ii) are equal because maximum marks are the same in both cases.

$$\frac{100}{30}(x-30) = \frac{100}{42}(x+42)$$

or

$$\frac{x-30}{5} = \frac{x+42}{7}$$

or

$$7x - 210 = 5x + 210$$

$$\Rightarrow$$

x = 210Putting the value of x in (i) we get

Maximum marks =  $\frac{100}{30}$  (210 – 30)

=600 Ans.

If maximum marks are 600 then passing marks = 210

If maximum marks are 100 then passing marks =  $\frac{210}{600} \times 100 = 35\%$ 

Passing percentage = 35 % Ans.

# Multiple Choice Questions (MCQs,

- QI. If the base of a rectangle is increased by 40% and its altitude is decreased by 20%, then its area
  - (A) decreased by 20%

(B) increased by 12%

decreased by 12% (C)

(**D**) increased by 16%

- Q2. If x% of y is 20, then y =
  - (A) 2000x

(B)

(D)

- 12 is  $\frac{1}{3}$ % of what number? Q3.
  - (A) 4

400 **(B)** 

(C) 36

- 3600 (D)
- Q4. If p is a positive number, 400% of p is what percent of 400 p?
  - 4 (A)

25

(C) 40 **(B)** 1

**(D)** 

- Q5. What is 10% of 30% of 40%?
  - (A) 0.12%

**(B)** 0.012%

(C) 12%

1.2% **(D)** 

- O6. What percent of 75 is x?
  - (A)

**(B)** 

(C)

- (D)
- Q7. If 35 students took an exam and 13 of them failed, what percent of them passed?
  - (A) 20% approx

**(B)** 63% approx

(C) 25% approx

- **(D)** 22% approx
- There are twice as many boys as girls in an economies class. If 20% of the boys and 35% of the girls have already handed over their result cards, what percent of the students have not yet handed over their cards?

	Starde I	Dogar's Unique Full	lly Solved "NEW TEST!	NG SYS	STEM" GUIDE 5.
	(A)	75		(B)	65
100	(C)			(D)	15
	A dealer		nental jar for Rs. 7,000 e of jar increase?		ter some days sold it for Rs. 21,000. By
	(A)			<b>(B)</b>	200
	(C)	150		(D)	20
Q10	On a test percent o exam to b	t consisting of 60 of the other 20 quote 90%?	) problems, Sonia solve uestions does she need	ed 75%	of first 40 problems correctly. What correctly for her grade on the entire
	(A)			<b>(B)</b>	65%
	( <b>C</b> )			(D)	cannot achieve 90%
Q11.	If 60% of		hen B is what percent of		
allegit accept	(A)			(B)	30%
Jan Jan	(C)	200%		(D)	3%
Q12.		cent of $p$ is $q$ ?		, <b>V</b> , ,	
	(4)	g			<u>g</u>
er eller	(A)	$\overline{p}$		(B)	p p
	(0)	100 <i>q</i>			100p
	<b>(C)</b>	$\overline{p}$		(D)	$\frac{v \circ p}{a}$
Q13.	What pere	eent of $\frac{1}{2}$ is $\frac{5}{4}$ ?		(B)	1.5
£ 34	(C)	250	•	(D)	150
Q14.			55% are boys. The nun	nber of p	girls and the number of boys are:
	(A)	369 boys, 451 g	girls	(B)	281 boys, 539 girls
	(C)	539 boys, 281 g	girls	(D)	451 boys, 369 girls
Q15.	sides of the	w a square. He the c first square. By		a second rea of th	I square whose sides were 3 times the he square increased?
	(A)	300%		<b>(B)</b>	800%
Q16.	(C)	400%		(D)	200%
Q10.	A team nas	s won 60 percent of	of the 20 games for all t	this seas	son. If the team plays a total 50 games
	the entire s	and wills of perce	ent of the remaining ga	mes, ho	ow many games will the team win for
	(A)	36		(B)	25
	(C)	42		(D)	39
Q17.			sed in price from 25Pa t	(D) to 30Pa	. What percentage increase was this?
	(A)	15%		(B)	what percentage increase was this?
	(C)	5%		(D)	20%
Q18.			oer month, which is 15%	( <i>D)</i> 'af big i	income. What is his income?
	(A)	3500		оог ніз і: (В)	5250
	(C)	2333.30		(D)	2523.30
219.			400% of x is what perce	(⊅) ∾taf40	2323,30 Mag
	(A)	1		at 01400 (B)	0.1
	(C)	0.01		(D)	100
20,	Babar gave	e 15% of his base	eball cards to Laeed an	ران اط 20% -	to Sarfraz. If he still had 520 cards,
	how many	did he have origin	nally?	U 2070	to Sarriaz. If he sun had 520 cards,

If the length of the rectangle is increased by 16% and the width is decreased by 25%, then the

If the base of a rectangle is increased by 40% and the altitude is decreased by 30%, the area is

**(B)** 

(D)

**(B)** 

**(D)** 

decreases by 41%

increases by 59%

increased by 12%

decreased by 2%

Q29.

O30.

area:

(A)

(C)

(A)

(C)

increases by 9%

decreases by 13%

increased by 10%

decreased by 10%

# Explanatory Answers

Q1. (B) If the value firstly increased by x% and then decreased by y% then there is  $\left[x - y - \frac{xy}{100}\right]$ % increase or decrease according as the sign +ve or -ve, respectively. In this problem, x = 40 and y = 20. Therefore

$$\left[40 - 20 - \frac{(40)(20)}{100}\right] \%$$

$$\left[20 - \frac{800}{100}\right]$$
%

$$[20 - 8]\% = 12\%$$

Because sign is +ve therefore its area is increased by 12%.

Q2. (C) 
$$y \times \frac{x}{100} = 20$$
  
 $\Rightarrow xy = 20 \times 100 \Rightarrow xy = 2000$   
 $\Rightarrow y = \frac{2000}{x}$ 

Q3. (D) Using,  $\frac{Part}{Whole} = Y$  percent, here P = 12, W = ? and Y percent  $= \frac{1}{300}$ 

$$\frac{P}{W} = \frac{Y}{100} \qquad \Rightarrow \qquad \frac{P}{W} = Y \times \frac{1}{100}$$

$$\frac{12}{W} = \frac{1}{3} \times \frac{1}{100} \qquad \Rightarrow \qquad W = 3 \times 1200 = 3600$$

**Q4.** (D) 400% of  $p = \frac{400}{100} \times p = 4p$ , which is 1% of 400 p.

Q5. (D) 30% of 40% = 
$$\frac{30}{100} \times \frac{40}{100} = \frac{12}{100} = 0.12$$

Now 10% of 30% of 40% =  $\frac{10}{100} \times 0.12 = 0.012 = 1.2$ 

Q6. (B) 
$$\frac{P}{W} = \frac{y}{100}$$
  $\Rightarrow$   $x = \frac{y}{100} \times 75$   $\Rightarrow$   $x = \frac{3y}{4}$   $\Rightarrow$   $y = \frac{4x}{3}$ 

Q7. (B) If 13 students failed, then the number of passed students = 35 - 13 = 22

Thus, 
$$\frac{22}{35} \times 100 = 63\%$$
 approx

Q8. (A) Let the number of girls = 100, then

Number of boys = 200

Then 35 girls (35% of 100) and 40 boys (20% of 200), have handed in their cards. Hence 75 of the 300 (100 + 200) students have handed them in. It means that 300 - 75 = 225 have not handed them in. Thus

$$\frac{225}{300} \times 100 = 75\%$$

Q9. (B) The increment in the value of the jar = Rs. 21000 - Rs. 7000 = Rs. 14000

The %age increase in the value of the jar

$$= \frac{Increment}{Actual} \times 100$$
$$= \frac{14000}{7000} \times 100 = 200\%$$

Q10.(D) To achieve 90% grade on the entire examination, Sonia needs 54 (as calculated below) problems:

$$\frac{P}{W} = y \% \implies \frac{P}{60} = \frac{90}{100} \implies P = \frac{90}{100} \times 60$$

$$\implies P = 54$$

to solve correctly. So far she has solved  $30 \left( \frac{P}{40} = \frac{75}{100} \Rightarrow P = \frac{75}{100} \times 40 = 30 \right)$  problems

correctly. Therefore, on the last 20 problems she needed 54 - 30 = 24 correct answers, which is impossible to get from 20 problems.

Q11.(C) 60% of A is 30% of B, i.e., 
$$\frac{60}{100}A = \frac{30}{100}B$$
.

$$\Rightarrow$$
 .60A = .30B,  $\Rightarrow$  B =  $\frac{.60}{.30}$ A  $\Rightarrow$  B = 2A

Now we find B is what percent of A, i, e,

$$B = \frac{x}{100} A \text{ or } B = (x\%)(A)$$

$$\Rightarrow$$
 B = (200%)A

Q12.(A) Using the relation  $\frac{\text{Part}}{\text{Whole}} = y\%$ 

$$\frac{q}{p} = y\%$$

Second Method: What % p x % p = q

$$x$$
 %  $p$  =  $q$ 

$$\Rightarrow x\% = \frac{q}{p}$$

Q13.(C) Using 
$$\frac{Part}{Whole} = y\%$$
.

$$\frac{5}{4} \div \frac{1}{2} = y\%$$

$$\frac{5}{4} \times 2 = y\% \Rightarrow y\% = \frac{5}{2} = 2.5$$
$$\Rightarrow y\% = 250\%$$

No. of boys = 
$$820 \times \frac{55}{100} = 451$$
 boys

No. of girls = 
$$820 - 451 = 369$$
 girls

Let the length of first square = 1 inch

Then Area of first square = 1 square inch

Then sides of the second square = 3 inch



Area of the second square = 9 square inch

:. Increase in the area of the 2nd square = 8 square inches

%age increase in the second square = 800%

Q16. (A) Total No. of games that

the team has won so far  $=\frac{60}{100} \times 20 = 12$  games

The total number of games left = 50 - 20 = 3080% of 30 games will the team win

$$\frac{80}{100} \times 30 = 24 \text{ games}$$

The total number of wins = 12 + 24 = 36

Q17. (D) Increase in local call = 30 - 25 = 5Pa

% increase = 
$$\frac{5}{25} \times 100 = 20\%$$

Q18. (C) Let "x" be his income then

$$15\% \text{ of } x = 350$$

$$x = 350 \div 15\% = 350 \times \frac{100}{15}$$

$$x = 2333.33$$

Q19. (A) 400% of x = 4x. Which is 1% of 400x.

Q20. (A) Actually, Babar had 100% of the cards. After distributing 35% (20% + 15%) of them, he had 100% - 35% = 65% of them left. So

$$520 = \frac{65}{100}x \Rightarrow x = \frac{520 \times 100}{65} = 800$$

Q21. (B) Infant mortality = 
$$20000 \times \frac{6.8}{100} = 1360$$

survived bodies = 
$$20000 - 1360 = 18640$$

Q22. (C) 
$$50\% \text{ of } 80 = 80 \times \frac{50}{100} = 40$$

$$20\% \text{ of } 40 = 40 \times \frac{20}{100} = \boxed{8}$$

Q23. (A) Let the can of acid used to cost Rs. 1

After increasing 20% cost it became =  $1 + \frac{1}{20} = 1.20$ 

Then 300 cans of acid used to cost = Rs. 300

Each can be bought for Rs 300

**Q24.** (C) The pears that are not spoiled = 180 - 9 = 171

Percentage = 
$$\frac{171}{180} \times 100$$
  
=  $19 \times 5$   
=  $95\%$ 

Q25. (D) After 21 days the rats have eaten wheat = 21q kilograms.

So, the required fraction in percentage =  $\frac{21q}{p} \times 100$ 

$$= 2100 \left(\frac{q}{p}\right)$$

Q26. (A)

20% of 100 = 20 cmployee

employees left = 100 - 20 = 80 employees

If it again increases by 20, the percentage of increase

$$= \frac{20}{80} \times 100 = 25\%$$

Q27. (B) Let x be the number of students, then

$$16\frac{2}{3}\% = \frac{1}{6} \Rightarrow \frac{1}{6}x = 6$$

$$\Rightarrow x = 36$$

36 students in class, 6 failed, 30 passed

Q28. (C) 30% of the 42% of the population who are women are voters so

(.30)(.42) = 0.126 = 12.60% of the population are women voters.

Q29. (C) Let L be the original length and W be the original width.

The new length= 100% + 16% = 116% of L  $\Rightarrow$  1.16L

Since the width decreases by 25% so the new width is 75% of  $W \Rightarrow .75W$ 

Arca = LW  

$$\Rightarrow$$
 New Area = (1.16)(.75)LW  
= 0.87 LW = 87% of Area

Since the area is 87% of the original area. Thus the area has decreased by (100 - 87) = 13%

Q30. (D) Let "b" be the base and "a" altitude. Then the new base will be (b + 0.4b). The new altitude after decreasing 30% is (a - 0.3a).

So the area is

$$((a - .3a)(b + 0.4b) = (0.7)(1.4)ab$$
  
= 0.98ab

The new area is 42% of the old. So the new area (98% - 100%)

=-2% is decreased by 2%

\*\*\*\*\*



# Chapter 7

# RATIO AND PROPORTION

# RATIO:

The number of times one quantity contains another quantity of the same kind is called the ratio of the two quantities.

Note: The ratio of two quantities is equivalent to the fraction that one quantity is to the other.

Example: There can be ratio between Rs. 30 and Rs. 40, but there can be no ratio between Rs. 30 and 40 apples.

Remember: The ratio 3:5 is written as 3:5 or  $\frac{3}{5}$ , 3 and 5 are called the terms of the ratio. 3 is the first and 5 is the second term.

Note: The first term of a ratio is called the antecedent and the second the consequent,

If a set of objects is divided into two groups in the ratio  $a \cdot b$ , then the first group contains  $\frac{a}{a+b}$  of the total objects. The second group contain  $\frac{b}{a+b}$  of the total number of objects.

# Important Example:

If a bag containing twelve mirrors is dropped, which of the following cannot be the ratio of the broken mirrors to unbroken mirrors?

(i) 2: 1 ii) 3:1 iii) 3:2 iv) 1:1 v) 7:5

# Solution:

Since there are 12 mirrors is the bag. So 12 must be divisible by the sum of terms in the ratio exactly. We see that 2+1=3 divides 12 exactly 3+1=4 also divides exactly. Only the ratio 3+2=5 doesn't divide 12 exactly. Thus the correct answer is (iii)

# PROPORTION:

The equality of ratios is called proportios.

## Example:

Consider the two ratios

 Ist ratio
 2nd ratio

 5:15
 7:21

Since 5 is one-third of 15, and 7 is one-third of 21, the two ratios are equal.

Note: The first and fourth terms are ealled extremes, and the second and third terms, are called the means. In above example 5 and 21 are extremes, while 15 and 7 are means.

# Important Points:

- 1. If four quantities be in proportion, the product of the extremes is equal to the product of the means.
- 2. Three quantities of the same kind are said to be in continued proportion when the ratio of the first to the second is equal to the ratio of the second to the third.

# Aid to Memory:

The mean proportional between two numbers is equal to the square root of their product.

# Example: Find

- i). Fourth proportions to 5, 10, 5
- ii) Third proportion of 5 and 10.
- iii) Mean proportions between .04 and 0.09.

## Solution:

(i) Let 5:10::5:x

0:

01

E

21

ΤI

Then 
$$5x = 10 \times 5 \Rightarrow 5x = 50 \Rightarrow x = 10$$

(ii) Let 5:.10::10:x

Then 
$$5x = 10 \times 10 \Rightarrow 5x = 100 \Rightarrow \boxed{x = 20}$$

(iii) Mean proportion between .04 and .09

$$=\sqrt{.04\times.09} = \sqrt{.0036}$$
$$=\sqrt{\frac{36}{1000}} = \frac{6}{100} = 0.06$$

# Direct Proportion:

If the given two quantities are so related to each other that if one of them is multiplied (or divided) by any number, the other is also multiplied (or divided) by the same number.

# Inverse Proportion:

If two quantities are so related that if one of them is multiplied by any number, the other is divided by the same number.

# Example:

1. If 5 balls cost Rs. 7, what do 15 balls cost?

Solution: This example is an illustration of direct proportion. Therefore, setting a proportion.

$$\therefore 5:7::15:x$$

$$\Rightarrow 5x = 15 \times 7 \Rightarrow x = \frac{15 \times 7}{5} = 21$$

2. If 5 men can build a house in 28 days, in how many days will 10 men build it? Solution:

This example is an illustration of inverse proportion. Here, if we increase number of men.

2, 3, 4 ..... times, the number of days will be decreased.

2, 3, 4...... times, Thus the inverse ratio of the number of men is equal to the ratio of the corresponding number of days.

$$\frac{1}{15} \cdot \frac{1}{10} :: 28 : x \text{ days}$$

$$\Rightarrow x = \frac{1}{5} = \frac{1}{10} \times 28$$

$$\Rightarrow x = \frac{28 \times 15}{10} = 42 \text{ days}.$$

# DOUBLE RULE OF THREE:

Example: If 8 men can reap 80 hectares in 24 days, how many hectares can 36 men reap in 30 days.

Solution: We resolve this problem in two parts.

Ist Part: If 8 men can reap 80 hectors, how many hectares can 36 men reap.

Setting a proportion

8 men : 36 men : : 80 hectares : x hecter

$$x = \frac{36 \times 80}{8} = 360 \text{ hectres}$$

2nd Part: If 360 heetares can be reaped in 24 days, how many hectares can be reaped in 30 days?

24 days: 30 days = 360 hectares: 
$$x$$
 hector

$$x = \frac{360 \times 30}{24} = 450$$

SINGLE STEP:

8 men : 36 men 24 days : 30 days

: : 80 hectare : x hector

Required No. of hectares : = 
$$\frac{\text{Multiplication of means}}{\text{Multiplication of 1st terms}}$$
  
=  $\frac{80 \times 36 \times 30}{8 \times 24} = 450$ 

# Model Examples:

**Example 1:** Three liquids contain petrol and spirit mixed in the ratio 2:3, 3:4 and 4:5, respectively. A motor owner mixes 20 litres of the first, 21 litres of the second and a few litres of third. If the ratio of petrol to spirit in the mixture is 29:39, find the number of litres of the third liquid taken for the mixture.

Solution: 20 litres of the first liquid has  $2/5 \times 20$ 

- = 8 litres of petrol and 12 litres of spirit
  - 21 litres of the second liquid have  $3/7 \times 21$
- = 9 litres of petrol and 12 litres of spirit.

Suppose x litres of the third liquid are taken, it will have  $\frac{4x}{9}$  litres of petrol and  $\frac{5x}{9}$  litres of

spirit.

or

Then

e

ng

Total petrol in the mixture 
$$= 8 + 9 + \frac{4x}{9}$$
 litres

and total spirit 
$$= 12 + 12 + \frac{5x}{9}$$
 litres.

Ratio of these = 
$$\frac{17 + \frac{4x}{9}}{24 + \frac{5x}{9}} = \frac{29}{39}$$

$$663 + \frac{156}{9}x = 696 + \frac{145}{9}x$$

$$\left(\frac{156}{9} - \frac{145}{9}\right)x = 696 - 663$$

$$\frac{11}{9}x = 33$$

$$x = \frac{9}{11} \times 33 = 27 \text{ litres.}$$

Example 2: In a regiment the number of officers to men was 3:31 before the battle. In the battle, 6 officers and 22 men were killed and the ratio become 1:13. Find the number of officers and men in the regiments. Solution: In the beginning i.e., before the battle

Let no. of officers = x

$$//$$
 // men =  $y$ 

then 
$$x: y: 3: 31 \Rightarrow \frac{x}{y} = \frac{3}{31}$$
 .....(i)

After the battle

No. of officers 
$$\approx x - 6$$
  
# # men  $= y - 22$ 

$$\frac{x-6}{y-22} = \frac{1}{13} \qquad \dots (ii)$$

From (i) we get 
$$x = \frac{3}{31}y$$

Substituting this value in (ii), we get

$$\frac{\frac{3}{31}y - 6}{y - 22} = \frac{1}{13} \qquad \dots (iii)$$

Solving for y in (iii), we get

$$y = 217$$

$$x = \frac{3}{31} \times 217 = 21$$

No. of officers = 21No. of men = 217 Ans.

Example 3: Of two kinds of alloy, silver and copper are contained in one in the ratio of 5: 1 and in the other in the ratio of 7; 2. What weights of the two alloys should be melted and mixed together so as to make up a 5 lb mass with 80% of silver?

Solution: Let the alloys taken be in the ratio of 6:9x

So in  $1^{st}$  alloy wt. of silver = 5

$$//$$
  $//$  copper = 1

in 
$$2^{nd}$$
 alloy wt. of silver =  $7x$ 

$$//$$
  $//$  copper  $=2x$ 

... wt. of silver = 
$$5 + 7x$$
  
and Total wt. =  $9x + 6$ 

and I otal wt. = 
$$9x + 6$$

$$(5+7x)\frac{100}{80} = 9x + 6$$

$$25 + 35x = 36x + 24$$

$$x = 1$$

So alloys are taken in 6:9 ratio.

Total wt. of 2nd alloys = 5 lb

But

" " 1st alloy = 
$$\frac{6}{15} \times 5 = 2 \text{ lb}$$

# # 1<sup>st</sup> alloy = 
$$\frac{6}{15} \times 5 = 2 \text{ lb}$$

# # 2<sup>nd</sup> # =  $\frac{9}{15} \times 5 = 3 \text{ lb}$ 

Ans.

Example 4: An alloy contains copper and zinc in the ratio of 5:3 and another alloy contains copper and tin in the ratio 8:5. If equal weights of both the alloys are melted together find the weight of tin in the resulting alloy per kg.

Solution: Let weight of both alloys be taken to be 13 kg.

In 
$$2^{nd}$$
 alloy in 13 kg. wt. of tin = 5 kg

$$26 \text{ kg.}$$
 wt. of tin =  $5 \text{ kg.}$ 

wt. of tin per kg. of resulting alloy = 
$$\frac{5}{26}$$
 kg.

- Q1. In a city 90% of the population own a car, 15% own a motorcycle, and everybody owns one or the other or both. What is the percentage of motorcycle owners to who own cars?
  - (A) 15%

5%

15%

- (D)
- Q2. Concrete consists of cement, sand and screenings in the ratio of 1:5:4, what is the percentage of the sand mixed?
  - 10% (A)

40% **(B)** 

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	· (C)	50%	(D	i)	60%	
Q3.			res have profit of Rs. 2400	) 10 i	in the ratio 5 : 4 : 3 Wha	t is the amount
	of the leas	t share?	1.00			t is the amount
	(A)	6000	(B	3	8000	
	(C)	10,000	. (1)	ì	1200	
Q4.	A machin of 44 hour	e produces 1280 p rs?	arts in 16 hours. How man	ny	parts would it make in a	working week
	(A)	2530	(B	`	3520	
	(C)	2122	(D		3960	. •
Q5.			what is the value of $2x$ to	•		
		3		•		
	(A)	11	(B)	`	22	
	` ,	6 22 3	(B)	,	$\frac{22}{6}$	
	(C)	22	(7)		11 5	
	(C)	3	$(\mathbf{D})$	)	5	
Q6.	If 80% ap number re	plication to a proge	gram were rejected, what	is 1		ecepted to the
	(A)	1:4	<b>(B</b> )		4:1	
	(C)	1:8	(D)		3:8	
Q7,			ımference of a circle to its	) ra:	dius?	
			to the to the	ıa	ulus:	
	(A)	π	(B)	)	$\frac{\pi}{2}$	
~~	(C)	$2\pi r$	(D)	)	2π	
Q8.	Win/Loss	ratio for two team	s are A, $5:2$ and B, $7:3$ w	yhi	eh team has the better re	cord?
	(A)	Α	(B)		В	
	(C)	both A and B	(D)	ı	wrong question	
<b>Q</b> 9.	take, work	ing at the same ra	rtain number of houses in te, to do the same job?	24	days, how many days w	ill 40 workers
	(A)	12 days	(B)		18 days	
	(C)	15 days	(D)		9 days	
Q10.	If a jet trav	vels 1280 km in 2 l	nours, how far will it trave	l ir		speed?
	(Å)	2100	(B)		3300	
	(C)	2700	(D)		3520	
Q11.		of a: b is 9:7 the	on $a + h$ is:		3320	
	(A)	14	(B)		16	
	(C)	63	(D)		not possible	
Q12.			n nickels (five cent coin), h	ΛU	meny apples can you be	n for d dimes
	and <i>q</i> quar	ters?	inches (iive cent com), ii	On		ly for <i>a</i> diffies
	(A) "	$\frac{\mathbf{A}(d+q)}{n}$ $\frac{\mathbf{A}}{n}(2d+5q)$	(B)		T)	•
	(C)	$\frac{A}{n}$ (2d + 5q)	(D)		$\frac{d+q}{An}$	
Q13.	If the ratio	of hove and girls	s in a class is 3:5 and th		alass soutsing 24 student	ta kass
	additional	hove would have to	o enroll to make the ratio o	ic i	ciass contains 24 student	is, now many
	(A)	9		) I I	_	
	· (C)	6	(B)		15	
Q14.		_	(D)		12	
- · · · · ·	much flour	to the negreet and	sugar and 18 gram of flow am, should be used?	ur.	11 only 100gram of sugar	r is used, how
	(A)	, to the hearest gra			12	
	(A) (C)	14	(B)		13 17	
Q15.			(D) blue and yellow paint in the	<b>.</b>	1/ matic 2 : 5 Ham	nah aslassi
	Lunyar	- vommed HVIII	blue and yellow paint in th	ue .	rand 5: 5. How much of 6	each colour is

# needed to make 40 litres of this green paint?

- Blue paint 15 litres, yellow paint: 25 (A)
- Blue paint: 25 litres, yellow paint: 15
- litres
- Blue paint: 10 litres, yellow paint: 30 (C) litres
- Blue paint: 13 litres, yellow paint: 27 litres

(D) Let x stand for the percentage who own both a car and a motorcycle. Then Q1.

(The %age who own a motorcycle) + (The %age who own a car) - (The %age who own one or the other or both) = 100% own one or other or both.

**(B)** 

$$15\% + 90\% - A = 100\%$$

∴ 
$$15\% + 90\% - A = 100\%$$
  
⇒  $105\% - A = 100\% \Rightarrow A = 5\%$ 

The %age of motorcycle owners to who own car is

$$=\frac{5\%}{15\%}=\frac{1}{3}=\boxed{33\frac{1}{3}\%}$$

Ratio = 1:5:4Q2. (C)

Sum of ratio = 
$$1 + 5 + 4 = 10$$

Sand = 
$$\frac{5}{10} \times 100 = 50\%$$

Q3.

Ratio = 
$$5:4:3$$
  
Sum of ratio =  $5+4+3=12$ 

least share 
$$=\frac{3}{12} \times 24000$$

- Let "x" be the number of parts in 44 hours Q4.

16:1280::44:x Then

$$\Rightarrow \frac{\frac{16}{1280}}{x} = \frac{\frac{44}{x}}{\frac{3520}{3520}} \Rightarrow x = \frac{\frac{44 \times 1280}{16}}{16}$$

The ratio of x to y can be written as  $\frac{x}{y}$ . The ratio of x to y is  $\frac{11}{3}$ , which can be written as Q5.

$$\frac{x}{y} = \frac{11}{3}$$

If 
$$\frac{x}{y} = \frac{11}{3}$$
, then  $2\left(\frac{x}{y}\right) = 2\left(\frac{11}{3}\right)$ 

$$\frac{2x}{y} = \boxed{\frac{22}{3}}$$

Since 80% of the application were rejected. Therefore, 20% = (100% - 80%) were accepted, the Q6. ratio of accepted to rejected is

20%:80%=1:4

The ratio of the circumference to the diameter of the eircle is  $\pi$ . Therefore Q7.

$$\pi = \frac{C}{d} \Rightarrow \frac{C}{2r} \Rightarrow 2\pi = \frac{C}{r}$$

Q8.

$$\begin{array}{c|c}
A & B \\
5:2 & 7:3 \\
= \frac{5}{2}:1 & = \frac{7}{3}:1
\end{array}$$

Team A has the better record.



Clearly, the more workers are there, the less time will be required, therefore, 15: 40:  $\frac{1}{24} \cdot \frac{1}{x}$ Q9.

$$\Rightarrow \frac{15}{40} = \frac{x}{24} \Rightarrow x = \frac{15 \times 24}{40} = 9 \text{ days}$$

(D) It's a direct variation question

$$1280: 2:: x : \frac{11}{2}$$

$$1280 x \Rightarrow 2x = 0$$

$$\frac{1280}{2} = \frac{x}{11/2} \implies 2x = \frac{1280 \times 11}{2}$$

$$\implies x = 3520 \text{ km}$$

Q11. In this question if a is 18 and b is 14, then the ratio a:b is 9:7 but a+b=32. The point in this question that a and b can take on many possible values. It is not possible here to establish one definite value for the sum of a and b.

Q12. (C) 
$$\frac{A \text{ apples}}{n \text{ nickels}} = \frac{A \text{ apples}}{5n \text{ cents}} = \frac{x \text{ apples}}{(10d + 25q)\text{cents}}$$

$$\Rightarrow \frac{A}{5n} = \frac{x}{10d + 25q} \Rightarrow 5nx = A(10d + 25q)$$

$$\Rightarrow x = \frac{A5(2d + 5q)}{5n}$$

$$\Rightarrow x = \frac{A}{n}(2d + 5q)$$

(C) Given ratio 3: 5 of boys and girls. Total number of students in the class is 24.

Number of boys = 
$$\frac{3}{8} \times 24 = 9$$
 boys  
Number of girls =  $\frac{5}{8} \times 24 = 15$  girls

In order of have same number of boys and girls, 6 additional boys would have to enroll.

Q14. (B) This is a direct proportion, because the more sugar, the more flour

$$\frac{13}{18} = \frac{10}{x}$$

$$13x = 180$$

$$\Rightarrow x = 13\frac{11}{12}$$

Q15. (A)

The ratio 3:5 gives (3+5) = 8 parts

Blue paints 
$$=\frac{3}{8} \times 40 = 15$$
 litres

Yellow paints 
$$=\frac{5}{8} \times 40 = 25$$
 litres

\*\*\*\*\*\*\*\*

E١

ru: So

Ex est: Gu

mir

(i) (ii) *Sol*.

# Chapter 8

# AVERAGE

In Mathematics, average is a representative of a number of given quantities. Average is of several kinds.

# METHOD OF FINDING AVERAGE

To find average of any number of quantities of the same kind is to add all the items together and then divide the sum by the number of items.

$$\therefore \text{ Average} = \frac{\text{Sum of all the items}}{\text{No. of items}}$$

# Model Examples.

**Example 1:** The average daily temperature from 9<sup>th</sup> January to 16<sup>th</sup> January (both inclusive) was 38.6° and that from the 10<sup>th</sup> to 17<sup>th</sup> January (inclusive) was 39.2°. What was the temperature on 17<sup>th</sup> January?

Solution: Total temp. from 9th Jan. to 16th Jan.

$$= 38.6 \times 8^{\circ} \text{C}$$

$$= 308.8^{\circ}C$$
Since the temp. on  $9^{th}$ 

$$= 34.6^{\circ}C$$

.. Total temp. from 10th Jan. to 16 Jan.

$$= 308.8 - 34.6$$
  
= 274.2°C

Total temp. from 10 to 17th Jan.

$$=39.2\times8^{\circ}\mathrm{C}$$

$$=313.6$$
°C

Temp on 
$$17^{th}$$
 Jan. =  $313.6 - 274.2$   
=  $39.4^{\circ}$ C

Example 2: A goods train in five successive minutes from its start runs 68 metres, 127 metres, 208 metres, 312 metres and 535 metres and for next five minutes in maintains average speed of 33 km/hr. Find the whole distance covered and the average speed of train in km/hour.

Solution: Distance covered in first five minutes.

$$= \frac{68+127+208+312+535}{1000}$$
 kms.  
$$= \frac{5}{4}$$
 kms.

Now average speed for next five minutes

$$= 33 \text{ km/hr}.$$

Distance covered in next five minutes 
$$=\frac{33 \times 5}{60} = \frac{11}{4}$$
 km

Total distance covered in 10 minutes 
$$=\frac{5}{4} + \frac{11}{4} = \frac{16}{4}$$

$$= 4 \text{ kms. Ans.}$$

Average speed = 
$$\frac{4}{10}$$
 km/min.

$$= \frac{4}{10} \times 60$$
$$= 24 \text{ km/hr. Ans.}$$

**Example 3:** The average salary per head of all the workers of an institution is Rs. 60. The average salary per head of 12 officers is Rs. 400. The average salary per head of the rest is Rs. 56. Find the total no. of workers in

**Solution:** Let the total No. of workers = x

Total salary drawn = 
$$60x$$
 .......(i)  
Salary of 12 officers =  $12 \times 400 = 4800$  Rs.

#### the rest = 
$$(x-12) \times 56$$

Hence total salary of the workers

$$=(x-12)56+4800$$
 .....(ii)

$$60x = 4800 + 56x - 672$$
  $\Rightarrow$   $4x = 4128$   $\Rightarrow$   $x = 1032 \text{ Ans.}$ 

Example 4: On a journey across Karachi the overage speed of a taxi 20 m.p.h. for 70% of the distance, 25 m.p.h. for 10% of it and 8 m.p.h. for the remainder. Find the average speed for the whole journey.

Solution: Let the distance be 100 miles.

Time taken for 70% journey at 20 m.p.h. 
$$=\frac{70}{20} = 3.5$$
 hrs.

Time taken for 10% journey at 25 m.p.h. 
$$=\frac{10}{25} = 2/5$$
 hrs.

Total taken for 20% journey at 8 m.p.h. 
$$=\frac{20}{8} = 2.5$$
 hrs.

Total time taken = 
$$3.5 + \frac{2}{5} + 2.5 = 6\frac{2}{5}$$
 hrs.

$$\therefore \text{ Average speed} = \frac{100}{\frac{32}{5}} = \frac{125}{8}$$

$$= 15.625 \text{ m.p.h. Ans.}$$

Example 5: A batsman has a certain average of runs for 16 innings. In the 17th innings, he makes a score of 85 runs there by increasing his average by 3. What is the average of the 17th inning.

**Solution:** To increase the average by 3 runs he has to make  $17 \times 3 = 51$  runs more than the average of previous innings.

$$\therefore \text{ Average of 16 innings} = 85 - 51 = 34$$

$$//$$
  $//$   $17$   $//$  = 34 + 3 = 37 Ans.

**Example 6:** A motorist set out at 10 a.m. to travel from Lahore to Gujrat, suppose a distance of 80 miles. He estimated that he could maintain an average speed of 25 m.p.h. For the first 44 miles from Lahore to Gujranwala his speed, averaged 30 m.p.h. but afterwards he was delayed by traffic and reached Gujrat 24 minutes later than the estimated time. Calculate:

- (i) His time of arrival in Gujrat
- (ii) His average speed from Gujranwala to Gujrat

**Solution:** Total distance from Lahore to Gujrat = 80 miles.

Average speed estimate from Lahore to Gujrat = 25 m.p.h.

Estimated time taken from Lahore to Gujrat =  $\frac{80}{25} = \frac{16}{5}$  hours

But he was late by  $\frac{24}{60}$  hours.

$$\therefore \text{ Total actual time taken } = \frac{16}{5} + \frac{24}{60}$$
$$= \frac{18}{5} \text{ hours}$$

= 3 hours 36 minutes.

He starts at 10:00 A.M. and will reach there at Gujrat at 1:36 P.M.

Now distance from Lahore to Gujranwala = 44 miles

Average speed from Lahore to Gujranwala = 30 m.p.h.

Time taken from Lahore to Gujranwala  $=\frac{44}{30}$  hours

$$=\frac{22}{15}$$
 hours

Now distance from Gujranwala to Gujrat = 80 - 44

= 36 miles.

Time taken from Gujranwala to Gujrat  $=\frac{18}{5} - \frac{22}{15}$ 

$$=\frac{32}{15}$$
 hours

Average speed from Gujranwala to Gujrat =  $\frac{36}{32}$  miles/hr.

=16.9 miles per hour (app.) Ans.

# Multiple Choice Questions (MCQs)

- Q1. The average of even integers from 2 to 100 inclusive is:
  - (A) 49

**(B)** 52

**(C)** 51

- (D) 50
- Q2. What is the average of first hundred natural numbers?
  - (A) 50

**(B)** 50.5

(C) 49.5

- **(D)** 100
- Q3. What is the average of x, y and z? If x + y = 5, y + z = 8 and x + z = 11.
  - (A)  $\frac{11}{2}$

(B)  $\frac{1}{2}$ 

(C)  $\frac{13}{5}$ 

- (D)
- Q4. The average of five numbers is 54. If three of the numbers are 26, 28 and 30, what is the average of the other two?
  - (A) 91

**(B)** 93

Q5.		54	(D)	186	
Q5.		da e e u da e e e e		100	
		the following is the a	average of $x^2 - 16, 39 - x^2$ a	1 + 10	
	(A)	x + 3	(B)		•
	(C)	u ± 11	• •	$\frac{x+11}{3}$	
	(C)	x+11	(D)	3	
Q6.	8 students class test.	in a elass obtained What is the average	60%, 3 obtained 75%, 2 o marks?	btained 80% and	7 obtained 45% in
	(A)	49%	(B)	59%	
	(C)	29%	(D)	51%	
Q7.	first 3 mai	ge number of goals a tehes and they seor e last two matches?	a team has scored in 7 mate ed 5 goals in each of the n	hes is 8. They ave	raged 10 goals for th What is the averag
	(A)	5 goals	(B)	4 goals	
	(C)	6 goals	- (B) (D)	8 goals	•
Q8,	If the mean	n (average) of 6 nun	ibers is 4.5. What is the sun		
	(A)	0.75	(B)	10.5	
	(C)	12	(D)	27 .	
Q9.			• •		
	hours, she	is paid S rupees p	r hour for the first 8 hours er hour. If she works 12 h	ours in one day,	what is her average
	(A)	8R + S	(B)	$\frac{8R + 4S}{4}$	
	(C)	$\frac{12R - 8S}{4}$	<b>(D)</b>	$\frac{2R+S}{3}$	
Q10.	dropped to	58. Find his recent	his first four math tests test grade.	After taking the r	next test, his average
	(A)	, 40	<b>(B)</b>	50	
Q11.	(C)	48	(D)	32	
QII.			= 11, what is the average o		
	-(A)	14	(B)	<u>28</u>	
			( <del>-</del> ,/	3	<i>i</i> •••
	(C)	14	(D)	$\frac{7}{3}$	
		6		3	
Q12.	If the avera		s 6, what is the value of S?		
	(A)	4	(B)	6	
012	(C)	12	¹ ( <b>D</b> )	0	v.
Q13.		e average of 3 <sup>10</sup> , 3 <sup>20</sup> a		. 0 10 70	
	(A)	3 <sup>57</sup>	(B)	$3^9 + 3^{19} + 3^{29}$	
Q14.	(C)	•	(D)	$3^{11} + 3^{21} + 3^{31}$	
ŽI4.	11 20x + 20y	v = 70, what is the av	erage of x and y?		
	(A)	$\frac{7}{2}$	(B)	7	
	(C)	<u>/</u> 4	(D)	$\frac{4}{7}$	
			4 4	10 . 10	
Q15.		e following is the av	/erage of $x' - 20, 40 - x'$ , an	1d $3x + 4$ ?	
Q15.	Which of the	the following is the av $x^4 - 24$ $x^4 + 3x + 24$	/erage of $x' = 20, 40 - x'$ , and (B)	$\frac{3x + 4?}{x + 8}$	

Q1. (C) As sum of the first n even numbers = n(n + 1)Now, the sum of even numbers from 2 to 100 is  $2 + 4 + 6 + 8 + \dots + 100$  (or 50 even number)

$$=50(50+1)=2550$$

Average = 
$$\frac{\text{Sum of numbers}}{\text{Number of terms}}$$
  
=  $\frac{2550}{50}$  = 51

Q2. (B) The first 100 natural numbers are {1,2,3,....,100}

sum of all the first *n* numbers=  $\frac{n(n+1)}{2}$ Now,

Sum of first 100 natural numbers 
$$=\frac{100(100+1)}{2}$$

$$=5050$$

Now, average = 
$$\frac{\text{Sum of numbers}}{\text{Number of terms}}$$
  
\(\cdot = \frac{5050}{100} = 50.5)

**Shortcut:** The average of first "n" natural number is  $\frac{n+1}{2}$ 

Thus, average 
$$=\frac{100+1}{2} = \frac{101}{2} = 50.5$$

Q3. (D) Adding the given three equations:

$$(x + y) + (y + z) + (z + x) = 5 + 8 + 11$$

$$2x + 2y + 2z = 24$$

$$2(x+y+z) = 24$$

Dividing both sides by 2

$$x + y + z = 12$$

Now average of x, y and z is

$$\frac{x+y+z}{3} = \frac{12}{3} = 4$$

Q4. (B) Let the missing numbers be a and b, then by given condition,

$$\frac{a+b+26+28+30}{5} = 5$$

$$a + b + 84 = 270$$
 (Multiplying both sides by 5)

$$a + b = 186$$

Hence average of a and b is

$$\frac{a+b}{2} = \frac{186}{2} = 93$$

Q5. (C)

Average = 
$$\frac{\text{Sum of the terms}}{\text{No. of terms}}$$
$$= \frac{x^2 - 16 + 39 - x^2 + 3x + 10}{3}$$

$$= x + 11$$

- Q6. (B) 8 students with 60%, total =480 marks
  - 3 students with 75%, total = 225 marks
  - 2 students with 80%, total = 160 marks
  - 7 students with 45%, total = 315 marks
  - 20 students obtain a total = 1180 marks

:. Average 
$$=\frac{1180}{20} = 59\%$$

Q7. (D) Total goals for 7 matches =  $7 \times 8 = 56$ 

Total goals for 3 matches with average score of 10 = 30

Total goals for 2 matches with average score of 5 = 10

Total goals for remaining 2 matches = 56 - 30 - 10

Average goals in last two matches  $=\frac{16}{2}$ 

(D) Average of 6 numbers =  $\frac{\text{Sum of numbers}}{\text{Sum of numbers}}$ Q8.

> $\Rightarrow$  Sum of the numbers = (Average of 6 numbers)  $\times$  6  $= 4.5 \times 6 = 27$

Q9. (D)

For first 8 hours, she is paid = 8R

Next 4 hours, she is paid = (12 - 8) = 4S

Total pay 
$$= 8R + 4S$$

Average = 
$$\frac{8R + 4S}{12} = \frac{2R + S}{3}$$

Q10. (B) Let "x" be the required grade, then

$$\frac{4(60) + x}{5} = 58$$

$$\Rightarrow$$
  $^{\circ}240 + x = 290 \Rightarrow x = 290 - 240 = 50$ 

Q11. (A)

$$\frac{(a+b)+(b+c)+(c+a)}{3} = \frac{8+9+11}{3}$$

$$\Rightarrow \frac{2(a+b+c)}{3} = \frac{28}{3}$$

$$\Rightarrow \qquad a+b+c = 14 \qquad \dots \dots (i)$$

$$a+b+c = 14 \qquad .....(i)$$
Put  $a+b = 8 \Rightarrow 8+c = 14 \Rightarrow c = 6$ 

Now put 
$$b+c = 9 \Rightarrow a+9 = 14 \Rightarrow a=5$$

again put c + a = 
$$11 \Rightarrow 11 + b = 14 \Rightarrow b = 3$$

Average of a, b and c = 
$$\frac{6+5+3}{3} = \frac{\boxed{14}}{3}$$

Q12. (B) 
$$\frac{3+5+10+S}{4} = 6 \Rightarrow 18+S = 24 \Rightarrow S = 6$$

Q13. (B) 
$$\frac{3^{10} + 3^{20} + 3^{30}}{3} = (3^{10} + 3^{20} + 3^{30})3^{-1}$$
$$= 3^{10-1} + 3^{20-1} + 3^{30-1}$$
$$= 3^9 + 3^{19} + 3^{29}$$

Q14. (C) 
$$20x + 20y = 70 \Rightarrow 20(x + y) = 70 \Rightarrow x + y = \frac{7}{2}$$

$$\Rightarrow$$
 Average of x and y =  $\frac{x+y}{2} = \frac{7}{2 \times 2} = \boxed{\frac{7}{4}}$ 

Q15. (B) 
$$\frac{(x^4 - 20) + (40 - x^4) + (3x + 4)}{3} = \frac{3x + 24}{3} = \frac{3(x + 8)}{3}$$

$$=x+3$$



### Chapter 1

#### **POLYNOMIALS**

### Polynomial:

A sum of finite number of monomials is called a polynomial. Each monomial is called a term of the polynomial.

#### Monomial:

A monomial is a variable, or a constant, or a product of constant and one or more variables, with the variables having only non-negative integer in exponents.

#### Example:

$$3x^2y$$
,  $-5xy$ , and  $-7xy^3$  are monomials.

The algebraic expression

$$4y^{-3}$$
 and  $\frac{3}{y}$ 

are not monomials, because these expressions have not non-negative integer in exponent, and cannot be written as a product of a constant and a variable with a non-negative integer exponent.

### Degree of Monomial:

In any monomial the sum of the exponents of the variables is called the degree of monomial.

#### Example:

What are the degrees of the monomials

$$-3x^2y$$
,  $7x^3y$ ,  $-18xy^2$ 

#### Solution:

In algebraic expression  $-3x^2y$ , the degree of the monomial is 3, because the exponents of x and y are 2 and 1 respectively therefore their sum is (2 + 1 = 3). Similarly the degree of the expressions  $7x^3y$  and  $-18xy^2$  are 4 and 3 respectively.

#### Note:

In monomial, the constant is called the numerical coefficient or simply the coefficient of the monomial.  $-3x^2y$ ,  $7x^3y$  and  $-18xy^2$  are monomials of coefficient -3, 7, and -18 respectively.

### Multiplication of Monomials:

The process of multiplication is illustrated in the following example:

#### Example:

What is the value of  $-5xy^2$ , when x = -2 and y = -3

#### Solution

First of all write the coefficient of the monomial, then substitute the value of x and y in monomial. Then evaluate:

$$-5(-2)(-3)^2 = -5(-2)(9) = 90$$

#### Polynomial:

A sum of a finite number of monomials is called a polynomial. Each monomial in a polynomial is called a term of the polynomial.

#### Degree of a Polynomial:

The degree of a polynomial is the largest degree of the terms in the polynomial.



## What are like terms in a Polynomial?

Terms of polynomial that have exactly the same variables raised to the same powers are called like terms.

### Example:

Each of the following is a polynomial:

$$3x^2 + 5$$
,  $3x^2$ ,  $2x^2 + 9x - 12$ ,  $-4x^2$ ,  $7x^2y$ ,  $9x^2 - 8$ 

#### Explanation.

In above lists of polynomials;  $3x^2 + 5$ , and  $9x^2 - 8$  are called binomial because each polynomial has two terms; the polynomials  $3x^2$ ,  $-4x^2$  and  $7x^2y$  are monomials; the polynomial  $2x^2 + 9x - 12$  is called trinomial because it has three terms. In above list of polynomials  $3x^2$  and  $-4x^2$  are like terms, similarly  $3x^2 + 5$  and  $9x^2 - 8$  are like terms, because they have exactly the same variables raised to the same power.

### General Form of a Polynomial:

In a single variable x, the general form of a polynomial of degree n is

$$a_n x^n + a_{n-1} x^{n-1} + \dots + a_2 x^2 + a_1 x + a_0$$
 where *n* is a non negative integer, and  $a_n \neq 0$ 

### Combination of Like Terms in a Polynomial:

The polynomial  $4x^2 + 3x + 6x + x^2 + x$  is equivalent to the binomial  $5x^2 + 10x$ , because like terms are combined in a polynomial. The process of combination is illustrated as:

$$4x^2 + x^2 = 5x^2$$
 and  $3x + 6x + x = 10x$   
 $4x^2 + 3x + 6x + x^2 + x = 5x^2 + 10x$ 

#### Remember:

Only like terms in a polynomial can be combined.

### **Arithmetic Operations on Polynomials:**

We use usual law of arithmetic, to add subtract, multiply and divide polynomials.

### Addition and Subtraction:

Polynomials are added or subtracted by combining like terms.

#### Example:

$$(2x^3 + 3x^2 + 7x + 6) + (4x^2 + 3x - 2) - (5x^2 + 4x)$$

$$= 2x^3 + (3x^2 + 4x^2 - 5x^2) + (7x + 3x - 4x) + (6 - 2)$$

$$= 2x^3 + 2x^2 + 6x + 4$$

The rules for adding like terms are:

#### Rule 1:

If all the terms are positive in a polynomial, then add their coefficients.

#### Example:

Find the value of  $8x^2 + 2x^2 + 7x^2$ 

#### Solution:

Here we have to increase 8 like things by 2 and 7 like things of the same kind, and aggregate is 17 of each thing.

#### Rule 2:

If all the terms in a polynomial are negative add the coefficient numerically and prefix the minus sign to the sum.

#### Example:

What is the sum of -4x, -x, -3x and -7x

#### Solution:

In this example the word sum indicates the aggregate of 4 subtractive quantities of like terms. In this case we have to take away successively 4, 1, 3 and 7 like things, therefore the result is the same as taking away 15(4 +

1 + 3 + 7) such things in the aggregate.

The sum of -4x, -x, -3x, -7x is -15x.

#### Rule 3:

If all the terms have not same sign, add together separately the coefficient of all the negative terms and the coefficient of all the positive terms: Then find the difference of those two results, preceded by the sign of the greater, will give the coefficient of the sum required.

### Example:

Find the sum of  $12x^2 - 3x^2 + 15x^2 - 17x^2$ 

#### Solution:

The sum of the coefficient of positive terms is 12 + 15 = 27

The sum of the coefficient of negative terms is 3 + 17 = 20

The difference of these is 7, and the sign of the greater is positive; hence the required sum is  $7x^2$ .

### Multiplication of Monomials:

To multiply two simple monomials together, first multiply their coefficients together and prefix their product to the product of the different letters, giving to each letter on index equal to the sum of the indices that letter has in the separate factors.

#### Example:

What is the product of  $5x^2y^3$  and  $-3xy^2$ 

#### Solution:

$$(5x^2y^3)(-3xy^2) = (5)(-3)(x^2 \times x)(y^3 \times y^2)$$
$$= -15x^3y^5$$

#### Note:

The product of a monomial by any polynomial is the algebraic sum of the partial products of each term of the polynomial by that monomial.

#### Example:

Find the product of 
$$2xy^2$$
 and  $(4x^2 + 3y + 7xy)$ 

#### Solution:

$$2xy^2(4x + 3y + 7xy) = 8x^3y^2 + 6xy^3 + 14x^2y^3$$

## Multiplication of two Binomials:

The procedure of multiplication of two binomials is illustrated as:

- 1. Multiply each term of the first binomial by each term of the second.
- 2. When the terms multiplied together have like signs, prefix to the product the sign +, when unlike prefix -.
- 3. The algebraical sum of the partial products so formed gives the complete product.

### Example:

Multiply 
$$(x + 3)$$
 by  $(x - 5)$ 

Solution: 
$$(x+3)(x-5) = x(x-5) + 3(x-5)$$
  
=  $x^2 - 5x + 3x - 15$   
=  $x^2 - 2x - 15$ 

Find the value of 
$$(x + 2)(x - 3) - (x + 4)(x - 5)$$

٠,



#### Solution:

First of all, multiply both pairs of binomials separately, then subtract the second result from the first.

$$(x+2)(x-3) = x(x-3) + 2(x-3) = x^2 - 3x + 2x - 6$$

$$= x^2 - x - 6$$

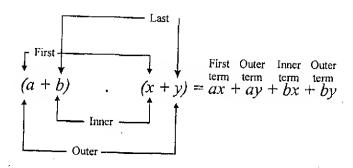
$$(x+4)(x-5) = x(x-5) + 4(x-5) = x^2 - 5x + 4x - 20$$

$$= x^2 - x - 20$$

Subtracting: 
$$(x^2 - x - 6) - (x^2 - x - 20) = x^2 - x - 6 - x^2 + x + 20$$
  
= 14

#### FOIL Method:

The product of the two binomials can be computed by the FOIL method. This method is illustrated in the following example



#### Example: .

Find the product of (2x-3) and (4x+2) using FOIL Method

First Outer Inner Last
$$(2x-3)(4x+2) = (2x)(4x) + (2x)(2) + (-3)(4x) + (-3)(2)$$

$$= 8x^2 + 4x - 12x - 6$$

$$= 8x^2 - 8x - 6$$

## Important Binomial Formulas:

Following are most important binomial products, those occur frequently in algebra.

1. 
$$(x+y)(x-y) = x^2 - y^2$$

2. 
$$(x+y)^2 = x^2 + 2xy + y$$

2. 
$$(x+y)^2 = x^2 + 2xy + y^2$$
  
3.  $(x-y)^2 = x^2 - 2xy + y^2$ 

#### Example:

Find each of the following products:

a) 
$$(2a+3)(2a-3)$$

b) 
$$(a - 5b)^2$$

#### Solution:

a) Using formula 
$$(x + y)(x - y) = x^2 - y^2$$
  
Here  $(2a + 3)(2a - 3) = (2a)^2 - (3)^2 = 4a^2 - 9$ 

b) Using formula 
$$(x - y)^2 = x^2 - 2xy + y^2$$
  
 $(a - 5b)^2 = (a)^2 - 2(a)(5b) + (5b)^2 = a^2 - 10ab + 25b^2$ 

Given 
$$x + y = 5$$
, and  $x^2 - y^2 = 10$ , what is the value of  $x - y$ ?

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#### Solution:

Using the fact 
$$(x + y)(x - y) = x^2 - y^2$$
  
 $(5)(x - y) = 10$   
 $x - y = \frac{10}{5}$ 

$$\Rightarrow x-y = 2$$

### Example:

Find the value of xy, when  $(x + y)^2 = 25$  and  $x^2 + y^2 = 3$ 

#### Solution:

We know
$$(x + y)^2 = x^2 + 2xy + y^2$$

We can write 
$$(x + y)^2 = (x^2 + y^2) + 2xy$$

Substituting the value of  $(x + y)^2$ , and  $x^2 + y^2$  in above

$$25 = (3) + 2xy$$

$$22 = 2xy$$

$$xy = \frac{22}{2}$$

$$xy = 11$$

### Division of Polynomial by Monomial:

Division is the inverse of multiplication. The object of division is to find out the quantity called quotient.

Thus 
$$\frac{\text{divided}}{\text{divisor}} = \text{quotient}$$

To divide a monomial by a monomial, use distributive law, the index of each letter in the quotient is obtained by subtracting the index of that letter in the divisor from that in the divided. To the result so obtained prefix its proper sign the quotient of the divided by that of divisor.

To divide a polynomial by a monomial, divide each term separately by that monomial, and take the algebraic sum of the partial quotient so obtained.

### Example 1:

What is the quotient when  $-4x^2y$  is divided by 2x.

#### Solution:

The quotient 
$$=\frac{-4x^2y}{2x} = -2xy$$

#### Example 2:

Divide 
$$12x^3 - 6x^2 - 9x$$
 by  $3x$ 

#### Solution:

$$\frac{12x^3}{3x} - \frac{6x^2}{3x} - \frac{9x}{3x} = 4x^2 - 2x - 3$$

### Evaluating a Polynomial:

To evaluate a polynomial, substitute the given value(s) for the variable(s) and then perform the given operation.

If 
$$x = 3$$
,  $y = -7$  and  $z = -2$ , find the value of  $x^2 - 26y + 17z$ 



Solution:

$$x^2 - 26y + 17z = (3)^2 - (26)(-7) + 17(-2)$$
  
= 9 + 182 - 34 = 157

### **Factorising Polynomials:**

Writing a polynomial as a product of polynomials of lower degree is called factoring.

When each of the terms which eompose a polynomial is divisible by a common factor, the polynomial may be simplified by dividing each term separately by this factor, and enclosing the quotient within brackets; the common factor being placed outside as a coefficient.

#### Example 1:

Resolve into factors  $4x^2 - 20x$ 

#### Solution:

The terms of the polynomials  $4x^2 - 20x$  have a common factor 4x;

$$\therefore 4x^2 - 20x = 4x(x-5)$$

#### Example 2:

Resolve into factors  $x^2 - sx + tx - st$ 

#### Solution:

We see that the first two terms contain a common factor x, and the last two terms a common factor t, we enclose the first two terms in one bracket, and the last in another. Thus,

$$x^{2} - sx + tx - st = (x^{2} - sx) + (tx - st)$$
  
=  $x(x - s) + t(x - s)$ , take  $(x - s)$  eommon  
=  $(x - s)(x + t)$ 

## Factorising Quadratic Trinomials:

Some trinomials of the form  $x^2 + bx + c$  can be factorized by trial and error procedure. This method is the reverse of the FOIL method. This is illustrated in the following example.

#### Example:

Consider the following binomial expansion:

$$(x+5)(x+6) = x(x+6) + 5(x+6)$$
  
=  $x^2 + 6x + 5x + 30$   
=  $(x+5)(x+6)$ 

Notice at 
$$11 = 5 + 6$$
 and  $30 = 5 \times 6$ 

This result can be used to factorize trinomials? For example, to factorize the trinomial  $x^2 + 7x + 12$  we need to find two numbers so that:

Product = 
$$12$$
 and sum =  $7$ 

The two numbers are 4 and 3

$$4 \times 3 = 12 \text{ and } 4 + 3 = 7$$
  

$$\therefore x^2 + 7x + 12 = (x + 4)(x + 3)$$

### Example:

Factorize i) 
$$x^2 + 7x - 18$$
  
ii)  $m^2 - 9m + 14$ 

#### Solution:

i) 
$$x^2 + 7x - 18$$
  
Product =  $9 \times (-2) = -18$   
Sum =  $9 + (-2) = 7$ 

$$\therefore x^2 + 7x - 18 = (x+9)(x-2)$$

$$ii$$
)  $m^2 - 9m + 14$ 

Product = 
$$(-7)(-2) = 14$$

Sum = 
$$(-7) + (-2) = -9$$

$$m^2 - 9m + 14 = (x - 7)(x - 2)$$

#### Example:

Find the value of (10001)<sup>2</sup>

#### Solution:

$$(10001)^{2} = (10000 + 1)^{2}$$

$$= (10000)^{2} + 2(10000)(1) + (1)^{2}$$

$$= 100000000 + 20000 + 1$$

$$= 100020001$$

#### Example:

What is the value of (9999)<sup>2</sup>

#### Solution:

$$(9999)^{2} = (10000 - 1)^{2}$$

$$= (10000)^{2} - 2(10000)(1) + (1)^{2}$$

$$= 100000000 - 20000 + 1$$

$$= 99980001$$

### Algebraic Fraction:

An expression which has a variable in the denominator, is called an algebraic expression. Algebraic fractions are added and subtracted using the same method as for arithmetic fractions. The denominator must be the same before these operations can be carried out.

### Example:

Simply i) 
$$\frac{3x}{4} + \frac{x}{6}$$

ii) 
$$\frac{x+3}{8} - \frac{x-4}{4}$$

#### Solution:

i) 
$$\frac{3x}{4} + \frac{x}{6}$$
  
 $= \frac{9x + 2x}{12}$  (lowest common denominator is 12)  
 $= \frac{11x}{12}$   
ii)  $\frac{x+3}{8} - \frac{x-4}{4}$   
 $= \frac{(x+3) - 2(x-4)}{8} = \frac{(x+3) - (2x-8)}{8} = \frac{x+3-2x+8}{8}$ 

# Multiplication and Division of Algebraic Fractions:

Algebraic fractions are multiplied and divided using the same method as for arithmetic fractions.

### Example:

 $=\frac{11-2x}{8}$ 



Simply *i*) 
$$\frac{x}{15} \times \frac{9}{y}$$

$$ii) \qquad \frac{a^2}{2} \div \frac{a^3}{4}$$

Solution:

$$i) \qquad \frac{x}{15} \times \frac{9}{y} = \frac{3x}{5y}$$

$$ii) \qquad \frac{a^2}{2} \div \frac{a^3}{4}$$

$$=\frac{a^2}{2}\times\frac{4}{a^3}$$

$$=\frac{2}{a}$$

Example:

Simplify 
$$\frac{9x^3 - x}{(3x - 1)(9x - 3)}$$
, also find the value when  $x = 39$ 

Solution:

$$\frac{9x^3 - x}{(3x - 1)(9x - 3)} = \frac{x(9x^2 - 1)}{(3x - 1)3(3x + 1)} = \frac{x(3x - 1)(3x + 1)}{3(3x - 1)(3x + 1)}$$
using  $a^2 - b^2 = (a + b)(a - b)$ 

$$= \frac{x}{3}$$

Now when x = 39

$$=\frac{39}{3}=13$$

Example:

Find the value of 
$$\frac{a^2 - b^2}{(a - b)}$$
, when  $a = 2.9$  and  $b = 9.1$ 

Solution:

$$\frac{a^2 - b^2}{a - b}$$

$$= \frac{(a - b)(a + b)}{(a - b)} = a + b$$

$$= (2.9 + 9.1) = 12$$

Example:

Simply 
$$\frac{e}{4c} \cdot \frac{eb}{ac}$$

Solution:

$$\frac{e}{4c} \times \frac{ac}{eb} = \frac{a}{4b}$$

⇒



What is the value of a and b, If  $a^2 - b^2 = 36$  and a + b = 6?

#### Solution:

$$a^2 - b^2 = 36$$
  $\implies$   $(a - b)(a + b) = 36$ 

$$(a-b)(6) = 36$$
 as  $a+b=6$ 

$$a - b = 6$$
 .....(1)

adding 
$$\underline{a+b} = 6$$
 .....(2)

$$2a = 12$$

Substituting 
$$a = 6$$
 in (2) we have

$$6 + b = 6$$
,  $b = 0$ 

$$a = 6, b = 0$$

#### Example:

Find the value of xy, when  $x^2 + y^2 = 58$  and  $x^2 - y^2 = 42$ 

#### Solution:

adding

$$(x^2 + y^2) + (x^2 - y^2) = 2x^2$$

$$(58) + (42) = 2x^2 \Rightarrow 2x^2 = 50 \Rightarrow x = +5$$

Substituting

$$x = \pm 5$$
 in  $x^2 + y^2 = 29$ 

$$(5)^{2} + y^{2} = 29 \qquad \Rightarrow \qquad y^{2} = 4 \qquad \Rightarrow y = \pm 2$$
$$\Rightarrow \qquad xy = (5)(2) = 10$$

Q1. If 
$$x = 235$$
 and  $y = 117$ , then  $\frac{x^2 - y^2}{x - y} = ?$ 

(A) 118 **(B)** 100

(C) 115

- 352 **(D)**
- If  $x^2 y^2 = 16$  and  $x^2 + y^2 = 34$ , which of the following could be the value of xy? Q2.
- П -15
- Ш 45 .

(A) · only I

**(B)** only II

I and II only

- **(D)** III only
- The average of the polynomials,  $2x^2 + 5x 6$ ,  $5x^2 5x 6$  and  $30 7x^2$  is: Q3.
  - (A)

**(B)** 18

(C) 6

- **(D)** 5x
- What is the value of  $x^2 + 14x + 24$ , when x = 854? Q4.
  - (A) 1000

**(B)** 100,000

**(C)** 741,296

- (D) 742,398
- Q5. If  $x^2 + y^2 = 9$  and  $(x - y)^2 = 3$ , what is the value of xy?
  - 16 (A)

**(B)** 

(C) 6

- **(D)** 3
- The value of (5x+6)(x+12) (5x-6)(x+3) is: **Q**6.
  - $2(5x^2 + 9x)$ (A)

**(B)** 14

**(C)** 

- (D) 22
- If  $\frac{1}{x} + \frac{1}{y} = \frac{1}{z}$  and xy = z, what is the average of x and y?



$$(\mathbf{A}) \quad \frac{1}{2}$$

(C) 
$$\frac{x+y+z}{3}$$

$$\mathbf{(D)} \qquad \frac{x+y+z}{2}$$

6

Q8. If 
$$p^2 - q^2 = 48$$
 and  $p - q = 12$ , what is the average of p and q?

12 **(D)** 

$$Q9. \qquad \left(\frac{1}{x} + x\right)^2 - \left(\frac{1}{x} - x\right)^2 = ?$$

**(B)** 

(C) 
$$2\left(\frac{1}{x^2} + x^2\right)$$

$$(\mathbf{D}) \qquad 2\left(\frac{1+x^2}{x^2}\right)$$

Q10. If 
$$\left(x + \frac{1}{x}\right) = 81$$
, then  $x^2 + \frac{1}{x^2} = ?$ 

6563

**(B)** 6561

(C) 6559

79 **(D)** 

If x < 0, then  $-3x^2$  is: Q11.

> (A) less than  $(-3x)^2$

**(B)** greater than  $(-3x)^2$ 

(**C**) equal to  $(-3x)^2$ 

greater than or equal to  $(-3x)^2$ . **(D)** 

If x > y, then (x - y)(x + y) is: Q12.

> $(\mathbf{A})$ equal to (x - y)(x - y)

**(B)** less than (x - y)(x - y)

**(C)** greater than (x-y)(x-y)

**(D)** options A and C

If a = -5 and b = 3 then  $-a^2b^3$  is:

(A) less than 0

**(B)** equal to 0

greater than 0 (C)

options B and C **(D)** 

Q14. (a+b)(a-b) =

 $(\mathbf{A})$ a(a-b)-b(a-b)

**(B)** a(b-a)+b(a-b)

(C) a(a+b)-b(b+a)

a(a-b)+b(b-a)**(D)** 

 $\frac{3x^2-27}{x-3}$  and (x > 0), is: Q15.

> (A) less than 2x+9

equal to 2x + 9**(B)** 

**(C)** greater than 2x + 9

**(D)** cannot find

The sum of the polynomials,  $6x^2 + 9x - 8$  and  $2x^2 - 5x + 3$  is: O16.

> $4x^2 - 14x - 5$ (A)

 $8x^2 + 14x + 11$ 

(C)  $8x^2 - 4x + 5$ 

 $8x^2 + 4x - 5$ (Đ)

 $(6x^2 + 9x - 8) - (4x^2 - 5x + 3) = ?$ 

 $2x^2 - 14x - 11$ (A)

 $2x^2 + 14x - 11$ **(B)** 

(C)  $10x^2 + 4x - 11$   $2x^2 + 14x + 11$ 

Q18. The product of  $-3x^2y$  and  $2x^2y^2z$  is:

> (A)  $-6x^4v^3z^2$

 $-6x^4y^3z$ (B)

 $-6x^3y^3z$ (C)

 $6x^2v^2z^2$ (D)

Q19. What is the product of 2x and  $6x^2 - 3xy^2 + 4$ ?

(A) 
$$3x^2 - xy^2 + 2$$

(B) 
$$3x - \frac{3}{2}y^2 + \frac{2}{x}$$

(C) 
$$12x^3 - 6x^2y^2 + 8x$$

(D) 
$$6x^3 - 6x^2y^2 - 8x$$

What is the product of (2x + y) and  $(4x^2 - 6xy^2)$ ? Q20.

(A) 
$$8x^3 + 12x^2y^2 + 4x^2y - 6xy^3$$

(B) 
$$8x^3 - 12x^2y^2 + 4x^2y + 6xy^2$$

(C) 
$$8x^3 + 12x^2y^2 - 4x^2y + 6xy^3$$

**(D)** 
$$8x^3 - 12x^2y^2 + 4x^2y - 6xy^3$$

What is quotient if  $36x^2y + 21xy^3z$  is divided by 9xy? Q21.

(A) 
$$4x - \frac{7}{3}yz^2$$

**(B)** 
$$4y - \frac{3}{7}y^2z$$

(C) 
$$4x + \frac{3}{2}y^2z^2$$

**(D)** 
$$4x + \frac{7}{3}y^2z$$

Q22. If p = 3q - s, then what is the value of q in terms of p and s?

$$(A) \quad \frac{p+s}{3}$$

(B) 
$$\frac{p-1}{3}$$

(C) 
$$\frac{s-p}{3}$$

(D) 
$$\frac{3}{p-s}$$

If x-3=11, what is the value of x-6? Q23.

Q24.  $\frac{x^2y^2-1}{xy-1}=?$ 

$$(A) \quad xy - 1.$$

$$(B) (xy+1)$$

(C) 
$$(xy+1)^2$$

(D) 
$$(1-xy)$$

If  $y = \frac{1}{1 + 1}$ , when a = 1 and  $b = \frac{1}{3}$ , then  $y = \frac{1}{3}$ Q25.

(A) 
$$\frac{1}{3}$$

(D) 
$$\frac{1}{4}$$

Q26. If 
$$\frac{1}{1 + \frac{x}{1 + x}} = 1$$
, then  $x = \frac{1}{1 + x}$ 

**(D)** 
$$\frac{1}{1+x}$$

If  $a^2 + b^2 = 16$  and  $(a - b)^2 = 4$ , then ab is equal to:

(C) 
$$-20$$

20

If  $a^2 - b^2 = 27$  and  $a^2 + b^2 = 13$  then the value of ab is equal to:

(A) 
$$2\sqrt{5}$$

**(B)** 
$$2i\sqrt{35}$$

Q.

Q3

Q3

Q3;

Q34

Q35

Q36.

Q37.

Q38.

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	NTS Guide
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Q29. What is the value of 
$$\left[\frac{1}{x} + x\right]^2 - \left[\frac{1}{x} - x\right]^2$$
?

**(A)** 4

(B)

(C)  $2x^2$ 

**(D)**  $\frac{2}{x^2}$ 

Q30. What is the arithmetic mean of x and y if  $\frac{1}{x} = \frac{1}{z} - \frac{1}{y}$  and xy = z?

(A)

 $(B) \qquad \frac{1}{2}$ 

(C)  $\frac{x+y+z}{3}$ 

(D)  $\frac{x+y}{2}$ 

Q31. If  $x^2 - y^2 = 25$  and x - y = 5, then the average of x and y is:

(A) 2.5

**B**)

(C) 15

**D**) 7.5

Q32. What is the value of  $\frac{1}{x^2} + x^2$ , when  $\left(x - \frac{1}{x}\right)^2 = 36$ ?

(A) · (

(B) 8

(C) 38

**(D)** 34

Q33. What is the value of  $\frac{m^2 - m - 6}{m^2 - 6m + 9}$ , when m = 6666?

(A) 6666

(B) -i

(C) 0

**(D)** 1

Q34. If 7 + 4p = q - kp, what is value of p?

(A)  $\frac{4+k}{q-7}$ 

(B)  $\frac{4-1}{2}$ 

(C)  $\frac{q-7}{4+k}$ 

(D)  $\frac{k-4}{7}$ 

Q35. If  $F = C + \frac{bv^2}{K}$ , then v is terms of F, C, K and b is:

 $(A) \pm \sqrt{\frac{K}{C}(F-b)}$ 

(B)  $\pm \sqrt{\frac{C}{b}(FK - C)}$ 

(C)  $\pm \sqrt{\frac{K}{h}(F-C)}$ 

 $\pm \sqrt{\frac{KF+C}{K}}$ 

8900

Q36. If x = 7, what is the value of  $x^{5/2} \div x^{1/2}$ ?

(A)  $\sqrt{2}$ 

(B) \

(C) 49

 $(\dot{\mathbf{D}})$  4

Q37. What is the value of  $m^2 + 7m - 18$  when m = 91?

(A) 8882

(B)

**(D)** 

**(C)** 1260

**(D)** 8918

Q38. What is the value of ab, when  $a^2 + b^2 = 9$  and  $(a - b)^2 = 7$ ?

(A) 10

(B)



8 **(D)** 

What is the difference of the reciprocals of  $x^2$  and  $y^2$ ? O39.

$$(A) \qquad \frac{y^2 - x^2}{x^2 y^2}$$

(B) 
$$\frac{-y^2-x^2}{x^2y^2}$$

(C) 
$$\frac{x^2y^2}{y^2-x^2}$$

$$(D) x^2 + y^2$$

What is the value of  $a^2 - b^2$ , when a + b = 2.95 and a - b = 1000? Q40.

.00000295

**(D)** 2950

Q41. What is the value of (x-7)(x+8) - (x-9)(x+10)?

**(B)** 146

(**D**) -14x + 34

Q1. (D) 
$$\frac{x^2 - y^2}{x - y} = \frac{(x - y)(x + y)}{x - y} = x + y = 235 + 117 = 352$$

Q2. (C) Adding both equations i.e.,

$$x^{2} + y^{2} = 34$$

$$x^{2} - y^{2} = 16$$

$$2x^{2} = 50 \implies x^{2} = 25$$

$$\implies x = +25$$

Now, 
$$x^2 + y^2 = 34 \Rightarrow 25 + y^2 = 34 \Rightarrow y^2 = 9$$

$$\Rightarrow y = \pm 3$$

Hence, 
$$xy = (-5)(-3) = 15 = (5)(3)$$

and 
$$xy = (-5)(3) = -15 = (5)(-3)$$

So correct answer is C.

Q3. (C) First of all we find the sum of the three polynomials, then divide the answer by 3. Sum of the three polynomials

$$2x^{2} + 5x - 6 
5x^{2} - 5x - 6 
-7x^{2} +30$$

Now, Average= Sum of the three polynomials

$$=\frac{18}{3}=6$$

Q4. (C) To avoid time consuming calculation, factorize the given polynomial  $x^2 + 14x + 24 = x^2 + 12x + 2x + 24 = x(x + 12) + 2(x + 12)$ 

$$x^{2} + 14x + 24 = x^{2} + 12x + 2x + 24 = x(x+12) + 2(x+12)$$
  
=  $(x+2)(x+12)$ 

Substituting the value of x in above

**Q5.** (D) Solving  $(x-y)^2 = 3 \Rightarrow x^2 + y^2 - 2xy = 3$ 

Substituting the value of  $x^2 + y^2$  in above

$$(x^{2} + y^{2}) - 2xy = 3 \implies 9 - 2xy = 3$$
$$\implies 9 - 3 = 2xy \implies 6 = 2xy$$

Q6. (D) 
$$(5x+4)(x+1)-(5x-6)(x+3)=$$



$$(5x^2 + 5x + 4x + 4) - (5x^2 + 15x - 6x - 18)$$
  
 $(5x^2 + 9x + 4) - (5x^2 + 9x - 18) = 4 + 18 = 22$ 

Q7. (A) 
$$\frac{1}{z} = \frac{1}{x} + \frac{1}{y} \Rightarrow \frac{1}{z} = \frac{x+y}{xy} \Rightarrow \frac{1}{z} = \frac{x+y}{z} (\because z = xy)$$
  
$$\Rightarrow 1 = x + y \Rightarrow \frac{1}{2} = \frac{x+y}{2}$$

Hence 
$$\frac{x+y}{2} = \frac{1}{2}$$

**Q8.** (C) 
$$p^2 - q^2 = 38 \Rightarrow (p+q)(p-q) = 48$$
 ...(i)

Now, given that p - q = 12...(ii)

Dividing equation (i) by (ii), we have

$$\frac{(p+q)(p-q)}{(p-q)} = \frac{48}{12}$$

$$p+q = 4 \qquad ...(iii)$$

Dividing both sides of equation (iii) by 2, we get

$$\frac{p+q}{2} = \frac{4}{2} = 2$$

Q9. (A) Expanding each square of the polynomial, we get

$$\left(\frac{1}{x^2} + x^2 + 2\right) - \left(\frac{1}{x^2} + x^2 - 2\right)$$

$$\Rightarrow \left(\frac{1}{x^2} + x^2 + 2 - \frac{1}{x^2} - x^2 + 2\right) = 4$$

Q10.(D) Given 
$$\left(x + \frac{1}{x}\right)^2 = 81 \Rightarrow x^2 + \frac{1}{x^2} + 2 = 81$$
  
 $\Rightarrow x^2 + \frac{1}{x^2} = 81 - 2 \Rightarrow x^2 + \frac{1}{x^2} = 79$ 

Q11.(A) Since x is negative (: x < 0), therefore  $x^2$  is positive, implies that  $-(+3)(+x^2) = -3x^2$  is negative Now, we take  $(-3x)^2$ , because x is negative.

$$[-3(-x)]^2 = (-3)^2(-x)^2 = 9x^2,$$

which is positive, hence  $-3x^2$  is less than  $(-3x)^2$ .

Q12.(C) Since x > y, therefore, x - y is positive. Thus dividing (x - y)(x + y) and (x - y)(x - y) by (x - y), we have,  $\frac{(x-y)(x+y)}{x-y}$   $\frac{(x-y)(x-y)}{x-y}$ 

$$x+v$$
  $x-v$ 

Because both quantities are positive, but L.H.S is greater than R.H.S.

Q13.(A) As 
$$a = -5$$
 and  $b = 3$   $\Rightarrow -a^2b^3 = -(-5)^2(3)^3$   
 $\Rightarrow -a^2b^3 = -(25)(27)$ 

which is clearly less than 0.

Q14.(C) If we multiply (a+b) by (a-b), we proceed as a(a+b) - b(a+b) so option C is the correct answer.

Q15.(C) 
$$\frac{3x^2 - 27}{x - 3} = \frac{3(x^2 - 9)}{x - 3} = \frac{3(x - 3)(x + 3)}{(x - 3)} = 3(x + 3) = 3x + 9$$

which is clearly greater than 2x + 9.

Q16.(D) 
$$(6x^2 + 9x - 8) + (2x^2 - 5x + 3)$$
  
=  $(6x^2 + 2x^2) + (9x - 5x) + (-8 + 3)$   
=  $8x^2 + 4x - 5$ 

Q17.(B) 
$$(6x^2 + 9x - 8) - (4x^2 - 5x + 3)$$
  
=  $(6x^2 - 4x^2) + (9x - (-5x)) + (-8 - 3)$   
=  $2x^2 + (9x + 5x) + (-11)$ 

Q18.(B) 
$$2x^{2}y^{2}z$$

$$\frac{\times -3x^{2}y}{-6x^{4}y^{3}z}$$
Q19.(C) 
$$6x^{2} - 3xy^{2} + 4$$

Q20.(D) 
$$(2x + y) \times (4x^2 - 6xy^2) = 2x(4x^2 - 6xy^2) + y(4x^2 - 6xy^2)$$
  
=  $8x^3 - 12x^2y^2 + 4x^2y - 6xy^3$ 

Q21.(D) 
$$(36x^2y + 21xy^3z) + 9xy$$
  
=  $\frac{36x^2y + 21xy^3z}{9xy} = \frac{36x^2y}{9xy} + \frac{21xy^3z}{9xy}$   
=  $4x + \frac{7}{3}y^2z$ 

Q22.(A) 
$$p = 3q - s$$
  

$$\Rightarrow p + s = 3q \implies q = \frac{p + s}{3}$$

Q23.(B) Given, 
$$x - 3 = 11$$
  
Subtracting 3 both sides of the equation

$$\Rightarrow x-3-3=11-3$$

$$\Rightarrow x-6=8$$

$$\frac{x^2y^2-1}{xy-1}=\frac{(xy+1)(xy-1)}{(xy-1)}=xy+1$$

Q25.(D) 
$$y = \frac{1}{\frac{1}{a} + \frac{1}{b}}$$
, putting  $a = 1$  and  $b = \frac{1}{3}$ , we get

$$y = \frac{1}{\frac{1}{1} + \frac{1}{1/3}} \Rightarrow y = \frac{1}{1/3} \Rightarrow y = \frac{1}{4}$$

Q26. A 
$$\frac{1}{1+\frac{x}{1+x}}=1$$
, Solving for x

$$\frac{1}{\frac{1+x+x}{1+x}} = 1$$
 (Taking "1 + x" L.C.M in denominator)

$$\Rightarrow \frac{1 \times (1+x)}{\frac{1+2x}{(1+x)} \times (1+x)} = 1$$
 (Multiplying denominator, and numerator by  $(1+x)$ )

$$\Rightarrow \frac{1+x}{1+2x} = 1 \Rightarrow 1+x = 1+2x \Rightarrow 1-1 = 2x-x$$
$$\Rightarrow x = 0$$

Q27. d) 
$$a^2 + b^2 = 16$$
 and  $(a - b)^2 = 4$   
 $(a - b)^2 = 4 \implies a^2 + b^2 - 2ab = 4$   
 $\implies a^2 + b^2 - 4 = 2ab$ 

but  $a^2 + b^2 = 16$  substituting above equation

$$12 = 16 - 4 = 2ab$$

$$\Rightarrow ab = 6$$

$$b^2 = 27 \text{ and } b^2 + 12$$

Adding 
$$a^{2} + b^{2} + a^{2} - b^{2} = 27 + 13$$
,  
 $2a^{2} = 40 \implies a^{2} = 20$   
Which gives  $20 + b^{2} = 13 \implies b^{2} = -7$   
 $a^{2}b^{2} = -140 = 140i^{2}$   
 $ab = 2\sqrt{35}i \implies 2i\sqrt{35}$   
Q29. a)  $\left[\frac{1}{x} + x\right]^{2} - \left[\frac{1}{x} - x\right]^{2}$ 

Expand each square

$$\left[\frac{1}{x} + x\right]^2 = \frac{1}{x^2} + x^2 + 2$$

$$\left[\frac{1}{x} - x\right]^2 = \frac{1}{x^2} + x^2 - 2$$

$$\left[\frac{1}{x^2} + x^2 + 2\right] - \left[\frac{1}{x^2} + x^2 - 2\right] = \frac{1}{x^2} + x^2 + 2 - \frac{1}{x^2} - x^2 + 2$$

$$= 4$$

Q30. d) 
$$\frac{1}{x} = \frac{1}{z} - \frac{1}{y} \Rightarrow \frac{1}{z} = \frac{1}{x} + \frac{1}{y} \Rightarrow \frac{1}{z} = \frac{x+y}{xy}$$
$$\Rightarrow \frac{xy}{z} = x + y$$

butxy = z which gives

$$\frac{z}{z} = x + y$$

$$\Rightarrow 1 = x + y$$

$$\Rightarrow \frac{x + y}{2} = \frac{1}{2}$$

$$\Rightarrow 1 = x + y$$

$$\Rightarrow \frac{x + y}{2} = \frac{1}{2}$$
Q31. a) Given  $x^2 - y^2 = 25$  and  $x - y = 5$ 

$$x^2 - y^2 = 25 \Rightarrow (x - y)(x + y) = 25$$
but  $x - y = 5$  (given)
$$\Rightarrow 5(x + y) = 25$$

$$\Rightarrow (x + y) = 5$$

$$\Rightarrow \frac{x + y}{2} = \frac{5}{2} = 2.5$$

Q32. c) 
$$\left(x - \frac{1}{x}\right)^2 = 36$$
, Expanding the square  $x^2 + \frac{1}{x^2} - 2 = 36$ 

$$\Rightarrow x^2 + \frac{1}{x^2} = 38$$

Q33. d) 
$$\frac{m^2 - m - 6}{m^2 - 6m + 9}$$
  
=  $\frac{m^2 - 3m + 2m - 6}{(m - 3)^2} = \frac{m(m - 3) + 2(m - 3)}{(m - 3)^2}$ 

$$=\frac{(m+2)(m-3)}{(m-3)^2} = \frac{m+2}{m-3} = \frac{6666+2}{6666-3}$$

$$=\frac{6668}{6663}=1 \text{ (approx)}$$

Q34. c) 
$$7 + 4p = q - kp$$
  
 $4p + kp = q - 7$ 

$$p(4+k) = q-7$$

$$p = \frac{q-7}{4+k}$$

Q35. (C) 
$$F = C + \frac{bv^2}{K}$$

$$FK - CK = bv^2$$
  $\Rightarrow$   $v^2 = \frac{K(F - C)}{b}$ 

$$v = \pm \sqrt{\frac{K}{b}(F - C)}$$

Q36. (C) 
$$x^{5/2} \div x^{1/2}$$
 and  $x = 7$   
 $7^{5/2} \div 7^{1/2} \implies \frac{7^{5/2}}{7^{1/2}} = 7^{5/2} \times 7^{-1/2}$ 

$$= 7^{5/2 - 1/2} = 7^2 = 49$$

Q37. (B) Given 
$$m^2 + 7m - 18$$
 and  $m = 91$   
 $m^2 + 9m - 2m - 18$   
 $\Rightarrow m(m + 9) - 2(m + 9) \Rightarrow (m - 2)(m + 9)$   
 $\Rightarrow (91 - 2)(91 + 9) = (89)(100)$   
 $= 8900$ 

Q38. (C) Given 
$$(a-b)^2 = 7$$
 and  $a^2 + b^2 = 9$   
 $a^2 + b^2 - 2ab = 7 \implies 9 - 2ab = 7$   
 $\Rightarrow -2ab = -2$ 

Q39. (A) Given 
$$x^2$$
 and  $y^2$ 

reciprocals of  $x^2$  and  $y^2$  are  $\frac{1}{x^2}$  and  $\frac{1}{v^2}$  and their difference is

$$\frac{1}{x^2} - \frac{1}{y^2} \Rightarrow \frac{y^2 - x^2}{x^2 y^2}$$

Q40. (D) Given 
$$a+b = 2.95$$
  $a-b = 1000$   
 $(a+b)(a-b)=(2.95)(1000)$   
 $a^2-b^2 = 2950$ 

Q41. (A) Given 
$$(x-7)(x+8) - (x-9)(x+10)$$
  
 $(x^2+x-56) - (x^2+x-90)$   
 $x^2+x-56-x^2-x+90=34$ 



### Chapter 2

### **EQUATION**

An equation is a statement that has an equal sign. The parts of an equation to the right and left of the sign of equality are called sides of the equation and are distinguished as the right side and left side.

Highest power of the variable determines the degree of the equation. The letters used for variables in an equation are ealled unknown quantity. The process of finding the values of variables is called solving the equation. The value so found is called the root or solution of the equation.

### Linear Equation:

The equation in which the highest power of the variable is one, is called a simple or linear equation of the first degree.

#### Example:

$$3x = 9$$
,  $2x + 5 = 7$ ,  $x - 7 = 9$   $\frac{x}{2} - \frac{2}{3} = 5$  are linear equations

### Axioms of Solving Linear Equation:

The process of solving linear equation depends only upon the following axioms:

- 1. If we add equals in an equation on both sides, the sums are equal.
- 2. If from equals we take equals the remainders are equal.
- 3. If equals are multiplied to both sides of an equation the products are equal.
- 4. If equals are divided by equals then the quotients are equal.

### Rules of Solving Linear Equation:

We use following rules to solving a linear equation.

#### Rule 1:

In a linear equation, any term may be transposed from one side of the equation to the other by changing sign.

### Example 1:

Consider a equation

$$-7x + 14 = -3x - 18$$

Transposing 
$$3x + 14 = 7x - 18$$

or 
$$18 + 14 = 7x - 3x$$

which is the original equation with the sign of some terms are changed.

#### Example 2:

Solve 
$$3x - 8 = 16$$

#### Solution:

The variable x is multiplied by 3 and then 8 has been subtracted

$$x \longrightarrow 3x \longrightarrow 3x \longrightarrow 3x-8$$

Transposing the operations of "x", "-" in other words "undo" or backtrack these two operations, first add 8, and then divide by 3.

$$x \leftarrow 3x \leftarrow 3x - 8$$

To keep this equation balance, the same operation must be carried out on both sides of the equation. The process of solving above equation is illustrated simply in two steps as fellows:

$$3x - 8 = 16$$
  
 $3x - 8 + 8 = 16 + 8$   
 $3x \div 3 = 24 \div 3$ 

$$x = 8$$

## Steps for Solving Linear Equations:

- 1. If the equation involves a fraction, first, if necessary, clear the fractions.
- 2. Transpose all the terms containing the unknown quantity to one side of the equation, and the known quantity to the other side of the equation.
- 3. Collect the terms on each side.
- 4. Divide both sides of the coefficient of the unknown variable.
- 5. Compute for the result.

#### Example:

Solve

$$(i) \quad 7x - 12 = 3x$$

(i) 
$$7x - 12 = 3x$$
 (ii)  $\frac{4}{x} = \frac{-1}{3}$ 

(iii) 
$$\frac{3}{1+x} = \frac{1}{2}$$

(iii) 
$$\frac{3}{1+x} = \frac{1}{2}$$
 (iv)  $\frac{4}{3+a} + 1 = \frac{1}{3}$ 

#### Solution:

Check

(i) 
$$7x - 12 = 3x$$
$$7x - 3x = 12$$
$$4x = 12$$
$$x = 3$$

Substituting 
$$x = 3$$
 in equation  $7x - 12 = 3x$   
 $7(3) - 12 = 3(3)$ 

$$21 - 12 = 9$$
$$9 = 9$$

Solution is correct

Substituting x = -12 in

$$(ii) \quad \frac{4}{x} = \frac{-1}{3}$$

Check

Multiplying both sides by 3x

$$\frac{4}{x} \times 3x = \frac{-1}{5} \times 3x$$

$$12 = -x$$

$$(-1)(x) \div (-1) = 12 \div (-1)$$
  
 $x = -12$ 

$$\frac{x}{4} = \frac{3}{3}$$

$$\frac{-1}{3}=\frac{-1}{3}$$

Note: 3x is LCD

Solution is correct

(iii) 
$$\frac{3}{1+x} = \frac{1}{2}$$

Check

Multiplying both sides by 2(1 + x)

$$\frac{3}{1+x} \times 2(1+x) = \frac{1}{2} \times 2(1+x)$$

$$6 = 1+x$$

$$6-1 = 1+x-1$$

$$x = 5$$

Substituting x = 5 in

$$\frac{3}{1+5} = \frac{1}{2}$$

$$\frac{3}{6} = \frac{1}{2}$$

$$\frac{1}{2} = \frac{1}{2}$$

Solution is correct

#### Check

(iv) 
$$\frac{4}{3+a}+1=\frac{1}{3}$$

Check

Multiplying both sides by 3(3 + a)

$$\left(\frac{4}{3+a}\right) \times 3(3+a) + 1 \times 3(3+a) = \frac{1}{3} \times 3(3+a)$$

$$(4 \times 3) + 3(3 + a) = 3 + a$$

Removing Brackets

$$12+9+3a = 3+a$$

$$21+3a = 3+a$$

$$21+3a-21-a=3+a-21-a$$

$$2a = -18$$

$$a = -9$$

$$\mathbf{a} = -1$$

Substituting a = -9 in given equation

$$\frac{4}{3 + (-9)} + 1 = \frac{1}{3}$$

$$\frac{4}{-6} + 1 = \frac{4 - 6}{-6}$$

$$=\frac{-2}{-6}=\frac{1}{3}$$

$$\frac{1}{3} = \frac{1}{3}$$

Solution is correct

### Example:

If 
$$\frac{1}{x} = \frac{1}{y} + \frac{1}{z}$$
, what is the value of x?

#### Solution:

$$\frac{1}{x} = \frac{1}{y} + \frac{1}{z}$$

$$\frac{1}{x} = \frac{z + y}{yz}$$

Multiplying both sides by (xyz)

$$\frac{1}{x} \times xyz = \frac{(z+y)}{yz} \times xyz$$

$$\frac{yz}{y+z} = \frac{x(y+z)}{(y+z)}$$

$$x = \frac{yz}{y+z}$$

### Example:

If x = y(a + b), find a in terms of x, y and b.

### Solution:

$$x = y(a + b)$$

$$\frac{x}{y} = \frac{y(a+b)}{y}$$

$$\frac{x}{y}$$
 - b = a + b - b

$$a = \frac{x}{y} - b$$

### Solving Second-Degree Equation:

A second-degree equation involving the variable x has the generalized form

$$ax^2 + bx + c = 0$$

where a, b, and c are constants with a  $\neq 0$ . Second-degree equations are usually called quadratic equations. A quadratic equation in which the term containing x is missing is called a pure quadratic equation. Examples of second-degree equations are

$$2x^{2} - 5x + 12 = 0$$

$$4x^{2} = 16$$

$$7x^{2} - 12 = 3x + 5$$

Example:

If  $z^2 = x^2 + y^2$  and x > 0, what is y in terms of x and z.

Solution:

$$z^{2} = x^{2} + y^{2}$$

$$z^{2} - x^{2} = x^{2} + y^{2} - x^{2}$$

$$\Rightarrow y^{2} = z^{2} - x^{2}$$

Taking square root

$$\sqrt{y^2} = \sqrt{z^2 - x^2}$$

The value of  $\sqrt{\ }$  is  $\frac{1}{2}$ 

$$y = \sqrt{z^2 - x^2}$$

$$y = \sqrt{z^2 - x^2}$$

Example:

If x is positive number and  $x^2 - 25 = 56$ , what is the value of x.

Solution:

$$x^{2}-25 = 56$$

$$x^{2}-25+25 = 56+25$$

$$x^{2} = 81$$

Taking square root

$$\sqrt{x^2} = \sqrt{81}$$
$$x = \pm 9$$

But x is +ive (given)

$$x = 0$$

Example:

What is the value of  $2^{x+3}$ , when  $3^{x+2} = 81$ ?

$$3^{x+2} = 81 \implies 3^{x+2} = 3^4 \implies x+2=4$$

$$\implies x = 2$$
Now
$$2^{x+3} = 2^{2+3} = 2^5 = 32$$

$$\therefore 2^{x+3} = 32$$

The Index Laws:

For multiplying and dividing powers, we use some rules. These rules are called index laws.

These rules are summarized below:

Multiplying powers 
$$x^a x^b = x^{a+b}$$

Dividing powers 
$$\frac{x^a}{x^b} = x^{a-b}$$



Power of a power	$(x^{a})^{b}$
	(

Power of a quotient 
$$\left(\frac{x}{y}\right)^a = \frac{x^a}{y^a}$$

Power of a product 
$$(xy)^a = x^a y^a$$

### Special Index:

Zero Index 
$$x^{\circ} = 1$$

Index in fraction 
$$x^{1/a} = \sqrt[a]{x}$$

Index in negative form 
$$x^{-a} = \frac{1}{x^a}$$

#### Example:

Find the value of x when  $27^{-2x+1} = 729^{-2x+3}$ 

#### Solution:

$$27^{-2x+1} = 729^{-x+3}$$
Take L.H.S. 
$$27^{-2x+1} = (3^3)^{-2x+1} = 3^{3(-2x+1)} = 3^{-6x+3} \dots (1)$$

by Power of a power in Index law

Now take R.H.S. 
$$729^{-x+3} = (3^6)^{-2x+3} = 3^{6(-2x+3)} = 3^{-12x+18}$$
.....(2)

$$3^{-6x+3} = 3^{-12x+18}$$

$$\Rightarrow \qquad -6x + 3 = -12x + 18$$

$$\Rightarrow -6x + 12x = 18 - 3$$

$$6x = 15 \Rightarrow x = \frac{15}{6}$$

$$\Rightarrow \qquad \boxed{x = \frac{5}{2}}$$

#### Check:

Substitute 
$$x = \frac{5}{2}$$
 in given equation  

$$27^{-2 \times 5/2 + 1} = 729^{-2 \times 5/2 + 3}$$

$$27^{-4} = 729^{-2}$$

$$(3^{3})^{-4} = (3^{6})^{-2}$$

$$3^{-12} = 3^{-12}$$

Hence the solution is correct.

### Systems of Linear Equations:

A system of equation is two or more equations considered together. If the equations in a system are linear, then it is called linear system of equations. The following system of the equations is a linear system of equations in two variables

$$\begin{cases} x + y = 3 \\ x - y = 3 \end{cases}$$

## Simultaneous Equations:

A pair of equation which has two unknown, and are solved together, are called simultaneous equation. In simultaneous equations the values of unknown quantities satisfied both the given equations.

$$3x + 5y = 9$$
$$3x + 7y = -19$$

### Solution of a System of Equations:

The solution of a system of equation is an order pair that is a solution of both equations.

This system of equations can be solved by following two method

- (1) Substitution Method
- (2) Elimination Method

### (1) Substitution Method:

This method is illustrated in the following example:

#### Example:

Solving the following system of equations using substituting method

$$3x - 4y = 2$$
$$4x + 3y = 14$$

Solution:

$$3x - 4y = 2$$
 ......(1)  
 $4x + 3y = 14$  ......(2)

Solving equation (1) for x in terms of y

$$3x - 4y = 2 \Rightarrow 3x = 4y + 2 \Rightarrow x = \frac{4y + 2}{3}$$

Substituting the value of  $x = \frac{4y + 2}{3}$  in (2)

$$4\left(\frac{4y+2}{3}\right) + 3y = 14 \dots (3)$$

To get rid of friction multiply both sides of the equation (3) by 3

$$4(4y+2) + 9y = 42$$

$$\Rightarrow 16y + 8 + 9y = 42$$

$$\Rightarrow 25y = 34$$

$$\Rightarrow y = \frac{34}{25}$$

To find the value of "x" substitute  $y = \frac{34}{25}$ , in equation (1) or (2). Here we substitute it in equation (1)

$$3x - 4\left(\frac{34}{25}\right) = 2$$

$$75x - 136 = 50$$

$$75x = 186$$

$$x = \frac{186}{75}$$

$$x = \frac{62}{25}$$

The solution of the equation in the form of order pair is  $\left(\frac{62}{25}, \frac{34}{25}\right)$ .

### **Elimination Method:**

The process by which we get rid of either of the unknown quantities is called elimination. In this method one of the unknown is eliminated by adding or subtracting one equation from the other.



Note: Since multiplying each side of an equation by the same non-zero constant does not change the solution of the equation. Therefore, if the coefficient of the unknown are not the same size, one or both equations are first multiplied by an appropriate number.

#### Example 1:

Solve  

$$x + 2y = 22$$
 .....(1)  
 $x - 2y = 2$  .....(2)

#### Solution:

Since y terms have equal but opposite coefficient, eliminate by adding

$$x + 2y = 22$$
 ......(1)  
 $x - 2y = 2$  .....(2)  
(by adding)  $2x = 24$   
 $x = 12$ 

Substitute 
$$x = 12 \text{ in } (1)$$

$$12 + 2y = 22 \Rightarrow 2y = 10$$

$$y = 5$$

Solution set is (12, 5)

### Example 2:

Solve  

$$3x + 6y = 11$$
 .....(1)  
 $2x + 4y = 9$  .....(2)

#### Solution:

In above system of equations, to eliminate the x variable. Multiplying equation (1) by 2 and equation (2) by -3. Then add the resultant equation and solve for y

$$6x + 18y = 11 \dots (1)$$

$$-6x - 12y = -27 \dots (2)$$

$$6y = -5$$

$$y = -\frac{5}{6}$$

Note: The multipliers we chosen so that the coefficient of the variables we want to eliminate are additive inverses.

Substitute 
$$y = -\frac{5}{6}$$
 in (1)  
 $3x + 6\left(\frac{-5}{6}\right) = 11 \implies 3x = 16 \Rightarrow \boxed{x = \frac{16}{3}}$ 

Solution is 
$$\left(\frac{16}{3}, -\frac{5}{6}\right)$$

#### Example 3:

What is the arithmetic mean (average) of x and y, when 3x + 4y = 21, and 4x + 3y = 35

$$3x + 4y = 21 \dots (1)$$

$$4x + 3y = 35 \dots (2)$$

$$7x + 7y = 56$$

$$7x + 7y = 56 \Rightarrow 7(x + y) = 56 \Rightarrow x + y = 8$$

Arithmetic mean of x and y is  $\frac{x+y}{2} = \frac{8}{2} = \boxed{4}$ 

# Multiple Choice Questions (MCQs)

- Q1. If 3x + 9 = 18, what is the value of x + 3?
  - (A) 3

**(B)** 6

**(C)** ~3

- **(D)** 36
- Q2. If 5x + 12 = 44, what is the value of 5x 12?
  - (A) 24

**(B)** 32

(C) 20

- (D) 22
- Q3. If 3x + 17 = 9 x, what is the value of x?
  - (A) 2

(B)

(C) -2

**(D)** −3

3

- Q4. If x 5 = 9, what is the value of  $x^2 5$ ?
  - (A) 196

**(B)** 191

(C) 16

- **(D)** 11
- Q5. If at b = c dt, what is the value of t in terms of a, b, c and d?
  - $(A) \quad \frac{b-c}{a-d}$

(B)  $\frac{a}{b}$ 

(C)  $\frac{c}{d}$ 

- (D)  $\frac{b+c}{a+d}$
- Q6. If  $\frac{1}{2}x + \frac{1}{4}x + \frac{1}{8}x = 22$ , what is the value of x?
  - (A) 88

(B) 44

(C) 1

- (D) 24
- Q7. If 2x-3 = 15, what is the value of  $(2x-3)^2$ ?
  - (A) 81

(B) 227

(C) ±225

- (D) 225
- Q8. If  $81^{10} = 3^{x-7}$ , what is the value of x?
  - (A) 47

(B) 27

(C) 51

(D) 14

- Q9. If  $\frac{1}{x-y} = 7$ , then x =
  - (A)  $x + \frac{1}{7}$

**(B)**  $x - \frac{1}{7}$ 

Q:

Q2

Q2

(C)  $\frac{1}{7} - x$ 

- **(D)**  $\frac{x}{7} 1$
- Q10. If x = 2t + 5, and  $y = 4t^2$ , what is y in terms of x?
  - (A)  $\left(\frac{x-5}{2}\right)^2$

 $(B) \qquad \frac{x+5}{2}$ 

(C)  $(x-5)^2$ 

- (D)  $\frac{x-5}{4}$
- Q11. If x is a positive number and  $x^2 + 36 = 100$ , what is the value of x?
  - (A) 6

(B) 8

**(C)** 14

**(D)** 64

Q12. If $4^{x+5}$ :	$=8^{x-1}$ , what	is the	value	of x?
---------------------	-------------------	--------	-------	-------

(A) 
$$\frac{3}{5}$$

**(B)** 
$$-\frac{5}{3}$$

(C) 
$$-\frac{3}{5}$$

Q13. If 
$$\sqrt{x} = 9$$
, then  $x^2 - \sqrt{x}$  equals:

**(D)** 
$$\sqrt{6} - 9$$

Q14. If 
$$\frac{a+3}{6} = \frac{12}{a+4}$$
, then positive value of x equals:

Q15. If x and y are positive integers and 
$$x^2 + 2y^2 = 41$$
,  $2x^2 + y^2 = 34$ , then  $x^2 = 41$ 

$$(A) = 6$$

Q16. For any positive integer 
$$p$$
,  $\$p = \frac{p^2}{3}$  and  $\pounds p = \frac{9}{p}$ , which of the following is an expression for the product of  $\$p$  and  $\pounds p$ ?

(A) 
$$\frac{2}{p}$$

(B) 
$$\frac{1}{p}$$

(D) 
$$3p$$

Q17. If a, b, and c are different positive odd integers and 
$$a + b + c = 11$$
, what is the greatest positive value of  $c$ ?

$$(\mathbf{D})$$

Q18. If 
$$n + 5 = n \times 5$$
, then  $n = 1$ 

$$(C) = 0.5$$

Q19. If 
$$\frac{a}{b} = .75$$
, then  $4a - 3b =$ 

$$(\mathbf{C}) = 0$$

$$(\mathbf{D})$$
 3

Q20. Let 
$$ab = c$$
, where a, b and c are non zero numbers. If a is multiplied by 3 and c is divided by 3, this is equivalent to multiply b by:

$$(\mathbf{A}) = \frac{1}{2}$$

**(D)** 

Q21. If 
$$5a = 3$$
, then  $(5a + 3)^2 = ?$ 

$$(C)$$
 4

Q22. If 
$$a = \frac{1}{3}$$
, then  $a^3 = ?$ 

(A) 
$$\frac{1}{9}$$

**(B)** 
$$\frac{1}{3}$$



(D) 
$$\frac{1}{27}$$

Q23. If 3a - 5 = 7, what is the value of a?

(A) 
$$\frac{2}{3}$$

Q24. If  $4 + \frac{5W}{2} = 19$ , what is the value of W?

Q25. What is the value of (11 - y) when 121 - 11y = 77?

$$(C)$$
 7

Q26. What is the value of  $x^2 - 4$ , when  $x^6 - 4x^4 = 64$  and  $x^2 = 4$ ?

Q27. One factor of  $8x^3 - 27y^3$  is (2x - 3y), what is the other factor?

(A) 
$$(2x + 3y)$$

**(B)** 
$$(4x^2 + 9y^2)$$

(C) 
$$(4x^2 + 6xy + 9y^2)$$

(D) 
$$(4x^2 + 12xy + 9y^2)$$

Q28. If  $32^{x+y} = 16^{x+2y}$ , then x =

(C) 
$$\frac{y}{3}$$

Q29. If px - q = r - sx, what is the value of x?

(A) 
$$\frac{p+s}{r+q}$$

(B) 
$$\frac{r+q}{p+s}$$

(C) 
$$\frac{r-q}{p+s}$$

(D) 
$$\frac{r-q}{p-s}$$

Q30. If one factor of  $a^2 - b^2 + am + bm$  is a + b, then the other factor is

(A) 
$$(a + b - m)$$

(B) 
$$(a-m)$$

(C) 
$$(b-m)$$

(D) 
$$(a - b + m)$$

# Explanatory Answers

Q1. (B)  $3x + 9 = 18 \Rightarrow 3(x + 3) = 18$ (Taking 3 common from L.H.S) 3(x + 3) = 18

$$\Rightarrow \frac{3(x+3)}{3} = \frac{18}{3} \Rightarrow x+3 = 6 \text{ (Dividing both sides by 3)}$$

Q2. (C) Given that 5x + 12 = 44, subtracting -24 on both sides of the given equation, we have 5x + 12 = 24= 44 - 24

$$\Rightarrow 5x - 12 = 20$$

Q3. (C) 3x + 17 = 9 - x  $\Rightarrow 3x + x = 9 - 17$ 

$$\Rightarrow 4x = -8$$

$$\Rightarrow x = \frac{-8}{4} = -2$$

(adding 5 both sides of the equation)

$$\Rightarrow x = 14 \Rightarrow x^2 = (14)^2 = 196$$
Now  $x^2 - 5 = 196 - 5 \Rightarrow x^2 - 5 = 191$ 

Q5. (D) 
$$at - b = c - dt$$
  $\Rightarrow at + dt = b + c$   
 $\Rightarrow t(a + d) = b + c$   
 $\Rightarrow t = \frac{b + c}{a + d}$ 

Q6. (D) 
$$\frac{1}{2}x + \frac{1}{4}x + \frac{1}{8}x = 21$$
, (taking L.C.M, 8)  $\frac{4x + 2x + x}{8} = 21$ , Multiplying both sides by 8, we have

$$\frac{7x}{8} \times 8 = 21 \times 8 \qquad \Rightarrow 7x = 21 \times 8$$

$$\Rightarrow x = \frac{21 \times 8}{7}$$

$$\Rightarrow x = 3 \times 8$$

$$\Rightarrow x = 24$$

**Q7. (D)** Given that 
$$2x - 3 = 15$$

Taking square both sides of the equation, we get

$$(2x+3)^2 = (15)^2$$
  

$$(2x+3)^2 = 225$$

Q8. (A) 
$$81^{10} = 3^{x-7}$$
  
 $(3 \times 3 \times 3 \times 3)^{10} = 3^{x-7}$   
 $(3^4)^{10} = 3^{x-7}$   
 $3^{40} = 3^{x-7}$   
 $\Rightarrow 40 = x-7$   
 $\Rightarrow 40+7 = x-7+7$   
 $\Rightarrow x = 47$ 

Q9. (B) 
$$\frac{1}{x-y} = 7$$
, Multiplying both sides of the equation by  $(x-y)$ , we have

$$\frac{1}{x-y} \times (x-y) = 7 \times (x-y)$$

$$1 = 7x - 7y$$

$$\Rightarrow 7y = 7x - 1 \qquad \Rightarrow y = \frac{7x - 1}{7}$$

$$\Rightarrow y = x - \frac{1}{7}$$

Q10.(C) Let 
$$x = 2t + 5...(i)$$
 and  $y = 4t^2$  ...(ii)  
Solving (i), for  $t$ 

$$x = 2t + 5 \Rightarrow x - 5 = 2t + 5 - 5$$
$$\Rightarrow x - 5 = 2t \Rightarrow \frac{x - 5}{2} = \frac{2t}{2}$$

Q

$$\Rightarrow \frac{x-5}{2} = t$$

Putting the value of t in (ii), we have

$$y = 4\left(\frac{x-5}{2}\right)^2$$
$$y = \frac{4}{4}(x-5)^2 \Rightarrow y = (x-5)^2$$

Q11.(D) 
$$x^2 + 36 = 100$$
  $\Rightarrow x^2 + 36 - 36 = 100 - 36$   
 $\Rightarrow x^2 = 64$   
 $\Rightarrow \sqrt{x^2} = \sqrt{64}$   
 $\Rightarrow x = \pm 8$ 

Since x is positive  $\Rightarrow$  x = 8

Q12.(B) 
$$4^{x+5} = 8^{x-1}$$

$$\Rightarrow (2 \times 2)^{x+5} = (2 \times 2 \times 2)^{x-1}$$

$$\Rightarrow (2^2)^{x+5} = (2^3)^{x+5}$$

$$\Rightarrow 2^{2 \times (x+5)} = 2^{3(x+5)}$$

$$\Rightarrow 2^{2x+10} = 2^{3x+15}$$

$$\Rightarrow 2x+10 = 3x+15$$

$$\Rightarrow 2x-3x = 15-10$$

$$\Rightarrow -3x = 5$$

$$\Rightarrow \frac{-3x}{-3} = \frac{5}{-3}$$

$$\Rightarrow x = -\frac{5}{3}$$

Q13.(C) 
$$\sqrt{x} = 9 \Rightarrow x = 81 \Rightarrow x^2 = 6561$$
  
Now  $x^2 - \sqrt{x} = 6561 - 9$   
 $\Rightarrow x^2 - \sqrt{x} = 6552$ 

Q14.(A) 
$$\frac{a+3}{6} = \frac{12}{a+4}$$
  $\Rightarrow$   $(a+3)(a+4) = 12 \times 6$   
 $\Rightarrow$   $a^2 + 7a + 12 = 72$   
 $\Rightarrow$   $a^2 + 7a + 12 - 72 = 0$   
 $\Rightarrow$   $a^2 + 7a - 60 = 0$   
 $\Rightarrow$   $a^2 + 12a - 5a - 60 = 0$   
 $\Rightarrow$   $a(a+12) - 5(a+12) = 0$   
 $\Rightarrow$   $(a-5)(a+12) = 0$   
 $\Rightarrow$   $a=5,-12$ 

Q15.(D) Given 
$$2x^2 + y^2 = 34$$
  
 $\Rightarrow y^2 = 34 - 2x^2$   
Substituting the value of  $y^2$  in the first equation

$$x^{2} + 2y^{2} = 41$$
, gives  
 $x^{2} + 7(34 - 2x^{2}) = 41$   
 $\Rightarrow x^{2} + 68 - 4x^{2} = 41$ 

$$\Rightarrow -3x^2 = 41 - 68 \Rightarrow -3x^2 = -27$$
$$\Rightarrow 3x^2 = 27 \Rightarrow x^2 = \frac{27}{3} \Rightarrow x^2 = 9$$

Q17.(B) The set of positive odd integers is  $\{1,3,5,7,9.....\}$ 

The sum of the three positive integers should be 11. If we take greatest possible value of c, then there exist least positive integers a and b, the value of least positive integers a and b is 1 and 3, so their sum = 1 + 3 = 4. Thus the greatest positive integer is  $1 + 3 + c = 11 \Rightarrow 4 + c = 11$ 

$$\Rightarrow c = 7$$

Q18.(A) Given that 
$$n + 5 = n \times 5$$

Subtracting n both sides of the equation

$$n + 5 - n = 5n - n$$

$$5 = n(5 - 1) \text{ (Taking } n \text{ common)}$$

$$5 = 4n$$

$$\Rightarrow \frac{5}{4} = \frac{4n}{4} \text{ (Dividing both sides by 4)}$$

$$\Rightarrow n = 1.25$$

Q19.(C) 
$$\frac{a}{b} = .75$$
  $\Rightarrow \frac{a}{b} = \frac{75}{100} \Rightarrow \frac{a}{b} = \frac{3}{4}$   
 $\Rightarrow 4a = 3b \Rightarrow 4a - 3b = 0$ 

Q20.(C) 
$$ab = c$$
 ...(1)

If a is multiplied by 3, and c is divided by 3, the above equation becomes

$$3ab = \frac{c}{3} \qquad \dots (2)$$

The above equation (2), is equivalent to (1), if b is multiplied by  $\frac{1}{9}$ 

$$3a \times \frac{1}{9}b = \frac{c}{3}$$

$$\frac{1}{3}ab = \frac{c}{3} \qquad \text{As } ab = c$$

$$\frac{1}{3}c = \frac{c}{3} \implies c = c$$

Q21.(B) 
$$5a = 3 \Rightarrow 5a - 3 = 0$$
 ...(1)

Adding 6 both sides of equation (1), we get

$$5a-3+6=0+6 \Rightarrow 5a+3=6$$
 ...(2)

Squaring both sides of equation (2), we get

$$(5a+3)^2 = (6)^2 = (5a+3)^2 = 36$$

Q22.(D) 
$$a = \frac{1}{3}$$
  $\Rightarrow (a)^3 = \left(\frac{1}{3}\right)^3$   
 $\Rightarrow a^3 = \frac{1 \times 1 \times 1}{3 \times 3 \times 3}$ 

$$\Rightarrow a^3 = \frac{1}{27}$$

**Q23.** (B) 
$$3a-5 = 7$$

$$\Rightarrow$$
 3a - 5 + 5 = 7 + 5 (adding 5 both sides)

$$\Rightarrow$$
 3a = 12

$$\Rightarrow$$
  $a = 4$ 

**Q24.** (A) 
$$4 + \frac{5W}{2} = 19$$

$$\Rightarrow$$
 4 +  $\frac{5W}{2}$  - 4 = 19 - 4 (To get rid 4 from L.H.S. subtract 4 both sides)

$$\Rightarrow \frac{5W}{2} = 15$$
 (To get rid 2 from L.H.S. multiply 2 both sides)

$$\frac{5W}{2} \times 2 = 15 \times 2 \quad \Rightarrow \quad 5W = 30$$

last to get rid 5 from L.H.S. divide both sides by 5

$$\frac{5W}{5} = \frac{30}{5}$$
  $\Rightarrow$   $W = 6$ 

$$11(11 - y) = 77$$
 Dividing 11 both sides

$$\frac{11(11-y)}{11} = \frac{77}{11}$$

$$\Rightarrow$$
 11 - y = 7

**Q26.** a) Given 
$$x^6 - 4x^4 = 64$$
 and  $x^4 = 4$ 

$$x^4(x^2-4) = 64$$
 (Taking  $x^4$  common)

$$4(x^2 - 4) = 64$$
 (Substituting the value of  $x^4$ )

$$\Rightarrow$$
  $x^2 - 4 = 16$  (Dividing both sides by 4)

**Q27.** (C) 
$$8x^3 - 27y^3$$

$$\Rightarrow$$
  $(2x)^3 - (3y)^3 = (2x - 3y)(4x^2 + 6xy + 9y^2)$  (factorizing)

**Q28.** (D) 
$$32^{x+y} = 16^{x+2y}$$

$$(2)^{5(x+y)} = (2)^{4(x+2y)} \Rightarrow 2^{5x+5y} = 2^{4x+8y}$$

$$\Rightarrow 5x+5y = 4x+8y$$

$$\Rightarrow 5x-4x = 8y-5y$$

$$\boxed{x = 3y}$$

**Q29.** (B) 
$$px - q = r - sx$$

$$px + sx = r + q$$

$$\Rightarrow$$
  $x(p+s) = r+q$ 

$$x = \frac{r + q}{p + s}$$

**Q30.** (D) 
$$a^2 - b^2 + am + bm$$

$$(a-b)(a+b) + m(a+b)$$
 as  $a^2 - b^2 = (a+b)(a-b)$ 

$$(a+b)(a-b+m)$$

Chapter 3

### **INEQUALITY**

An inequality, or inequation is a statement which involves one of the sign below:

- < Less than
- ≤ Less than or equal to
- > Greater than
- ≥ Greater than or equal to

Examples:

$$\begin{array}{rrr}
-6x & > 52 \\
11y & \ge -101 \\
-3x & \le 8 \\
-52w & < 9
\end{array}$$

The set of all solutions of an inequality is called the solution set of the inequality. For example the solution of x + 3 > 5 is the set of all real numbers greater than 2.

Note:

Equivalent Inequalities have the same solution set.

Representation of Inequality on number line:

Inequalities such as x > 3 or  $x \le 3$  can be represented on number line.

In following number line a circle " $\square$ " shows that x is included and a rectangle "O" shows that it is not

$$x \le 3$$
  $-4$   $-3$   $-2$   $-1$   $0$   $1$   $2$   $3$   $4$   $5$   $6$   $7$ 

Note:

1. Any quantity x is said to be greater than another quantity y when (x - y) is positive.

Example:

If 
$$x = 2$$
 and  $y = -3$ , thus  $x > y$  because  $2 - (-3) = 5$  or positive.

2. y is said to be less than x when y - x is negative.

Example:

If 
$$x = 2$$
 and  $y = -3$ , than  $y < x$  because  $-3 - 2 = -5$  or negative.

Properties of Inequalities:

We apply the following properties to solve in-equalities.

1. An inequality will still hold after each side has been increased, decreased, multiplied or divided by the same positive quantity

For example: 
$$x > y$$
  
 $x + z > y + z$ ;  
 $x - z > y - z$ ;  
 $xz > yz$ ;  
 $x = xz > yz$ ;

2. In an un-equality any term may be transposed from one side to the other if its sign be changed

If 
$$x-y > z$$

For example: x > z + y

3. If the sides of an inequality is transposed, then the sign of inequality is reversed

Example: If x > y, then evidently

4. If both sides of the inequality are multiplied or divided by a negative number, then direction of the inequalities sign is reversed

Example: If x > y, then -x < y and

$$-xz < yz$$

5. The square of real quantity is positive, therefore it is greater than zero.

Therefore $(x - y)^2$  is always positive

$$\therefore (x-y)^2 > 0$$
  
 
$$\therefore x^2 + y^2 > 2xy$$

**6.** If x and y are two positive quantities, then their arithmetic mean  $\left(\frac{x+y}{2}\right)$  is greater than their geometric mean  $(\sqrt{xy})$ .

$$\frac{x+y}{2} > \sqrt{xy}$$

Example:

Solve the following inequalities

(i) 
$$3x - 11 < 13$$
 (ii)  $\frac{-x}{2} \le 2$ 

Solution:

(i) 
$$3x - 11 < 13$$
  
 $3x - 11 + 11 < 13 + 11$  (using property 1)

$$\therefore \qquad 3x < 24$$

$$3x < 24$$

$$\frac{3x}{3} < \frac{24}{3} \text{ (using property 1)}$$

$$x < 8$$

$$\therefore$$
  $x < 8$ 

$$\frac{-x}{2} \leq 2$$

$$\frac{-x}{2} \times 2 < 2 \times 2$$
 (by property 1)

$$-x \leq 4$$

$$-x \le 4$$

$$-x \times -1 \ge 4 \times -1 \text{ (using property 4)}$$

$$x > -4$$

$$x \ge -4$$

Example: Find the greatest possible value of x, when the arithmetic mean of 5, 7 and x is less than 24. Solution:

The arithmetic mean of three numbers 5, 7 and x is

$$\frac{5+7+x}{3}$$

By given condition  $\frac{5+7+x}{3}$  < 24

Now 
$$\frac{(5+7+x)}{3} \times 3 < 24 \times 3$$
 (using property 1)

$$12 + x < 72$$

$$12 + x - 12 < 72 - 12$$
 (using property 1)

Thus the greatest possible value of x is 59.

Example:

Solve 
$$\frac{x}{4} - 4 > \frac{x}{5}$$

Solution:

$$\frac{x}{4} - 4 > \frac{x}{5}$$



$$\frac{x}{4} - \frac{x}{5} - 4 + 4 > \frac{x}{5} - \frac{x}{5} + 4 \qquad \text{(using property 1)}$$

$$\frac{x}{4} - \frac{x}{5} > 4$$

$$\frac{5x - 4x}{20} > 4$$

$$\frac{x}{20} > 4$$

$$\frac{x}{20} > 20 > 4 \times 20 \quad \text{(using property 1)}$$

$$\frac{x}{20} \times 20 > 4 \times 20$$
 (using property 1)

Q1. If xy > 0 and x < 0, which of the following negative?

**(A)** 

**(B)** 

**(C)** 

**(D)** 

Q2. If a > 0, b > 0 and a - b < 0, then?

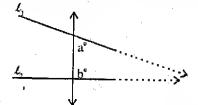
**(A)**  $a \le b$ 

**(B)** a+b<0

**(C)** 

b-a < 0**(D)** 

If lines  $\ell_1$  and  $\ell_2$  meet when extended to the right, which inequality best expresses the relationship Q3. between a and b?



(A) 
$$a = b$$

**(B)** a + b < 180

**(C)** a - b > 0 (D) b - a > 0

Q4. If a + b > 7 and a - b > 5, then which of the following gives all possible values of a and only possible value of a?

**(A)** 

**(B)** a < 5,

(C) a > 4 **(D)** 

If A > B an C < 0, then which of the following is not true? Q5.

AC < BC

**(C)**  $A - C \le B - C$ 

a > 6

A + C > B + C**(B)** 

**(D)** All of the above Q6. If a = 1 and 1 > b > 0, then which of the following statement is true?

**(A)** 

b > a**(B)** 

 $\frac{1}{b} > a$ (C)

 $\frac{1}{a} < b$ **(D)** 

Q7. If  $a \le c$  and  $a \le b$ , assume  $a \ge 0$  then which of the following statements are always true?

- (i) b < c
- (ii) a < bc
- (iii) 2a < b + c
- (A) . only (i)

**(B)** only (ii)

**(C)** only (iii)

**(D)** (i) and (ii)

a > -1

Q8. If 6 - a > 7, then

> (A) a > 1

**(B)** 

 $a \le -1$ 

**(D)** a < 1

Q9. a has to be a whole number such that  $0 \le a \le 10$ . The solution for a < 4 and  $a \ge 6$  is:

- (A)

(B)

**(C)** 

**(D)** no solution



Q10. If $5x > 2$ and $\frac{1}{2}x \le 4$ , list all the possible integral v	values of x?
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(A) 2, 3, 4, 5, 6

**(B)** 1, 2, 3, 4, 5, 6, 7, 8

(C) 2, 3

- **(D)**
- Q11. The solution of the inequality  $-1 < 5x 6 \le 4$  in whole number is
  - (A) 1

**(B)** 2

**(C)** 4

- $(\mathbf{D})$  5
- Q12. In inequality y > 3x 2 if a > b, then which of the following statement is true?
  - (A) x = 1

(B) x > 1

(C) x < 1

- (D)  $x \ge 1$
- Q13. If  $\frac{a}{2} 2 > \frac{a}{3}$ , then which of the following statement is true?
  - $(A) \qquad a < 12$

 $(B) \qquad a \ge 12$ 

(C) a = 12

- (D)  $a \ge 12$
- Q14. Which of the following inequalities is the solution of the inequality 7a 5 < 2a + 18?
  - $(A) \qquad a < 23$

(B) a > 13

(C)  $a \le 23$ 

- (D)  $a \ge 13$
- Q15. For which values of p is  $p^2 5p + 6$  negative?
  - (A) p < 0

(B) 2

(C) x > 3

(D) x < 2

# Explanatory Answers

- Q1. (C) The product of two numbers > 0 is only possible when either both numbers are positive or both are negative. Since x < 0, y must also be negative.
- Q2. (A) In this case a and b are both positive (a > 0, b > 0), but a b is negative, which is only possible when a < b.
- Q3. (B) When the lines will be extended to the right. They will make a triangle, and the sum of the angles of the triangle is 180°. Therefore, the sum of the two angles in a triangle is less than 180°.
- Q4. (A) Since both inequalities have the same direction, therefore the corresponding sides can be added. Thus,

$$a+b>7$$

$$\frac{a-b>5}{2a>12}$$

Q5. (C)  $\frac{a > 6}{\text{If } A > B \text{ and } C < 0$ , then multiplication of both sides by C reverses the inequality. Which implies

AC < BC. Also adding and subtracting in inequality, gives

$$A+C>B+C$$
 and

$$A-C \ge B-C$$

But  $A - C \le B - C$  is not possible.

Q6. (C) Since b is a +ve fraction less than 1, therefore  $\frac{1}{b}$  is a positive fraction greater than 1. Hence

$$\frac{1}{h} > a$$

- Q7. (C) Statements (i) and (ii) are not always true.
- **Q8.** (C) Given 6 a > 7

$$\Rightarrow$$
 -a > 1

Dividing both sides by -1. This will reverse the inequality sign

$$a \le -1$$

Q9. (D) Given set is  $\{0,1,2,3,4,5,6,7,8,9,10\}$ , the number a < 4 are  $\{0,1,2,3\}$  and the numbers  $a \ge 6$  are  $\{6,7,8,9,10\}$ . Since there are no common elements between the last two sets. Therefore, there

is no solution of the inequality.

Q10. (B) 
$$5x > 2$$
  $\frac{1}{2}x \le 4$   $x > \frac{2}{5}$   $\frac{1}{2}x \times 2 \le 4 \times 2$ 

from above the integers greater than  $\frac{2}{5}$  and less than and equal to 8 are 1,2,3,4,5,6,7,8

Q11. (B) Given 
$$-1 < 5x - 6 \le 4$$
, first of all get rid  $-6$  then 5 in the middle term To get rid  $-6$ , add 6 to each part  $-1 + 6 < 5x - 6 + 6 < 4 + 6$ 

$$\Rightarrow$$
 5 < 5x < 10

To get rid of 5, divide each part by 5.

$$\frac{5}{5} < \frac{5x}{5} < \frac{10}{5}$$
$$1 < x \le 2$$

only 2 is a whole number solution

Q12. (C) Since 
$$x > y$$
 and  $y > 3x - 2$ , this implies that  $x > 3x - 2 \implies -2x > -2$ 

Dividing both sides by -2 will reverse the inequality symbol

$$\frac{-2x}{-2} < \frac{-2}{-2}$$

$$\Rightarrow x < 1$$

Q13. b) Given 
$$\frac{a}{2} - 2 > \frac{a}{3}$$

adding  $\frac{-a}{2}$  both sides of the inequality

$$\frac{a}{2} - 2 - \frac{a}{2} > \frac{a}{3} - \frac{a}{2}$$
$$-2 > \frac{-a}{6} \Rightarrow \frac{-a}{6} < -2$$
$$-a < -12$$

dividing both sides by -1 will reverse the inequality sign, therefore

$$a \ge 12$$

Q14. (A) 
$$7a-5 < 2a+18$$
  
 $7a-2a < 18+5$   
 $5a < 23$   
 $\Rightarrow a < 23$ 

Q15. (B) Given  $p^2 - 5p + 6$ . The given expression factors into (p - 3)(p - 2). If the expression is negative then the factors must have opposite signs. If (p - 2) is negative and (p - 3) is positive there are no such number. It is only possible when (p - 3) is negative and (p - 2) is positive, then p > 2 and p < 3. So, 2 is the correct choice.

# Chapter 4

# WORD PROBLEMS

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<ul> <li>Q9. Mohin is now three times Mohsin's age. Four years from now Mohin will be y years old. In terms of y, how old will Mohsin be?</li> <li>(A) x-4/3</li> <li>(B) x+4/3</li> <li>(C) x+4</li> <li>(D) x-4</li> <li>Q10. If the sum of one third of a number and twice the same number is 28, the number is: <ul> <li>(A) 10</li> <li>(B) 12</li> <li>(C) 28</li> <li>(D) 14</li> </ul> </li> </ul>		(A)	5	(B)		
terms of y, how old will Mohsin be?  (A) $\frac{x-4}{3}$ (B) $\frac{x+4}{3}$ (C) $x+4$ (D) $x-4$ Q10. If the sum of one third of a number and twice the same number is 28, the number is:  (A) $10$ (B) $12$ (C) $28$ (D) $14$						
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(C) $x+4$ (D) $x-4$ Q10. If the sum of one third of a number and twice the same number is 28, the number is:  (A) 10 (B) 12 (C) 28 (D) 14		terms of y,				
(C) $x+4$ (D) $x-4$ Q10. If the sum of one third of a number and twice the same number is 28, the number is:  (A) 10 (B) 12 (C) 28 (D) 14	1	(A)	$\underline{x-4}$	(B)	$\frac{x+4}{2}$	
Q10. If the sum of one third of a number and twice the same number is 28, the number is:  (A) 10 (B) 12 (C) 28 (D) 14		(11)	3	(2)	3	
(A) 10 (B) 12 (C) 28 (D) 14						_
(C) 28 (D) 14	Q10.	If the sum	-			e number is:
(*)	ŀ	(A)				
Q11. A man's present age is x years. If his age in 8 years will be $\frac{4}{5}$ of what it will be in 20 years, then						
	011	A man's n	resent age is y years. If his	s age in 8 years will b	$\frac{4}{5}$ of what it	will be in 20 years, then
· · · · · · · · · · · · · · · · · · ·	<sup> </sup>	т шан э р	resent age is a years. If the	suge in o years will t	5 5 7 77 77 77 78 78 78 78 78 78 78 78 78 7	
	L					

his present age is:

(C)

- (A) 45
  - 45 30 (B)
- Q12. When 42 is added to twice a number, the result is 346, the number is:
  - (A) 304

**(B)** 242

25

40

**(C)** 152

- **(D)** 265
- Q13. A man was 26 years old when his daughter was born. Now, he is three times as old as his daughter. How many years old is the daughter now?
  - (A) 13 years

(B) 22 years

(C) 15 years

- (**D**) 12 years
- Q14. 13 years ago Shabbir's mother was 7 times as old as he was. She is now 48 years old. How many years old is Shabbir now?
  - (A) 28

**(B)** 18

(C) 38

- $(\mathbf{D})$  20
- Q15. If 5 years are added to a man's present age and that age is tripled, he will be 84. What is his present age?
  - (A) 18

(B) 23

(C) 32

 $(\mathbf{D})$  54

# E Explanatory Answers

- Q1. (A) Let the required number be x. Then x 5 = 2x 7
  - $\Rightarrow$  x = 2. Thus the correct answer is 2.
- Q2. (C) Let

e

is

as

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x =first integer

- x + 2 = second integer
- x + 4 = third integer
- 3(x) = 3 + 2(x+4)
  - 3x = 3 + 2x + 8
  - x = 11

Third integer is (x+4) = 15

Q3. (A) Let the number = x, then

$$\frac{2}{5}x = 30$$

$$\Rightarrow \qquad x = \frac{30 \times 5}{2}$$

$$\Rightarrow$$
  $x = 75$ 

Q4. (C)Let the weight of Saira = x and Umber's weight = y

$$x - 25 = y$$

and

$$x + y = 205$$

⇒

$$x - y = 25$$

$$x + y = 205$$

$$2x = 230$$

$$x = \frac{230}{2} = 115$$
 pound

**Q5.** (A)Let the smaller number = x

Then the larger number = 3x

Now

$$3x + x = 36$$

$$4x = 36$$

$$x = 9$$

The larger number is 36 - 9 = 27

**Q6.** (C)  $p + q = 352 \text{ and } \frac{P}{10} = q \Rightarrow p = 10q$ 

$$10q + q = 352 \Rightarrow 11q = 352 \Rightarrow q = 32$$
Now p + 32 = 352 \Rightarrow \begin{pmatrix} p = 320 \\ p = 320 \end{pmatrix}

- Q7. (B) 30 packers will load  $30 \times \frac{1}{8}$  or  $\frac{30}{8}$  boxes in 9 minutes. There are 90 minutes in  $1\frac{1}{2}$  hours. So the 30 packers will load  $10 \times \frac{30}{8}$  or  $37\frac{1}{2}$  boxes in  $1\frac{1}{2}$  hours.
- Q8. (D) Asma is one-third older or  $\frac{1}{3} \times 15 = 5$  years older. Let x be the age of Uzma and x + 5 be Asma's age. When Asma was twice the age of Uzma, 2x = x + 5 or x = 5. Uzma was 5 years old and Asma was x = 5 or 10 years old, twice Uzma's age. Since Uzma is 15 years old now, Uzma was 5 years old 10 years ago.
- Q9. (A) Assume x for Mohin and y for Mohsin

  x is three times  $y \Rightarrow x = 3y$ x in four years  $\Rightarrow x = x + 4$   $\Rightarrow x = 3y + 4$   $\Rightarrow x 4 = 3y$  x = 4
- Q10. (B) Let x be the required number, then

$$\frac{1}{3}x + 2x = 28$$

$$\Rightarrow x + 6x = 84$$

$$\Rightarrow 7x = 84$$

$$\Rightarrow x = 12$$

Q11. (D) Present age = x

$$x + 8 = \frac{4}{5}(x + 20)$$

$$5x + 40 = 4x + 80$$

$$5x - 4x = 80 - 40$$

$$x = 40$$

Q12. (C) Let x be the required number, then

$$2x + 42 = 346$$

$$\Rightarrow 2x = 304$$

$$\Rightarrow x = 152$$

Q13. (A) Let x be the age of man and y be the age of his daughter

$$x-26 = y$$
 .....(1)  
 $x = 3y$  .....(2)

Substituting the value of x in (1)

$$3y - 26 = y$$

$$2y = 26 \implies y = 13$$

Q14. (B) Let x be the age of Shabbir

$$7(x-13) = 48-13$$

$$7(x-13) = 35$$

$$x-13 = 5$$

Q15. (B) Let x be the man's present age, then

$$3(x+5) = 84$$

$$x+5 = 28$$

$$x = 23$$





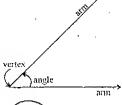
#### Chapter 1

#### LINES AND ANGLES

#### Angle:

An angle is formed by the intersection of two line segments, which may be rays or lines.

In the diagram, an angle is shown by two lines (the arms) meeting at a point. The meeting point or point of intersection is called the vertex.

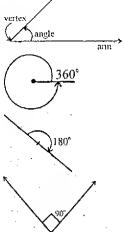


The unit of measure is the degree.

One full turn is 360 degrees (360°)

A half  $\left(\frac{1}{2}\right)$  turn is 180 degrees (180°)

A  $\frac{1}{4}$  turn is 90 degrees (90°).



#### Note:

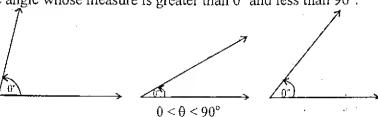
- 1. A half turn (180°) is also called straight angle.
- 2. A  $\frac{1}{4}$  turn (90°) is also called a right angle.

### Classification of Angles:

Angles are classified according to their degree measures.

#### Acute Angle:

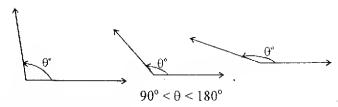
An acute angle is the angle whose measure is greater than 0° and less than 90°.



In all above figures  $\theta$  lies between 0 and 90°.

#### Obtuse Angle:

An angle whose measure is greater than 90° and less than 180° is called obtuse angle. Examples:

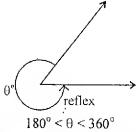


In all above figures 0 lies between 90° and 180°.

#### Reflex Angle:

A reflex angle is between 180° and 360°.

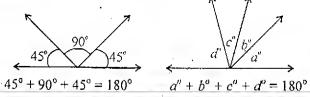
Example:



A reflex angle lies between 180° and 360° degrees.

### Calculating Angles:

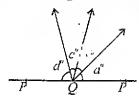
Angles on a straight line add up to 180°.



A straight angle is 180°. So angles on a straight line add up to 180°.

#### Example 1:

What is the average of a, b, c and d in the following figure



#### Solution:

In the given figure since  $\angle PQR$  is a straight angle. Because the angles on a straight line add up to  $180^{\circ}$ , therefore

$$a + b + c + d = 180^{\circ}$$

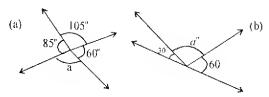
Average is

$$\frac{180^{\circ}}{4} = 45^{\circ}$$

Angles in a full turn add upto 360°.

#### Example 2:

Find the angle a in these diagrams.



#### Solution:

a) 
$$a = 360^{\circ} - (60^{\circ} + 105^{\circ} + 85^{\circ})$$
$$= 360^{\circ} - 250^{\circ}$$



$$b) = 110^{\circ}$$

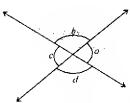
$$a = 180^{\circ} - (60^{\circ} + 30^{\circ})$$

$$= 180^{\circ} - 90^{\circ}$$

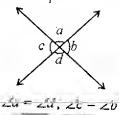
$$= 90^{\circ}$$

#### Vertical Angles:

When two straight lines intersect, they make four angles. The two opposite angles are called vertical angles. In this diagram angles a, c and b, d are vertical angles.

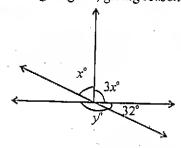


Vertically opposite angles are equal



#### Example 3:

Find the value of pronumerals in the following diagram, giving reasons:



#### Solution:

Because angles on a straight line add up to 180°, and vertically opposite angles are equal:

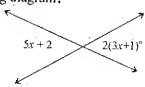
$$3x + x + 32 = 180^{\circ} \Rightarrow 4x = 148 \Rightarrow x = 37^{\circ}$$

$$y^{\circ} = 3x^{\circ} + x^{\circ} \Rightarrow y = 4(37^{\circ}) \Rightarrow y = 148^{\circ}$$

#### Example 4:

Again

What is the value of x in the following diagram?



#### Solution:

Since the vertically opposite angles are equal:

$$5x+11 = 2(3x+1) 
5x+11 = 6x+2 
 x = 9$$

#### Parallel Lines:

Parallel lines are always the same distance apart. They never meet, even if you make them longer. Parallel lines form no angles.

	(A)	65		(B)	55	1
	(C)	35		(D)	Insufficient information	1
13.	In the figuare there in	re, line <i>PQ</i> is nangle c?	parallel to line RS, angle a	$=60^{\circ}$	and angle $b = 140^{\circ}$ . How many degrees	
			P	60"	2	
	٠		b=140°			
			P	S	<b>.</b> .	
	(A)	80	!	(B)	110	Ш
•	(C)	100		(D)	95	
4.	In the fig b	elow, what is 1	the value of $\hat{x}$ ?			
			207/ x <sup>w</sup>			
	(A)	20°		(B)	70°	1
	(C)	100°		( <b>D</b> )	110°	
5.	In the fig be	elow, what is t	the value of a?			1
			<b>₹80°</b>			1
				<del></del>	11	1
						1
			$\bigwedge_{a^n}$			ı,
				<del>&gt;</del>		ľ
						1
	(A)	100°		(B)	60°	ł
6.	(C)	80°		( <b>D</b> )	40°	II.
<b>.</b> .	an the figure	e below, what	is the value of $m + n$ ?			
		,	130° m° 53°			I
	(A)	103°		D)	779	
			(	<b>B</b> )	77°	11
	(C)	13 <b>0</b> °	1	D)	85°	

 $(3x+7)^{\circ}$ 

(A)

61

131°

(B)

 $(7x-30)^{\circ}$ 

42

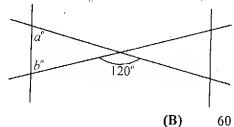
**(C)** 41

- **(D)** 72
- If P, Q and R are points on a line, with B between P and R. Let A and B be the mid points of PQQ18. and QR, respectively. If PQ: QR = 3:1, what is PQ: AB?
  - (A) 3:2

(C) 1.5:.5

1:2 **(D)** 3:1

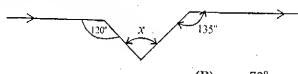
Q19. In the figure below, a + b =



(A) 80

**(C)** 135

- **(D)** 120
- In the figure below, what is the value of x? Q20.

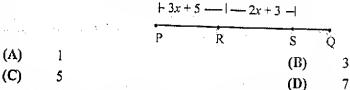


**(A)** 45°

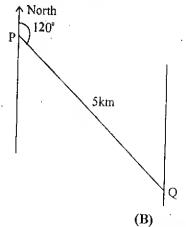
**(B)** 72°

**(C)** 57°

- **(D)** 65°
- In the figure below, if the length of PQ is 5x + 9, what is the length of SQ? Q21.



A ship leaves a port P and sails for 5km on a bearing of  $120^{\circ}$  to a port Q. What is the bearing of Q22.



(A) 60°

120°

**(C)** 40°

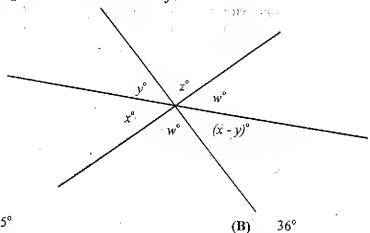
- **(D)** 300°
- **Q23**. A hill-walker set off from P on a bearing of 225° to arrive at Q. What bearing must they take to retrace their steps?
  - 55° **(A)**

**(B)** 135°

**(C)** · 45°

- **(D)** 95°
- In the figure below, the straight line ABC is parallel to DE and BD is parallel to CF. AD = BD,  $DBC = 110^{\circ}$  and  $FED = 45^{\circ}$ . What is the value of x?

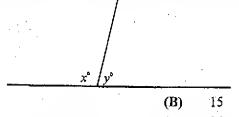
Q4. In the following figure, what is the value of y?



- 45° (A)
- 46° (C)

**(D)** 35°

Q5. In the figure below, if x is 130 more than y, what is the value of y?

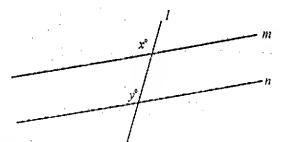


(A) 7

25 (C)

**(D)**. 35

In the following figure,  $m \parallel n$  and l is a transversal, then which of the following statement is (are) Q6. true?



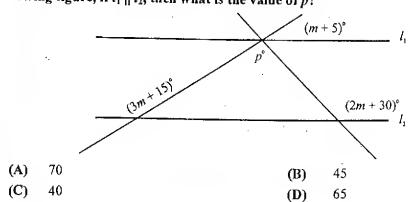
x + y = 180

**(B)** x - y = 180

 $180 < x + y \le 270$ 

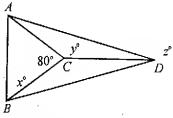
**(D)** Insufficient information

Q7. In the following figure, if  $l_1 \parallel l_2$ , then what is the value of p?



Q8.

**a)** 



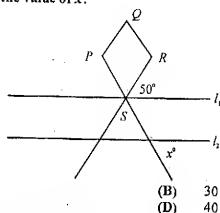
In the above figure, AC = BC = CD and  $m\angle ACB = 80^{\circ}$ . This information is sufficient to determine the value of which of the following?

(A) x only

(C)

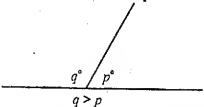
x and y only

- **(B)** y only
- **(D)** y and z only
- Q9. In the following figure, lines  $l_1$  and  $l_2$  are parallel, and line  $l_1$  passes through S, one of the corners of square PQRS. What is the value of x?



- **(A)** 50 .
- (C) 45

- In the following figure, what is the largest value of p?

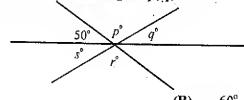


**(A)** 89

**(B)** 90.9

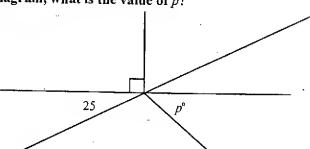
89.9 (C)

- **(D)** 105
- In the following figure, what is the average of p, q, r and s? Q11.



- (A) 70°
- (C)

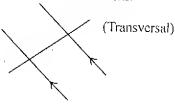
- $60^{\circ}$ **(B)**
- $65^{\circ}$ **(D)**
- In the following diagram, what is the value of p? Q12,





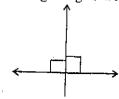
#### Transversal:

A straight line which cuts parallel lines is called a transversal.



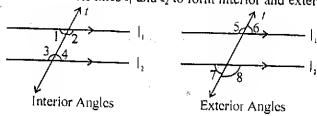
# Perpendicular:

If two lines interest in such a way that they form right angles are called perpendicular



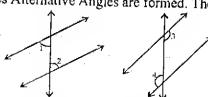
### Interior Angles:

In the figure below, transversal t intersects lines  $\ell_1$  and  $\ell_2$  to form interior and exterior angle.



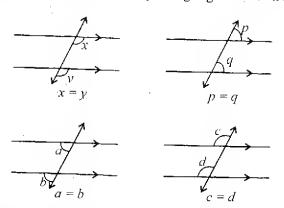
# Alternate Angles:

When a transversal cuts parallel lines Alternative Angles are formed. These alternative angles are equal.



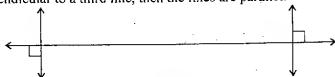
# Corresponding Angles:

Corresponding angles are two angles in corresponding positions relative to the two lines and the transversal. These corresponding angles are also equal. A pair of equal corresponding angles is shown below.



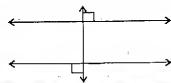


If two lines are both perpendicular to a third line, then the lines are parallel.

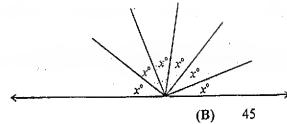


#### Alternatively

If a line is perpendicular to each of a pair of lines, then that pair of lines are parallel.



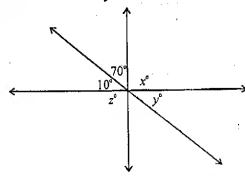
Q1. In the following figure, what is the value of x?



- (A)
- **(C)**

- (D) 35

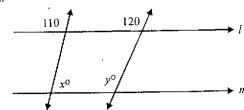
Q2. In the figure below, what is the value of x + y + z?



- 200 (A)
- 210. (C)

- 220 **(B)**
- 190 **(D)**

Q3. In the following figure, if  $l \parallel m$ 



Then  $x^{\circ} + y^{\circ}$ 190°

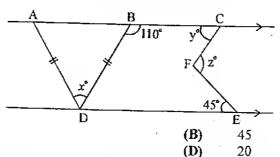
(A)

**(B)** 

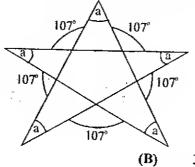
**(D)** 







In the copy of decoration given below, what is the value of angle a? Q25.



**(A)** 73° (C) 107°

**(A)** 

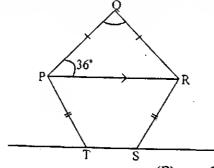
(C)

40

70

34° (D) 45°

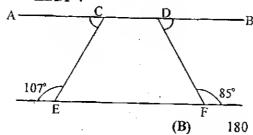
PQRST represents a swimming pool with all its sides of equal length. A rope joins PR and is Q26. parallel to TS. Given that  $\angle QPR = 36^{\circ}$ . What is the value of  $\angle PQR$ ?



(A) 72 (C) 108

(B) 36 (D) 90°

Q27. What is the sum of  $\angle ACE + \angle BDF$ ?

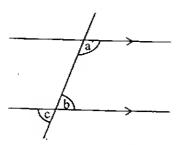


(A) · 192

168

**(D)** 

(C) 85 Q28. In the figure below a + b =



**(A)** a + c

(B)

b + c(C)

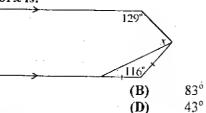
(A)

(C)

(A)

**(C)** 

- **(D)** c - a
- In the figure below, the value of x is: Q29.



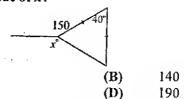
Q30. In the figure below, what is the value of x?

4115°

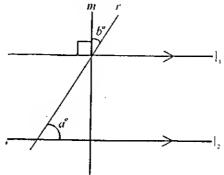
69°

120

110



In the figure below, line  $\ell_1$  is parallel to line  $\ell_2$  and is perpendicular to line m. If a=b, what is the Q31. value of a?

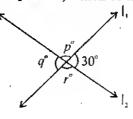


30° (A)

90° (B)

(C) 60°

- (D) 45°
- Q32. For the intersecting two lines  $\ell_1$  and  $\ell_2$  below, which of the following must be true?

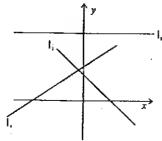


- I.
- II. p = 5q

**(C)** 

- III.  $p + 30^{\circ} = q + r$ Ionly
  - (A)
    - III only

- **(B)** I and II only
- **(D)** II and III only
- Q33. In the figure below, lines  $\ell_1$ ,  $\ell_2$  and  $\ell_3$  have slopes a, b and c, respectively. Which of the following is a correct statement?

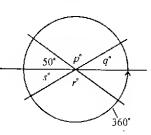


Q11. (D) : vertical angles are equal

$$p + q + r + s + 50 + 50 = 360$$

$$\Rightarrow p + q + r + s = 260$$

Average 
$$\frac{p+q+r+s}{4} = \frac{260}{4} = 65$$

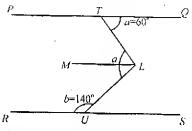


Q12. (E) Since vertical angles are equal, here,

$$a = 25$$
, and so

p+q=155. We see that b=65, and there is no other vertical angle. So it is impossible to determine p and q from the given information.





Through point L, draw ML parallel to RS and PQ.

$$\angle c = \angle MLU + \angle MLT$$

$$\angle MLU = \angle LUS = 180^{\circ} - 140^{\circ} = 40^{\circ}$$

$$\angle$$
MLT =  $\angle$ LTQ = 60°

Then 
$$\angle c = 60^{\circ} + 40^{\circ} = 100^{\circ}$$

Q14. (B) Since 
$$x + 90 + 20 = 180$$
, Therefore

$$x = 70^{\circ}$$

Q15. (C) Since, vertical opposite angles are equal, therefore  $\angle b = 80^{\circ}$ . Again because alternative angles are equal. Therefore,  $\angle a = \angle b$ 

$$\Rightarrow$$
  $\angle a = 80^{\circ}$ 

Q16. (D) 
$$180 - 130 = 50^{\circ}$$

Because vertical opposite angles are equal

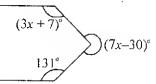
...

$$m = 50$$

and 
$$n = 35^{\circ}$$

$$m + n = 35^{\circ} + 50^{\circ} = 85^{\circ}$$

Q17. (B)



As 
$$131^{\circ} + (3x + 7)^{\circ} = 7x - 30$$

$$131 + 3x + 7 = 7x - 30$$

$$\Rightarrow 7x - 3x = 138 + 30$$

$$4x = 168^{\circ}$$

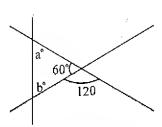
$$x = 42^{\circ}$$

Q18. (A)

From above we see that

$$PQ : AB = 3 : 2$$
  
=  $\frac{3}{2}$  = 1.5

Q19. (D)

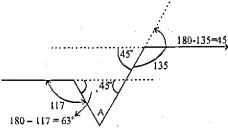


The 120 degrees angle and the angle next to it, is  $60^{\circ}$  because  $180^{\circ} - 120^{\circ} = 60^{\circ}$  (straight angle)

We know sum of all angles of any triangle is 180°

$$a + b + 60^{\circ} = 180^{\circ}$$
  
 $a + b = 120^{\circ}$ 

Q20. (B) The process of finding the value of x is illustrated by the following figure



Because the sum of the angles of a triangle always equal to 180°

$$\therefore x + 45^{\circ} + 63^{\circ} = 180^{\circ}$$

$$\Rightarrow$$
  $x = 72^{\circ}$ 

Q21. (A) Using figure we can see

$$SQ = PQ - (PR + RS)$$

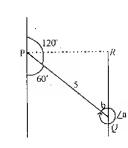
$$SQ = 5x + 9 - (3x + 5 + 2x + 3)$$

$$SQ = 5x + 9 - 5x - 8$$

$$SQ = 1$$

Q22. (D) 
$$\angle b = 180 - 120^{\circ} = 60^{\circ}$$

bearing of P from Q =  $\angle a = 360 - \angle a$ = 360 - 60=  $300^{\circ}$ 

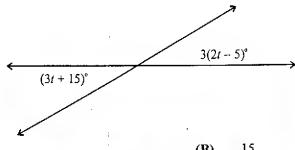


les



- (A) 30°
- 45° (C)

- 40° **(B)**
- 60° (D)
- Q43. In the following figure, what is the value of t?



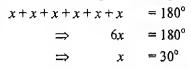
(A) 10

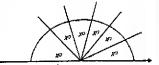
15 **(B)** 

30 (C)

**(D)** 45

Q1. (A) The sum of the given six angles make a straight angle, and the straight angle equal 180°. Thus





Q2. (C) In the given figure, the arc shows a straight angle, hence

$$10 + 70 + x = 180^{\circ}$$

$$x = 100$$

Because opposite angles are equal, thus

$$x = z^{\circ} = 100 \Longrightarrow z = 100$$

Similarly,

$$z + 70 + y = 180^{\circ}$$

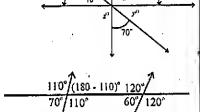
$$100 + 70 + y = 180^{\circ} \quad (\because z = x = 100)$$

$$\Rightarrow$$
  $y = 10$ 

Thus,

Sum of the angles 
$$x + y + z = 100 + 10 + 100$$

$$\Rightarrow x+y+z=210$$



Q3. (A) Because when two straight lines intersect each other, the corresponding angles are equal. This fact is shown in the adjacent figure

$$x^{0} = 70$$

and 
$$y = 120$$

$$x^{0} + y^{0} = 120 + 70 \implies x^{0} + y^{0} = 190$$

Q4. (B) Because vertical angles are equal, therefore

$$x-y = y \implies x=2y$$

$$x = w \text{ also } z = w$$

If we add y, z and w, then the sum of these angles is a straight angle which is equal to  $180^{\circ}$ .

$$y + z + w = 180$$

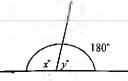
$$y + 2y + 2y = 180$$
 (:  $z = w = x = 2y$ )

$$5y = 180$$

$$y = 36$$

Q5. (C) In the given figure, the sum of the given two angles x and y is a straight angle, and straight angle equals to 180, therefore

$$x + y = 180$$





By given condition

$$x = y + 130$$

$$\Rightarrow x - y = 130 \qquad \dots (ii)$$

Adding (i) and (ii), we have

$$x + y = 180$$

$$x - y = 130$$

$$2x = 310$$

$$x = 155$$

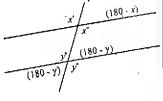
Substituting the value of x, in (i), we have

$$155 + y = 180$$

$$\Rightarrow \qquad y = 180 - 155$$

$$\Rightarrow \qquad y = 25$$

- Q6. (D) Since, there is not enough information, and the figure is not drawn in right scale, thus it is not possible to get the exact value of  $x^{o} + y^{o}$ .
- Q7. (D) Since, when two straight lines intersect, the vertical angles are equal, therefore



 $x^{\circ} = m + 5$ and x + (3m + 15) = 180, but x = m + 5

Hence,

$$(m+5)+(3m+15) = 180 \Rightarrow 4m+20 = 180 \Rightarrow 4m = 160$$
  $(3m+15)$ 

 $\Rightarrow$ 

$$m = 40$$

As,

$$x = m + 5 \Rightarrow x = 40 + 5 \Rightarrow \boxed{x = 45}$$

From figure, x + p = 2m + 30 (: Alternative angles are equal)

$$45 + p = 2(40) + 30$$
  $\Rightarrow 45 + p = 80 + 30 \Rightarrow 45 + p = 110$ 

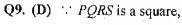
$$\Rightarrow p = 110 - 45 \qquad \Rightarrow \boxed{p = 65}$$

Q8. (A) Since AC = BC, we know that when two sides of a triangle are equal then their opposite angles are also equal. Hence  $\angle A = \angle B$ , and  $\angle A = \angle B = \ddot{x}^{\circ}$ . In any triangle, the sum of the three angles is equal to 180.

$$\angle A + \angle B + \angle C = 180^{\circ} \Rightarrow x^{\circ} + x^{\circ} + 80^{\circ} = 180^{\circ} \Rightarrow 2x = 100$$

$$x = 50$$

 $\therefore$  y and e are not necessarily equal, therefore, we cannot determine y and z. The answer is x only.



$$\therefore$$
  $y = 90$ . Then

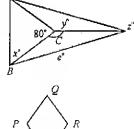
$$x + y + 50 = 180$$

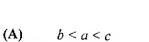
$$x + 90 + 50 = 180$$

(: Alternative angles are equal)

$$x + 140 = 180$$
  $\Rightarrow x = 40$ 

Q10. (C) q > p, then q must be greater than 90 and p less than 90. Therefore, the largest number less than 90 that can fit in the grid is 89.9.

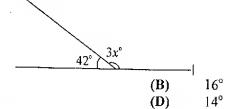




**(B)**  $a \le b \le c$ 

**(C)**  $c \le b \le a$ 

- **(D)**  $c \le a \le b$
- In the figure below, what is the value of x? Q34.

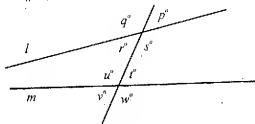


(C) In the following diagram  $I \parallel m$ , Q35.

74°

46°

(A)



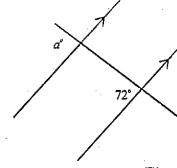
If A represents the average measure of all the eight angles, then A =

(A) 45°

 $180^{\circ}$ 

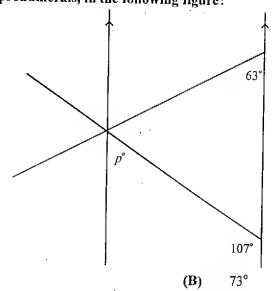
90° (C)

- (D)  $360^{\circ}$
- Q36. In the following figure, what is the value of  $a^{\circ}$ ?



- (A) 108°
- (C) 36°

- 72° **(B)**
- **(D)** 160
- What is the value of pronumerals, in the following figure? Q37.



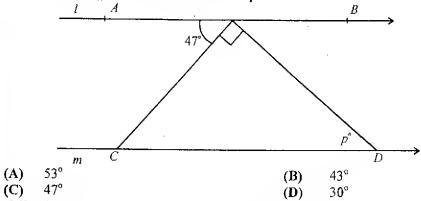
107° (A)

**(B)** 

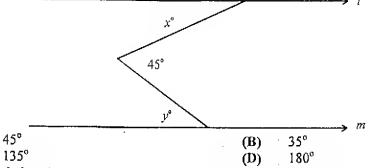
(C)  $170^{\rm o}$ 

- 44°
- (D)

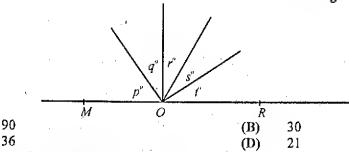
Q38. In the figure below  $l \parallel m$ . What is the value of p?



Q39. In the following figure lines  $l \parallel m$ , then what is the value of x + y?



(A)  $45^{\circ}$  (B)  $35^{\circ}$  (C)  $135^{\circ}$  (D)  $180^{\circ}$  Q40. In the figure below M, O and N are all on line n. What is the average of p, q, r, s and t?

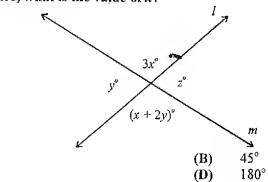


Q41. In the following figure, what is the value of x?

(A)

**(C)** 

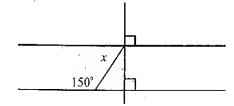
(A) (C)



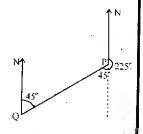
Q42. In the following figure, what is the value of x?

 $90^{\circ}$ 

85°

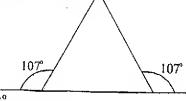


Q23. The north lines are parallel and so  $\angle NQP = 45^{\circ}$ So to retrace their steps, the hill-walker must take a bearing of 45° from Q



Q24. (A) 
$$\angle BAD = \angle ABD$$
  
=  $180^{\circ} - 110^{\circ} = 70^{\circ}$   
 $\angle ADB = 180^{\circ} - 2\angle BAD$   
=  $180^{\circ} - 140^{\circ}$   
=  $40^{\circ}$   
 $\therefore x = 40^{\circ}$ 

Q25. (B) Take one side of the copy of this decoration

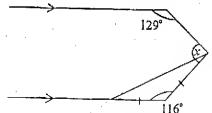


from above  $\angle b = 180 - 107 = 73^{\circ}$ .

In above triangle two angles are 73°, the third angle is

$$\angle a = 180 - 73 - 73$$
  
= 34°

- Q26. (C) Because In  $\triangle PQR$ , the value of  $\angle P$  and  $\angle R$  is 36. Therefore the third angle  $\angle PQR$  must equal to  $108^{\circ}$  (180 – 36 – 36)
- (D) In the given figure  $\angle CDF = 85^{\circ}$  and  $\angle DCE = 107^{\circ}$  because the vertically opposite angles are Q27. equal. Now  $\angle BDF = 95 (180 - 85)$  and  $\angle DCE = 73$ , (180 - 107)Sum of the angles  $\angle BDF + \angle ACE = 168^{\circ}$ .
- (A) b and c are vertical angle and therefore equal angles. a + b = a + cQ28.
- Q29. **(B)**



$$116^{\circ} + y + y = 180^{\circ}$$

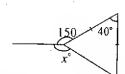
$$\Rightarrow 2y = 180^{\circ} - 116 = 64$$

$$y = 32^{\circ}$$
As  $x+y+116+129 = 360^{\circ}$ 

$$x+32+116+129 = 360^{\circ}$$

$$x+277 = 360^{\circ}$$

$$x = 360^{\circ} - 277 = 83^{\circ}$$



In triangle

$$40^{\circ} + y + y = 180^{\circ}$$

$$2y + 40 = 180^{\circ}$$

$$\Rightarrow 2y = 180 - 40 = 140$$

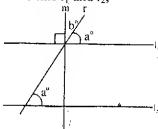
$$y = 70^{\circ}$$

$$70^{\circ} + 150 + x = 360^{\circ}$$

$$x + 220 = 360^{\circ}$$

$$\Rightarrow x = 360^{\circ} - 220 = 140^{\circ}$$

Q31. (D) Since line m is perpendicular to line  $l_1$  and  $l_2$ ,



$$a^{\circ} + b^{\circ} = 90^{\circ}$$
  
 $a^{\circ} + a^{\circ} = 90^{\circ}$   
 $2a^{\circ} = 90 \Rightarrow a^{\circ} = 45$ 

Q32. (D) Since vertically opposite angles are equal. Therefore,  $\angle q = \angle 30^{\circ}$  and sum of the straight angles is  $180^{\circ}$ . Thus

$$a^{\circ} + 30 = 180 \Rightarrow a = 150$$
  
 $\Rightarrow a = 5(q) \text{ and } p + 30^{\circ} = q + r$ 

Q33. (A)

Q34. (A) 
$$42 + 3x = 180^{\circ} \Rightarrow 3x = 138$$

$$\Rightarrow x = 46^{\circ}$$

Q35. (C) Sum of the angles p + q + r + s = 360Similarly t + u + v + w = 360

Sum of the measure of above 8 angles = 360 + 360 = 720

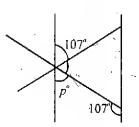
Average = 
$$\frac{720}{8}$$
 = 90°

Q36. (B) Since corresponding angles of parallel lines are equal, therefore,

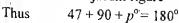
$$a = 72$$

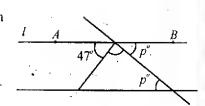
Q37. (B)  $p^{\circ} = 73$ 

$$107^{\circ} + p^{\circ} = 180^{\circ}$$
  
 $p^{\circ} = 180^{\circ} - 107^{\circ} = 73$ 



Q38. (B) The angles in the given figure, is decomposed as shown in the adjacent figure





$$137 + p^{\circ} = 180^{\circ}$$

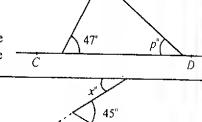
$$p^{\circ} = 180 - 137$$

$$p^{\circ} = 43$$

Second Method: Because in any triangle, the sum of the three angles is equal to  $180^{\circ}$ , thus  $47^{\circ} + 90^{\circ} + p^{\circ} = 180$ 

$$\Rightarrow p^{\circ} = 43$$

Q39. (A) Extend the line which makes angle  $x^{\circ}$  with the upper line towards the down-ward line. Sine l and m are parallel, the measure in the bottom line in the triangle equals. In any triangle



180 - 45

$$x + y + (180 - 45) = 180^{\circ}$$

$$x + y + 135 = 180^{\circ}$$

$$x + y = 180 - 135$$

$$x + y = 45$$

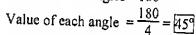
Q40. (C) In the figure, the angle MOR is straight angle. Thus, sum of the angles p, q, r, s and t is 180 and their average is

Q41. (B) Because, when the straight lines intersect each their then vertical angles are equal. Thus, in the given figure

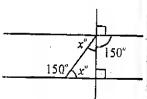
Similarly 
$$y^{\circ} = z^{\circ}$$
  
 $3x^{\circ} = (x + 2y)^{\circ}$   
 $\Rightarrow 3x - x = 2y \Rightarrow 2x = 2y \Rightarrow x = y$   
 $x = y = z \Rightarrow x = z$ 

Hence the four angles, are equal.

As the sum of angles= 180°



Q42. (A) Sinee a line is perpendicular to each pair of lines, thus the pair of lines are parallel, and when a line intersect pair of lines corresponding angles are equal.



First Method: Calculation of upper line

$$x + 150 = 180$$

$$x = 30$$

Second Method: Calculation of lower line

$$150 + x^{\circ} = 180^{\circ}$$

$$x = 30$$

Third Method: Calculation of triangle

Sum of the three angles in a triangle equals 180°

$$x^{0} + 90 + (150 - 90) = 180^{0}$$

$$x^{0} + 90 + 60 = 180^{0}$$

$$x^{0} + 150 = 180^{0}$$

$$\Rightarrow \qquad \boxed{x = 30^{0}}$$

Q43. (A) When two lines intersect each other corresponding angles are equal, thus

$$3t + 15 = 3(2t - 5)$$

$$3t + 15 = 6t - 15$$

$$30 = 3t$$

$$t = 10$$



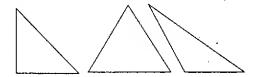
## Chapter 2

#### TRIANGLES

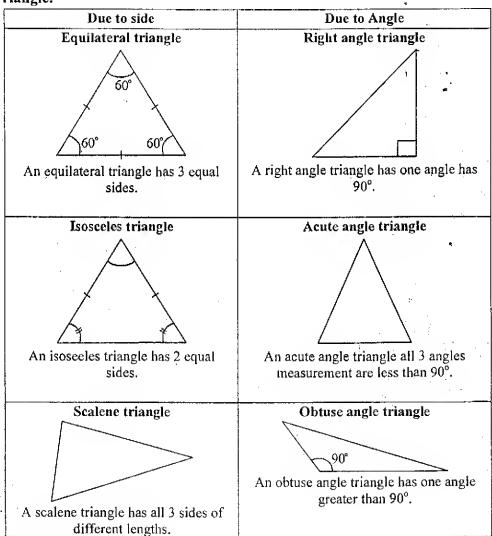
#### Triangle:

A three-sided polygon is called a triangle.

Examples:

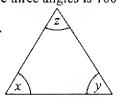


#### Types of Triangle:



#### Angle's Sum of Triangle:

In any triangle, the sum of the measures of the three angles is 180°.



E IJ

E.

So Sir

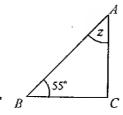
Ex

Th

$$x + y + z = 180^{\circ}$$

Example 1:

In the figure below, what is the value of z?



Solution:

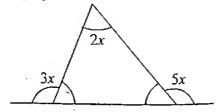
Because, the angle of a triangle add up to 180°. Therefore

$$55^{\circ} + 90^{\circ} + Z = 180^{\circ}$$
  
 $Z = 180^{\circ} - 145^{\circ}$   
 $Z = 35^{\circ}$ 

Example 2:

 $\Rightarrow$ 

Calculate the value of x in the following figure:



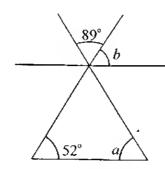
Solution:

Because the sum of the straight angles is 180°, therefore the missing angles of the triangle are  $(180^{\circ} - 3x)$ ,  $(180^{\circ} - 5x)$  and 2x $(180^{\circ} - 5x)$  and 2x.

$$(180^{\circ} - 5x) + (180^{\circ} - 3x) + 2x = 180^{\circ}$$
$$360^{\circ} - 6x = 180^{\circ}$$
$$-6x = 180^{\circ} - 360^{\circ}$$
$$-6x = -180^{\circ}$$
$$x = 30^{\circ}$$

Example 3:

Calculate the value of



Solution:

We know when two lines intersect each other then opposite angles are equal, therefore, the third angle of the triangle will be 80°. Hence triangle will be 89°. Hence

$$\angle 52^{\circ} + \angle a + \angle 89^{\circ} = 180^{\circ}$$

$$\angle a = 180^{\circ} - (52^{\circ} + 89^{\circ})$$

$$\boxed{\angle a = 39^{\circ}}$$

Now, because corresponding angles are equal, here ∠52 and ∠b are pair of corresponding angles. Therefore

$$\angle b = \angle 52^{\circ}$$

$$\angle b = 52^{\circ}$$

## Properties of Isoseeles Triangle:

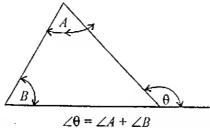
- 1. If two sides of a triangle are congruent, then the angles opposite to these sides are congruent.
- 2. If the three angles of a triangle are congruent, then the three sides are also congruent.
- 3. If two angles of a triangle are congruent, then the sides opposite these angles are also congruent.
- 4. If three sides of a triangle are congruent, then the three angles are also congruent.

# Angle Properties of Triangle:

- 1. In every triangle the greatest angle is opposite to the longest side.
- 2. In every triangle the sum of the lengths of any two sides is always greater than the length of the third side.
- 3. In every triangle the shortest side is opposite to the smallest angle.
- 4. When the side of a triangle is produced the exterior angle so formed which is equal to the sum of the opposite interior angles.

#### Example:

In the figure below

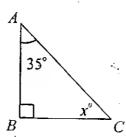


5. In any right triangle, the sum of the measures of the two acute angles is 90%

### Example:

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the



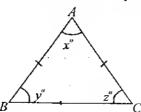
Find the value of x.

#### Solution:

Since, the sum of the measures of the two acute angles is 90°, therefore

$$x + 35^{\circ} = 90^{\circ}$$
  
 $x = 90^{\circ} - 35^{\circ} = 55^{\circ}$ 

.6. An equilateral triangle has three equal sides, and three equal angles of 60°.



#### Example:

The above triangle is an equilateral triangle. Therefore,

$$x^0 = v = z = 60^\circ$$

### Right Triangle:

#### 1. Pythagoras' Theorem:

It states that, in any right-angled triangle, the square on the hypotenuse is equal to the sum of the squares of the other two sides.

Using the letters in the diagram, the theorem is written as

$$c^2 = a^2 + b^2$$

. This relation may be written as

$$a^2 = c^2 - b^2$$
 or  $b^2 = c^2 - a^2$ 

#### 2. Pythagorean Triples:

Pythagorean triples are sets of numbers that satisfy Pythagorean theorem.

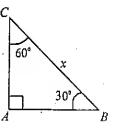
Let x be any positive number, then there is a right triangle whose sides are 3x, 4x and 5x.

It mean, any multiples of this set such as 6x, 8x, 10x or 9x, 12x, 15x form a Pythagorean triple. The most common Pythagorean triples are:

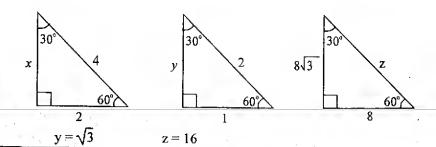
# 3. The 30°-60°-90° Triangle:

Let x be the hypotenuse of triangle ABC. Then

- 1) The leg opposite the 30° angle is  $\frac{1}{2}(x)$ .
- 2) The leg opposite the 60° angle is  $\frac{1}{2}(x)(\sqrt{3})$ .



# Examples:



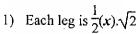
 $x = 2\sqrt{3}$ 

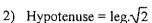
In an equilateral triangle, an altitude forms a 30°-60°-90° triangle and is equal to

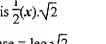
$$\frac{1}{2}$$
 (hyp). $\sqrt{3}$ 

# 4. The 45°-45°-90° Triangle:

Let x be the hypotenuse of an isosceles right triangle, then

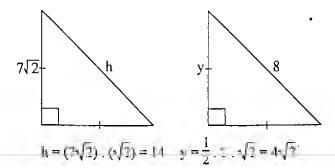








#### Examples:

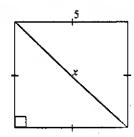


#### Note:

In a square, the diagonal forms a 45°-45°-90° triangle. Thus, in a square

Diagonal = side.
$$\sqrt{2}$$

#### Example:



In a square, diagonal = (Side). $\sqrt{2}$ 

$$x = 5.\sqrt{2}$$

$$x = 5\sqrt{2}$$

#### Example:

What is the area of the square whose diagonal is 12?

#### Solution:

Let S be the side of the square, then

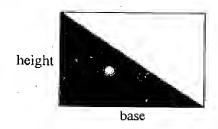
Diagonal = (Side).
$$\sqrt{2}$$
  
12 = S.  $\sqrt{2}$   
S =  $\frac{12}{\sqrt{2}}$ 

⇒'

Area of square 
$$= S^2 = \left(\frac{12}{\sqrt{2}}\right)^2 = \frac{144}{2} = 72$$

# Area of Triangle:

To calculate the area of a triangle, first look at the following rectangle

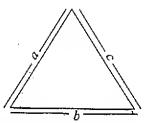


Area of rectangle = base  $\times$  height

Area of triangle  $=\frac{1}{2} \times \text{base} \times \text{height}$ 

# Perimeter of a triangle:

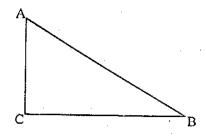
Perimeter of a triangle = sum of lengths of sides



Perimeter of a triangle = a + b + c

# Triangle Inequality:

In  $\triangle ABC$ , given below



$$\angle C > \angle A > \angle B$$

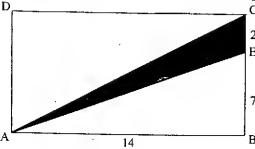
These inequalities suggest the following theorems.

- 1. The perpendicular segment from a point to a line is the shortest distance from the point to the line.
- 2. Triangle Inequality Theorem:

The sum of the lengths of two sides of a triangle is greater than the length of the third side.

#### Example;

What is the area and perimeter of the triangle AEC, where ABCD is a rectangular?





#### Solution:

The area of Rectangle ABCD is

$$= 9 \times 14 = 126$$

Now area of triangle ABE

$$=\frac{1}{2}(14)(7)=49$$

and area of triangle ADC

$$=\frac{1}{2}(9)(14)=63$$

Total area of the triangles ABE and ADC

$$=49+63=112$$

Area of  $\triangle AEC = (Area of the rectangle) - (Sun of the area of the triangle)$ 

$$= 126 - 112$$

$$= 14$$

Perimeter of AAEC

In triangle ABE

$$(AE)^2 = (14)^2 + (7)^2$$

$$= 196 + 49 = 245 \implies AE = 7\sqrt{5} = 16$$

In triangle ADC

$$(AC)^2 = (AD)^2 + (BC)^2$$

$$= (9)^2 + (14)^2 = 81 + 196 = 277 \implies AC = 17$$

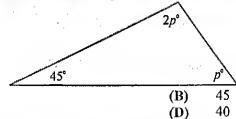
Perimeter of AAEC

$$= AE + EC + CA$$

$$= 16 + 17 + 2 = 35$$

# Multiple Choice Questions (MCQs)

Q1. In the following triangle, what is the value of p?



Q2. The area of an equilateral triangle whose altitude is 10, is:

(A)

(C)

(A)  $8\sqrt{3}$ 

**(B)**  $2\sqrt{3}$ 

(C)  $96\sqrt{3}$ 

35

55

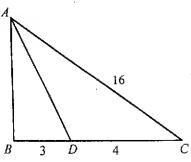
- **(D)**  $4\sqrt{3}$
- Q3. The two sides of a right triangle are 3 and 5. Then the length of the third side is:
  - (A)  $\sqrt{34}$

(B)  $\sqrt{22}$ 

(C)  $2\sqrt{3}$ 

**(D)**  $3\sqrt{2}$ 

Q4. In the following triangle, AD =



**(A)**  $3\sqrt{2}$ 

**(B)**  $6\sqrt{6}$ 

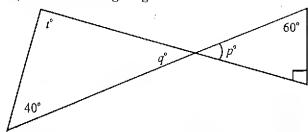
Q5.



- $6\sqrt{3}$ (C)
- In the following figure, t =

- $3\sqrt{7}$ (D)
- 40 40° 40
- (A) 110
- (C) 70

- (B) 115
- **(D)** 140
- Q6. What is the value of t, in the following diagram?

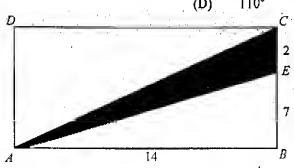


100° (A)

(B)  $60^{\circ}$ 

30° (C)

110° (D)



- Fig. 1
- What is the area of the triangle AEC, in the above figure 1? Q7.
  - (A) 12

49 **(B)** 

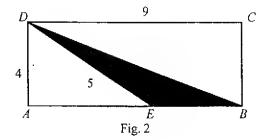
(C) 14

- (D) 21
- Q8. What is the perimeter of  $\triangle CEA$ , in the figure 1?
  - 16 (A)

**(B)** 25

(C) 17

 $2 + 7\sqrt{5} + \sqrt{277}$ (D)



Q9. In figure 2, what is the area of  $\triangle BED$ ?

- (A) 16
- **(C)** 12

**(B)** 14

6

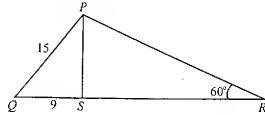
- (D)
- Q10. In figure 2, what is the perimeter of  $\triangle BED$ ?
  - $3 + \sqrt{93}$ (A)

**(B)** 11

(C)  $11 + \sqrt{97}$ 

**(D)** 81

Questions 11-12 refer to the following figure:



- Q11. What is the area of  $\Delta PQR$ ?
  - (A)  $3 + 4\sqrt{3}$

 $18(3 + 4\sqrt{3})$ **(B)** 

**(C)** 54

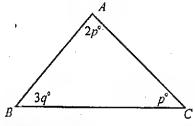
84√3 **(D)** 

- Q12. What is the perimeter of  $\Delta PQR$ ?
  - **(A)** 54

**(B)** 72

(C)  $4 + \sqrt{3}$ 

- $12(4+\sqrt{3})$ **(D)**
- In the following figure, which of the following expresses a true relationship between p and q? Q13.



**(A)** p = 180 + q

**(B)** q = 30 + p

(C) p = 90 + q

(D) p = 60 - q

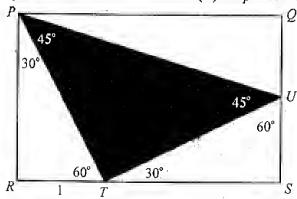


Fig. 3

Questions 14-15 refer to the above figure 3:

- What is the perimeter of shaded triangle PTU?
  - (A)  $2(2+\sqrt{2})$

**(B)**  $4 + \sqrt{2}$ 

 $2 + \sqrt{2}$ (C)

- **(D)**
- What is the area of the shaded triangle?

- (A) 2
- (C)  $2\sqrt{2}$

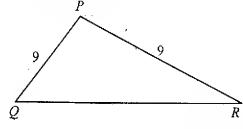
- **(B)** 4
- **(D)**  $4\sqrt{2}$
- Q16. If the length of the two sides of a triangle are 4 and 6, then the length of the third side is:
  - (A) less than 11

- (B) greater than 11
- (C) less than or equal to 11
- (D) None of these
- Q17. What is the ratio of the diagonal to a side of a square?
  - (A) 1:1

**(B)**  $\sqrt{2}:\sqrt{3}$ 

(C)  $\sqrt{2}:1$ 

- **(D)**  $\sqrt{2}:\sqrt{2}$
- Q18. In the following figure, the perimeter of  $\Delta PQR$  is:



(A) less than 18

(B) greater than 18

(C) equal to 18

(D) None of these

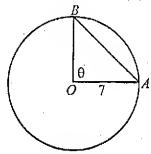


Fig. 4

- Q19. In figure 4, if  $\theta > 90$ , then the length of AB is:
  - (A) less than 14

(B) greater than 14

(C) equal to 14

- (D) not possible
- Q20. In figure 4, if  $\theta = 90$ , then the perimeter of  $\triangle AOB$  is:
  - (A)  $7 + \sqrt{7}$

**(B)**  $14 + \sqrt{2}$ 

(C)  $14 + \sqrt{7}$ 

**(D)**  $7(2+\sqrt{2})$ 

8

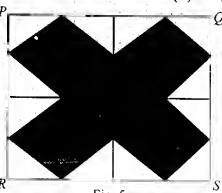


Fig. 5

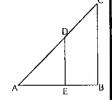
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Q21.	In figure 5, the perimeter of shaded region is:			
	(A) 17	<b>(B)</b>	24	
	(C) 34	(D)	21	
Q22.	In figure 5, what is the area of the shaded region?	(D)	21	
	(A) 40	(12)	24 .	•
	(C) 20	(B)	24	
	^	<b>(D)</b>	12	
	$\sqrt{z^{\circ}}$			•
022				
Q23.	\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \		•	
	$\frac{135^{\circ}}{x^{\circ}}$ $y^{\circ}$ $110^{\circ}$			
	7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7			
	Refer to the above figure, which of the following st			
	(A)  x+y>z	<b>(B)</b>	x + y < z	
024	(C)  x + y = z	(D)	x + y = x - z	
Q24.	In the following figure:			
	60° 45°	$\lambda$		·.
	p / You 43	$\triangle_{\mathbb{Z}}$		
	which of the following statement is true?	C		
	(A) $AB > BC$	(D)	$AD \geq DC$	
	(C) $AB = BC$	(B)	AB < BC	
Q25.		(D)	AC > BC	
₹-•,	In a right triangle, if the difference between the mean what is the measure (in degrees) of the smallest ang	ieasur	e of the two smaller	r angles is 30°, the
	(A) 35		1.5	·
	(C) 60	(B)	45	
Q26.	7 7	(D)	30	
Q=0.	In an isoseeles triangle that is not equilateral, if all than 25, then what is the largest perimeter?	ofits	sides are integers a	nd no side is longe
	(1) 71	-		
	4.00	(B)	75	•
727		(D)	72	
Q27.	What is the smallest integer, s, for which, s, $s + 3$ , at triangle?	nd 2 <i>s</i> <sup>–</sup>	15 can be the leng	ths of the sides of a
	criangic;			
	(m) (n)	(B)	<b>1</b> 1	
	(C) 10	(D)	8 ,	
<b>228.</b>	If the perimeter of the triangle is $45 + 15\sqrt{3}$ , and if	the m	easure of the angles	of the triangle are
	in the ratio of 1:2:3, then what is the length of the	small	est side?	
	$(\mathbf{A}) = 10$	(B)	15	•
	(C) $3 + \sqrt{3}$	(D)	$2 + \sqrt{2}$	
<b>)29.</b>	Consider the aecompanying diagram. Which of the	follow	ing statements is tr	167
	(A) $PQ < QR$	P	ing statements is tr	10,
	$(\mathbf{B}) \qquad P\widetilde{R} < \widetilde{P}Q$			
	(C) $PQ > QR$			
	$(\mathbf{D}) \qquad PQ + QR < PR \qquad .$		65'	
		Q		
<b>)30.</b>	Regarding the adjacent triangle, which of the follow	ing sta	atements is true?	A
	(A) AD > AO	(B)	AB > BC	
		( <b>D</b> )	AC > BC	
	··· · · · · · · · · · · · · · · · · ·	w)	AC / DC	

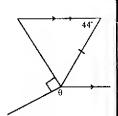
In diagram, DE is parallel to CB, AE = BE, DE = 4, and EB = 3. What is CB?

Q31.

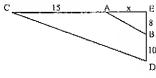
- (A)
- **(B)** 8
- (C) (D) 6
- 12



- Q32. The value of  $\theta$  is:
  - 134° (A)
  - 148 **(B)**
  - (C) 112
  - 206 (D)



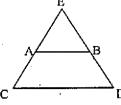
In  $\triangle ECD$ ,  $\overline{AB} \parallel \overline{CD}$ . What is the value of x? Q33.



- (A) (C) 15
- 12

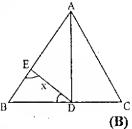
- **(B)**
- (D)

In  $\triangle CDE$ ,  $\overline{AB} \parallel \overline{CD}$ , then  $\frac{EA}{AC} =$ Q34.



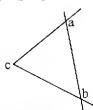
- $\frac{\mathrm{BD}}{\mathrm{AC}}$ (A)
- EB BD (C)

- EC AC **(B)**
- $\frac{AB}{CD}$ **(D)**
- In figure given below, If  $\overrightarrow{AB} = \overrightarrow{AC}$ ,  $\overrightarrow{AE} = \overrightarrow{AD}$  and Q35.  $\angle DAC = 20^{\circ}$ . What is the value of x?



- 45° (A)
- (C) 40°

- $10^{\circ}$
- 35° **(D)**
- Q36. In figure below. What is the size of a + b - c



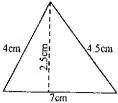
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(A)	120°

**(B)** 175°

**(D)** 180°

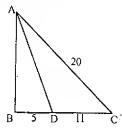
Q37. What is the area of the triangle?



(A) 8.75cm<sup>2</sup> (C) 17.5cm<sup>2</sup>

(B) (D) 15.5cm<sup>2</sup> 3.5cm<sup>2</sup>

Q38. What is the value of AD in the following triangle?



(A) 11

**(B)** 12

(C)  $5\sqrt{2}$ 

**(D)** 13

Q39. If a triangle of base 4 has the same area as a circle of radius 4, what is the altitude of the triangle?

(A)  $4\pi$ 

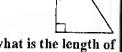
(B)  $8\pi$ 

(C)  $2\pi$ 

(D)  $10\pi$ 

Q40. The area of the right triangle given below is  $18 \text{cm}^2$ . The ratio of its legs is 2:3. What is the length of the hypotenuse?

- (A)  $\sqrt{39}$ cm<sup>2</sup>
- (B)  $3\sqrt{13} \text{em}^2$
- (C)  $2\sqrt{18}$ em<sup>2</sup>
- (D)  $6\sqrt{13} \text{em}^2$



Q41. In a triangle, the ratio of the legs is 1:2. If the area of the triangle is 32cm<sup>2</sup>, what is the length of the hypotenuse?

(A)  $4\sqrt{5}$ 

**(B)**  $2\sqrt{3}$ 

(C)  $3\sqrt{2}$ 

(D)  $5\sqrt{6}$ 

Q42. The angles of a triangle are in the ratio 1:2:3. The largest angle in the triangle is:

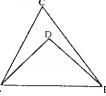
(A)  $160^{\circ}$ 

**(B)**  $75^{\circ}$ 

(C) 40°

(D) 90°

Q43. In triangle ABC below, angle BAC is greater than angle CBA. The bisector of angle A and angle B meet at point D, which of the following statement is (are) true?



$$(A) \qquad BD = AD$$

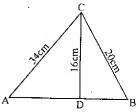
(B)

BD > AD BD < AD

(C) 
$$BD \le AD$$

**(D)** 

What is the length of AB in the figure below? Q44.



- (A) 30cm
- (C) 24cm

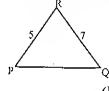
- **(B)** 
  - 12cm
- **(D)**
- Two angles of a triangle are  $(2a 40)^{\circ}$  and  $(3a + 10)^{\circ}$ . The third angle is: Q45.
  - (A)  $(230 + a)^{\circ}$

**(B)**  $(180 + a)^{\circ}$ 

42cm

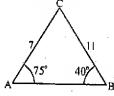
(C)  $(210 - 5a)^{\circ}$ 

- **(D)**  $(220 - 5a)^{\circ}$
- If the perimeter of  $\Delta PQR$  below is 3 times the length of QR, then PQ = Q46.



- (A)
- (C)

- **(B)**
- **(D)** 5
- Which of the following statements concerning the length of side AB is true? Q47.



AC < 7 (A)

**(B)** AB < 7

(C) 7 < AB < 11

- **(D)** AB > 11
- The three angles of a triangle are  $(2a + 20)^{\circ}$ ,  $(3a + 20)^{\circ}$  and  $(a + 20)^{\circ}$ . The value of a is Q48.
  - (A) 10

**(B)** 80

**(C)** 20

- (D) 30
- What is the area of an equilateral triangle PQR whose altitude is 6? Q49.
  - $2\sqrt{3}$ (A)

**(B)** 

(C)

(D)  $12\sqrt{3}$ 

Q

Q

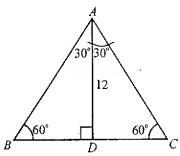
Q1. (B) In any triangle, the sum of the angles =  $180^{\circ}$ 

$$45 + p + 2p = 180^{\circ} \Rightarrow 3p = 180 - 45$$

$$\Rightarrow p = \frac{135}{3} = 45$$

Q2. (C) To find the area, first of all we draw a equilateral triangle ABC, in which AD is altitude.





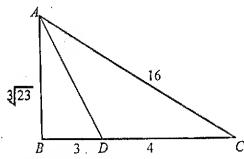
By, 30 - 60 Right Triangle Theorem,

$$BD = \frac{12}{\sqrt{3}} = \frac{4 \times \sqrt{3} \times \sqrt{3}}{\sqrt{3}} = 4\sqrt{3}$$

Now, Base= 
$$4\sqrt{3} + 4\sqrt{3} = 8\sqrt{3}$$
 and altitude = 12

Thus, Area= Base × Altitude  
= 
$$8\sqrt{3} \times 12 = 96\sqrt{3}$$

- Q3. If the triangle is not right, then any number greater than 1 and less than 25 could be the length of the third side. Now, if the triangle is right, then there are only two possibilities:
  - (i) If 5 is the hypotenuse, then the legs are 4 and 3.
  - (ii) If 3 and 5 are two legs then hypotenuse is  $\sqrt{34}$ .
- Q4, (B)



In  $\triangle ABC$ , AC = 16, BC = 3 + 4 = 7, using

Pythagorean theorem, 
$$AC^2 = (AB)^2 + BC^2 \Rightarrow 16^2 = AB^2 + 7^2$$

$$\Rightarrow 256 = AB^2 + 49 \Rightarrow AB^2 = 256 - 49 = 207 \Rightarrow AB = \sqrt{207}$$

$$\Rightarrow AB = 3\sqrt{23}$$
.

Now, in 
$$\triangle ABD$$
,  $AD^2 = AB^2 + BD^2 \Rightarrow AD^2 = (3\sqrt{23})^2 + (3)^2$ 

$$\Rightarrow AD^2 = 9(23) + 9 \Rightarrow AD^2 = 207 + 9 \Rightarrow AD^2 = 216$$

$$\Rightarrow AD = 6\sqrt{6}$$

**Q5.** (A) Here, 
$$\angle A + \angle B + \angle C = 180 \Rightarrow a + b + 40 = 180 \Rightarrow a + b = 140$$

Because the given triangle is an isosceles, i.e., a = b

Therefore, a and b are each 70, and

$$x = 180 - 70 = 110^{\circ}$$

**Q6.** E Here 
$$90^{\circ} + 60^{\circ} + p^{\circ} = 180$$
  $\Rightarrow p^{\circ} = 30 \Rightarrow q^{\circ} = 30^{\circ}$ 

Now
$$q + t + 40 = 180$$
  $\Rightarrow q + t = 140 \Rightarrow t = 140 - q$ 

$$\Rightarrow t = 140 - 30$$
  $\Rightarrow t = 110^{\circ}$ 

Q7. (C) Area of the rectangle 
$$ABCD = 14 \times 9 = 126$$

To find the area of the shaded region, we subtract the two white areas of the right angled triangles ABE and ADC

Area of 
$$\triangle ABE = \frac{1}{2}(14)(7) = 49$$

Area of 
$$\triangle ADC = \frac{1}{2}(9)(14) = 63$$

Sum of the white areas = 49 + 63 = 112

Area of the shaded region = 126 - 112 = 14 square unit

Q8. (D) To calculate the value of AE in  $\triangle ABE$ , we use Pythagorean theorem,

$$(AE)^2 = (AB)^2 + BE^2$$

$$\Rightarrow AE^2 = (14)^2 + (7)^2 \Rightarrow AE^2 = 196 + 49$$

$$\Rightarrow AE^2 = 245 \qquad \Rightarrow AE = \sqrt{245} = 7\sqrt{5}$$

Now, in  $\triangle ADC$ , we calculate AC

$$AC^2 = AD^2 + DC^2 \implies AC^2 = 9^2 + 14^2$$

$$\Rightarrow AC^2 = 81 + 196 \qquad \Rightarrow AC^2 = 277 \Rightarrow AC = \sqrt{277}$$

Perimeter of  $\triangle AEC = 2 + 7\sqrt{5} + \sqrt{277}$ 

Q9. (C) Area of the rectangle  $ABCD = 4 \times 9 = 36$ 

Now, in  $\triangle DAE$ ,

$$DE^2 = (4)^2 + AE^2 \Rightarrow (5)^2 = 4^2 + (AE)^2 \Rightarrow AE^2 = 25 - 16$$

$$\Rightarrow AE^2 = 9 \Rightarrow AE = 3$$

Thus, 
$$EB = AB - AE \Rightarrow ED = 9 - 3 = 6 (AB = DC = 9)$$

Now Area of 
$$\triangle DAE = \frac{1}{2}(3)(4) = 6$$

and Area of the 
$$\triangle BCD = \frac{1}{2}(9)(4) = 18$$

Now Area of the shaded region

= Area of the rectangle 
$$ABCD$$
 – (Area of  $\triangle AED$  + Area of  $\triangle BCD$ )

$$= 36 - (18 + 6) = 36 - 24 = 12$$
 Square units

Q10. (C) In 
$$\triangle DEB$$
,  $DE = 5$ ,  $EB = 6$  (from above  $Q$ ),  $DB = ?$ 

Now we find the value of DB

In  $\triangle BDC$ .

$$(BD)^2 = (BC)^2 + (DC)^2 \Rightarrow BD^2 = 16 + 81$$

$$\Rightarrow BD^2 = 97 \Rightarrow BD = \sqrt{97}$$

Now the perimeter of the  $\triangle DEB$ 

$$=DE + EB + BD = 5 + 6 + \sqrt{97} = 11 + \sqrt{97}$$

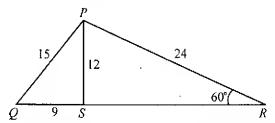
Q11. (B)  $\Delta PQS$  is a right triangle, whose hypotenuse is 15 and its one leg is 9, using Pythagorean theorem

$$PQ^2 = QS^2 + PS^2$$

$$\Rightarrow (15)^2 = (9)^2 + PS^2 \Rightarrow = 225 - 81 = PS^2$$

$$\Rightarrow PS^2 = 144 \Rightarrow PS = 12$$





Now  $\triangle PRS$  is a 30 - 60 - 90 right triangle, its shorter leg is 12. Then according to 30 - 60 Right Triangle Theorem hypotenuse PR will be 24 and leg RS will be  $12\sqrt{3}$ . So the area of the triangle PQR is

Area=
$$\frac{1}{2}$$
(Base) Altitude  
= $\frac{1}{2}$ (9 + 12 $\sqrt{3}$ )(12)  
= 18(3 + 4 $\sqrt{3}$ )

Q12. (D) The perimeter of the triangle PQR is the sum of its sides

So perimeter of 
$$\triangle PQR = PQ + QR + PR$$
  
=  $15 + (9 + 12\sqrt{3}) + 24$   
=  $48 + 12\sqrt{3}$   
=  $12(4 + \sqrt{3})$ 

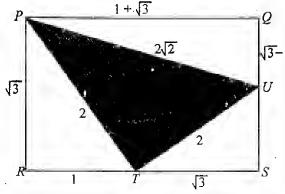
Q13. (D) In any triangle, sum of its interior angles is 180°. So

$$p + 2p + 3q = 180^{\circ}$$

$$\Rightarrow 3p + 3q = 180 \Rightarrow 3(p + q) = 180$$

$$\Rightarrow p + q = 60 \Rightarrow p = 60 - q$$

Q14. (A) Triangles PRT and PQU both are 30 - 60 - 90 triangles. Thus both triangles will have sides 1,  $\sqrt{3}$  and 2, and the inner triangle PTU is a 45 - 45 - 90 triangle and has sides 2, 2 and  $\sqrt{2}$ , as shown in the following figure



Also, 
$$PQ = RS = 1 + \sqrt{3}$$
 and  $PR - US = QU = \sqrt{3} - 1$ 

Thus the perimeter of the shaded triangle is

$$2 + 2 + 2\sqrt{2} = 4 + 2\sqrt{2} = 2(2 + \sqrt{2})$$

Q15. (A) The area of  $\triangle PTU = \frac{1}{2} (Base) (Altitude)$ 

$$=\frac{1}{2}(2)(2)$$

**O3** 

= 2

Q16. (A) The sum of the two sides of a triangle always greater than the third side. Hence the third side is less than

$$4 + 6 = 10 < 11$$

Q17. (C) First we draw the diagram, the diagonal of a square is the hypotenuse of each of the 45 - 90 - 45 triangle. Using

$$(AC)^2 = (AB)^2 + (BC)^2$$

$$AC^2 = \sqrt{x^2 + x^2} = \sqrt{2x^2} = x\sqrt{2}$$

Now 
$$x\sqrt{2}: x = \sqrt{2}: 1$$

Q18. (B) In the given triangle,  $QR < PQ + PR \implies QR < 9 + 9$ 

$$\Rightarrow QR < 18$$

Therefore, the perimeter can be any number greater than 18.

Q19. (A) Since in the given figure OA and OB are radii, each is equal to 7. Thus AB could be any positive number less than 14.

Q20. (D) 
$$(AB)^2 = (OA)^2 + (OB)^2$$
  
=  $(7)^2 + (7)^2$   
 $(AB)^2 = 49 + 49$ 

$$AB = \sqrt{98} \Rightarrow AB = 7\sqrt{2}$$

Now perimeter of AOB = AO + OB + AB

$$= 7 + 7 + 7\sqrt{2}$$
$$= 14 + 7\sqrt{2}$$

$$= 7(2 + \sqrt{2})$$

Q21. (B) In the given figure, the perimeter of the shaded region consists of 12 line segments, these line segments are the hypotenuse of a 45 - 45 - 90 white triangle whose legs are 2. Then each line segment is,  $\sqrt{(2)^2 + (2)^2} = \sqrt{4 + 4} = \sqrt{8} = 2\sqrt{2}$ , and the perimeter of the shaded region is  $24\sqrt{2} = 24$  approx.

Q22. (A) The white region consists of 12 right triangles, each of which has area of  $\frac{1}{2}$  of the small square. Now

the area of the small square is  $2 \times 2 = 4$ . The area of  $\frac{1}{2}$  small square  $= \frac{1}{2} \times 4 = 2$ , the total area of the white half small squares is  $= 12 \times 2 = 24$ . Since the area of the large square is  $8 \times 8 = 64$ . Thus the area of shaded region is 64 - 24 = 40.

Q23. (A) Here, 
$$x = 180 - 135 = 45$$
, and  $y = 180 - 110 = 70$ , then  $x + y = 45 + 70 = 115$ 

Now, 
$$x + y + z = 180 \Rightarrow 45 + 70 + z = 180 \Rightarrow z = 65$$

Thus 
$$115 > 65 \Rightarrow x + y > z$$

Q24. (B) Since  $60 + 45 = 105 \Rightarrow \text{m} \angle A = 75$ , this shows that  $\angle A$  is the largest angle and BC is the side opposite to the largest angle. Thus BC is the largest side.

Q25. (D) First of all we draw the diagram

By the given condition

$$x - y = 30$$
 ...(i)

Because, 
$$\angle A + \angle B + \angle C = 180$$

$$90 + y + x = 180$$

$$x + y = 90$$
 ...(ii)

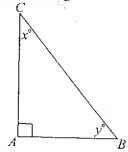
Adding (i) and (ii), we have

$$x - y = 30$$

$$x + y = 90$$

$$2x = 120$$
  $\Rightarrow x = 60^{\circ}$ 

Put 
$$x = 60$$
 in (ii), we get



$$60 + y = 90 \implies y = 30^{\circ}$$

Q26. Since no side of the triangle can be longer than 25, thus, we suppose that both of the equal sides are 25. Then the largest possible value of the third side is 24. Its perimeter is

$$25 + 25 + 24 = 74$$

Q27. (C) In a triangle the sum of the sides of any sides must be greater than the third side. S + (S + 3) to be greater than

2S-15, thus 2S+3 must be greater than 2S-15; but that is always true. For S+(2S-15) to be greater than

 $S+3 \Rightarrow 3S-15$  must be greater than S+3;

but 3S - 15 > S + 3 is true only if

$$3S - S > 3 + 15$$

$$2S > 18 \Rightarrow S > 9$$

Thus answer is 10.

Q28. (B) Since, angles are in ratio 1:2:3, thus

$$\theta + 2\theta + 3\theta = 180 \Rightarrow 6\theta = 180 \Rightarrow \theta = 30$$

Here,  $\theta = 30$ ,  $2\theta = 60$  and  $3\theta = 90$ , so the given triangle is a 30 - 60 - 90 triangle, thus its sides are x, 2x and  $x\sqrt{3}$ . Thus its perimeter is  $3x + x\sqrt{3}$ 

but given that perimeter is  $45 + 15\sqrt{3}$ ,

$$\Rightarrow 3x + x\sqrt{3} = 45 + 15\sqrt{3}$$

$$x(3+\sqrt{3}) = 15(3+\sqrt{3})$$

$$\Rightarrow$$
  $x = 15$ 

- Q29. (C) Since the measure of angle R is 65°, the measure of angle P is 25°. Since the larger side is opposite the larger angle, therefore, PQ > QR
- Q30. (C) Since the larger side is always opposite to the larger angle. In the fig, angle A is 90° the larger side of the triangle is BC, followed by AC and then at last AB.
- Q31. (B) Since DE is parallel CD, the triangle ADE and ACB are similar. Therefore, corresponding sides are proportional. So DE is to AB as AB to CB. Since AE = EB,  $\frac{AB}{AE}$  is  $\frac{1}{2}$ . Therefore CB is twice or 8.
- Q32. (A)

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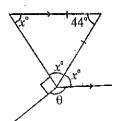
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Since the triangle is isosceles triangle than

$$x^{0} + x^{0} + 44^{0} = 180^{0}$$

$$\Rightarrow$$
  $2x^{\circ} = 180^{\circ} - 44^{\circ} = 136^{\circ}$ 

and

$$2x + \theta + 90^{\circ} = 360^{\circ}$$

$$136 + \theta + 90^{\circ} = 360^{\circ}$$

$$\theta + 226 = 360^{\circ}$$

$$\Rightarrow$$
 .0 = 360° - 226 = 134°

therefore  $\theta = 134$ 

Q33. (C) Since, If a line interesting the interior of a triangle is parallel to one side, then the line divides the other two sides proportionally.

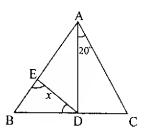
$$\frac{x}{15} = \frac{8}{10}$$

$$10x = 120$$

x = 12

Q34. (C) Since the line AB is parallel to line CD, therefore the line AD divides CE and ED proportionally.

$$\frac{EA}{AC} = \frac{EB}{BD}$$



As 
$$AB = AC$$

So, 
$$m\angle ACB = m\angle ABC =$$

ln ΔABC

$$m\angle ACB + m\angle BCA + m\angle CAB = 180^{\circ}$$

$$y + y + 40 = 180^{\circ}$$

$$\Rightarrow 2y = 180^{\circ} - 40^{\circ} = 140$$

$$y = 70^{\circ}$$

In AADE

$$AD = AE$$

So, 
$$m\angle AED + m\angle ADE = z^{\circ}$$

$$m\angle AED + m\angle ADE + m\angle DAE = 180^{\circ}$$

$$z + z + 20^{\circ} = 180^{\circ}$$

$$\Rightarrow$$
 2z = 180° - 20° = 160°

$$\Rightarrow$$
  $z = 80^{\circ} = m \angle AED$ 

$$m\angle AED + m\angle DEB = 180^{\circ}$$

$$80^{\circ} + \text{m} \angle \text{DEB} = 180^{\circ}$$

$$\Rightarrow$$
 m $\angle$ DEB =  $180^{\circ} - 80^{\circ} = 100^{\circ}$ 

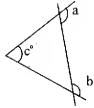
In ABED

$$m\angle BED + m\angle EDB + m\angle DBE = 180^{\circ}$$

$$100 + x + 70^{\circ} = 180^{\circ}$$

$$\Rightarrow x + 170^{\circ} = 180^{\circ}$$

$$x = 180^{\circ} + 170^{\circ} = 10^{\circ}$$



$$(180^{\circ} - a) + (180^{\circ} - b) + c = 180^{\circ}$$

$$180^{\circ} - a + 180^{\circ} - b + c = 180^{\circ}$$

$$360^{\circ} - (a + b - c) = 180^{\circ}$$

$$a + b - c = 360^{\circ} - 180^{\circ}$$

$$\Rightarrow$$
 a + b - c = 180°

Q37. (A) Area of the triangle 
$$=\frac{1}{2}$$
 Base × Altitude

N

Q3{

Q39.

Q40.

Q41.

Q42.

Q43.

Q44.

$$= \frac{1}{2} \times 7 \times 2.5$$
$$= 8.75 \text{ cm}^2$$

Q38. (D) Using the Pythagorean theorem in AABC

$$(per)^2$$
 =  $(hyp)^2 - (base)^2$   
 $AB^2$  =  $(20)^2 - (11 + 5)^2$   
 $AB^2$  =  $400 - 256 = 144$   
 $AB$  = 12

Again using the Pythagorcan theorem in AABD

$$(hyp)^2 = (base)^2 + (per)^2$$

$$AD^2 = (12)^2 + (5)^2$$

$$= 144 + 25 = 169 \Rightarrow AD = 13$$

Q39. (B) Area of the circle  $= \pi r^2$ =  $\pi (4)^2 = 16\pi$ 

Area of the triangle= $\frac{1}{2} \times 4 \times Altitude$ 

= 2 × Altitude

Since area of the given triangle is equal to the area of the circle of radius 4, therefore

$$16\pi = 2 \times \text{Altitude}$$
Altitude =  $8\pi$ 

Q40. (D) Let legs be 2x and 3x, by Pythagorean theorem

But 
$$(hyp)^2 = (2x)^2 + (3x)^2$$

$$\frac{1}{2} \cdot 2x \cdot 3x = 18$$

$$3x = 18 \Rightarrow x = 6$$

$$(hyp)^2 = (12)^2 + (18)^2$$

$$= 144 + 324 = 468$$

$$hyp = \sqrt{468} = 6\sqrt{13}$$

Q41. Let legs of the triangle be x and 2x, then

hyp<sup>2</sup> = 
$$(x)^2 + (2x)^2$$
  
But 32 =  $\frac{1}{2} \cdot x \cdot 2x$   
 $\Rightarrow$   $x^2 = 16 \Rightarrow x = 4$   
hyp<sup>2</sup> =  $(4)^2 + (8)^2 = 16 + 64 = 80$   
 $\Rightarrow$  hyp =  $\sqrt{80} = \boxed{4\sqrt{5}}$ 

Q42. (D) The sum of the angles in a triangle =  $180^{\circ}$ 

Given ratio 1:2:3Sum of the ratios = 1+2+3=6

Largest angle =  $\frac{3}{6} \times 180 = 90^{\circ}$ 

Q43. If  $\angle CAB > \angle ABC$ , then  $\angle A > \frac{1}{2} \angle B$ . Then  $\angle DAB$  greater than  $\angle DBA$ . Therefore DB > DA (opposite sides of the angle)

Q44. **(D)** Solving  $\triangle$ CAD  $(AD)^2 = (34)^2 - (16)^2$ = 1156 - 256 = 900

Now solving ΔCBD

$$(BD)^{2} = (20)^{2} - (16)^{2}$$

$$= 400 - 256$$

$$(BD)^{2} = 144$$

$$BD = 12$$

$$AB = AD + BD$$

$$AB = \overline{AD} + BD$$
$$= 30 + 12 = \boxed{42}$$

Q45. (C) Let the angles of triangle be

$$(2a-40)^{\circ}$$
,  $(3a+10)^{\circ}$ , x then  
 $(2a-40)^{\circ} + (3a+10^{\circ}) + x = 180^{\circ}$ .  
 $\Rightarrow x = 180^{\circ} - [(2a-40) + (3a+10)]$   
 $= 180^{\circ} - [5a-30^{\circ}]$   
 $= 180^{\circ} - 5a + 30^{\circ}$ 

x = (210 - 5a)

Q46. (B) The perimeter of the triangle is the sum of the lengths of the 3 sides. Since the perimeter is equal to 3 times the length of QR  $(3 \times 7 = 21)$ 

$$5 + 7 + PQ = 21$$
  
 $PQ = 21 - 12$   
 $PQ = 9$ 

Q47. (C)  $\angle C + 75^{\circ} + 40^{\circ} = 180 \Rightarrow \angle C = 65$ . Here  $\angle A$  is the largest angle, B is the smallest and C is in between. Therefore

Q48. (C) 
$$(2a + 20) + (3a + 20) + (a + 20)$$
 = 180  
 $6a = 180 - 60$   
 $6a = 120$   
 $\Rightarrow a = 20$ 

Q49. (D)

As PQR is equilateral triangle

$$\therefore \overline{PQ} = \overline{QR} = RP = 2x$$

In APTR

$$(hyp)^{2} = (base)^{2} + (prep)^{2}$$

$$(2x)^{2} = (x)^{2} + (6)^{2}$$

$$4x^{2} = x^{2} + 36$$

$$4x^{2} - x^{2} = 36$$

$$3x^{2} = 36$$

$$x^{2} = 12$$

$$x = 2\sqrt{3}$$

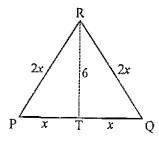
So

$$PQ = 2x = 2(2\sqrt{3})$$
$$= 4\sqrt{3}$$

Area of PQR =  $\frac{1}{2}$  × base × Altitude

$$=\frac{1}{2}\times 4\sqrt{3}\times 6$$

Area of PQR =  $12\sqrt{3}$ 





### Chapter 3

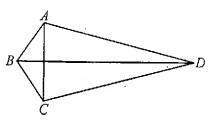
### **QUADRILATERALS AND POLYGONS**

#### Quadrilateral:

A quadrilateral is a plane figure with four straight sides. The elements of a quadrilateral are its four sides and four angles.

### Diagonal of Quadrilateral:

A diagonal of a quadrilateral is a line segment joining two non-consecutive vertices. In the following figure, the diagonals of the quadrilateral ABCD are AC and BD.



### Family or Types of Quadrilateral:

The properties of a quadrilateral are the features that are characteristic of that shape. They can include any of the following:

Sides:

a

in

Are the side lengths equal? Are the sides parallel?

Angles:

Are any angles equal? Are any angles right angles?

Diagonals:

Are the diagonals equal? Do the diagonals bisect each other? Do the diagonals bisects the

angles through which they pass? Do the diagonals cut at right angles?

The combination of properties is different for each quadrilateral.

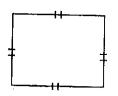
Quadrilateral	Properties
Trapezium	A quadrilateral with one pair of opposite sides parallel.
Kite	A quadrilateral with two pairs of equal adjacent sides.
Parallelogram	❖ A quadrilateral with opposite sides
	parallel.
Rectangle	❖ All properties of parallelogram plus.
	(i) All angles are right angles. Diagonals are equal.
	(ii) Two axes of symmetry (perpendicular to sides)

Rhombus



- All properties of parallelogram plus.
- (i) All sides are equal.
- (ii) Diagonals bisect at right angles.
- (iii) Diagonals bisect the angles through which they pass.
- (iv) Two axes of symmetry.
- All properties of rectangle plus.
- All sides are equal
- Four axes of symmetry.

Square

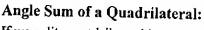


### Convex Quadrilateral:

A quadrilateral is called convex if each of its interior angles is less than two right angles.

### Re-entrant Quadrilateral:

A quadrilateral is called re-entrant if one of its interior angles is reflex. A kite with one reflex interior angle is an example of a re-entrant quadrilateral.



If we split a quadrilateral into two triangles as shown, then we can ealculate the angle sum.

Angle sum = a + b + c + d + e + f

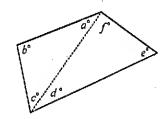


$$a+b+c=180$$

$$d+e+f=180$$

So 
$$a + b + c + d + e + f = 180 + 180$$

$$= 360^{\circ}$$



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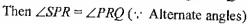
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### Additional Properties of Parallelograms:

We have learnt that, in a parallelogram, it has two pairs of parallel sides. Opposite sides are equal. Opposites angles are equal. Diagonals bisect each other. Now, we shall derive some

of the properties of parallelogram using the properties of parallel lines and angles. Consider a parallelogram PQRS with diagonal  $\overline{PR}$ .



$$\angle QPR = \angle PRQ \ (\because Alternate angles, PS \parallel QR)$$

$$\therefore \angle SPR + \angle QPR = \angle PRQ + \angle PRS$$

$$\angle QPS = \angle QRS$$

Now, in  $\Delta PQR$ 

$$\angle PQR + \angle QPR + \angle PRQ = 180^{\circ}$$

$$\angle PQR = 180 - (\angle QPR + \angle PRQ)$$

$$= 180 - (\angle PRS + \angle SPR) = \angle PSR$$

$$\angle QPR = QRS \text{ and } PQR = PSR$$
 .....(i)

Hence, from (i), we can say that in a parallelogram "opposite angles are congruent."

Now, also in parallelogram PQRS,

$$\angle QPS + \angle PQR + \angle QRS + \angle RSP = 360^{\circ}$$

But 
$$\angle QPS = \angle QRS$$
 and  $\angle PQR = \angle RSP$ 

$$\therefore 2(\angle QPS + \angle PQR) = 360^{\circ}$$

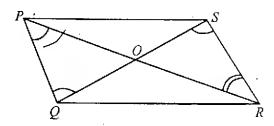
$$\angle QPS + \angle PQR = 180^{\circ}$$

Similarly, 
$$\angle QRS + \angle RSP = 180^{\circ}$$

Thus, from (ii), we can say, that, in a parallelogram,

"Pairs of adjacent angles are supplementary."

Now in triangle PQR and RSP,



$$\angle PRQ = \angle SPR$$

$$\angle QPR = \angle PRS$$

$$\Rightarrow$$
  $PR = PR$  (common)

$$\therefore \Delta PQR = \Delta RSP \quad (\because \text{Two angles and a side are congruence})$$

$$\Rightarrow$$
  $PQ = RS$  and  $PS = QR$  .....(iii)

Hence, in a parallelogram,

"Opposite sides are congruent."

In triangles PQO and RSO

$$PQ = RS$$

$$\angle PQO = \angle RSO$$

$$\angle OPO = \angle SRO$$

$$\therefore \Delta PQO \cong \Delta RSO$$
 (by AAS congruence)

$$\Rightarrow$$
 PO = RO and QO = SO .....(iv)

Hence, in a parallelogram

:S

"Two diagonals bisect each other."

Now in triangles PQR and RSP

$$QR = PS$$

$$PO = RS$$

$$PR = PR$$
 (common)

Similarly 
$$\triangle PQS \cong \triangle RSQ$$

Hence, in a parallelogram

"A diagonal divides into two congruent triangles."

#### Test for Quadrilaterals:

We have seen, that each of the quadrilaterals has several properties, but it is not necessary to check all the properties when trying to identify a shape.

### Tests for a Parallelogram:

To identify the shape as a parallelogram, satisfying any of these conditions is sufficient.

Both pairs of opposite sides are parallel or equal.

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So

- 2. Both pairs of opposite angles are equal.
- 3. One pair of opposite sides is equal and parallel.
- 4. Diagonals bisect each other.

#### Tests for a Rhombus:

To identify the shape as a rhombus, satisfying any of these conditions is sufficient.

- 1. All sides are equal.
- 2. Diagonals bisect at right angles.

### Common Properties in all Quadrilaterals:

The common properties in all quadrilaterals are:

- 1. Diagonals bisect each other.
- 2. Opposite angles are equal.

#### Polygons:

A simple closed figure formed by three or more line segments is known as a polygons. Polygons are named by the number of sides they have. The following is a list of the names given to polygons according to the number of their sides.

Number of sides	Name of the polygon
3	Triangle
4	Quadrilateral
5	Pentagon
6	Hexagon
7	Heptagon
8 .	Oetagon
9	Nanagon
10	Decagon

#### Vertex of a Polygon:

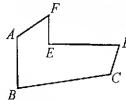
The angular points of a polygon are called its vertices, and the number of sides of a polygon is equal to the number of its vertices.

### Other Names of Polygons:

Other words used to describe polygons are:

#### Concave:

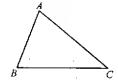
A polygon is said to be coneave when one or more of its interior angles is greater than two right angles.

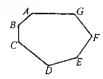


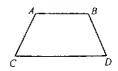
The above figure shows a concave polygon: the measure of interior angle DEF is greater than 180°.

#### Convex Polygon:

A polygon is said to be convex when all its interior angles are less than two right angles. The following figures are examples of convex polygon.





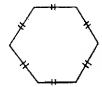


### Regular Polygon:

A polygon is said to be regular if all its sides as well as its angles are equal. The following figures are some examples of regular polygons:







### Angle Sum of a Polygon:

The angle sum of a polygon with n sides is equal to

$$(n-2)\times 180^{\circ}$$

The size of each interior angle of a regular polygon with n sides is

$$\frac{(n-2)\times 180^{\circ}}{n}$$

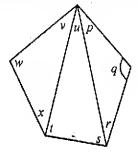
or S = (2n - 4) right angles.

In words

The sum of the angles in a polygon is equal to 'the number of sides less 2' multiplied by 180°.

#### Example 1:

What is the sum of the angles in a pentagon?



Solution:

$$S = p + q + r + s + t + u + v + w + x$$

$$S = (n-2) 180^{\circ}$$

$$S = (5 - 2) 180^{\circ}$$

$$S = 540^{\circ}$$

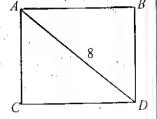
#### Example 2:

What is the length of each side of a square if its diagonals is 8?

#### Solution:

In the adjacent diagram, diagonal AD is the hypotenuse of a  $45 \div 45 - 90$  right triangle.

Then = 
$$\frac{AC}{\sqrt{2}} = \frac{8}{\sqrt{2}} = \frac{8\sqrt{2}}{2} = 4\sqrt{2}$$



Example 3: A decagon is drawn in which each angle has the same measure. What is the measure of each angle?

Solution: The sum of the measures of n sided is

$$(n-2) 180^{\circ}$$

Here n = 10

Sum of the angles of a decagon = (10-2) 180

. .

to the

d by mber

g figures

$$= 8(180)$$
  
= 1440

Angles are equal measure, so each angle is

$$= 1440 \div 10 = 144$$

#### Perimeter:

The distance all around a shape is called its perimeter. Or

The perimeter of a figure is the measure of its bounding line-segments or curves.

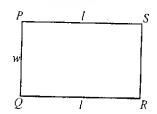
### Perimeter of a Quadrilateral:

For a quadrilateral PQRS

$$=PQ+QR+RS+SP$$

$$=2(PQ+QR)$$

$$=2(l+w)$$



### Perimeter of a Rectangle:

Similarly, the perimeter of rectangle = 2(l + w), where l and w are the length and the width, respectively.

## Perimeter of a Square and Rhombus:

Since, in a square and rhombus all sides are equal, so the perimeter of a rhombus or a square =41Where I is the length of each side.

#### Area:

The area of a shape is the amount of flat space taken up by the shape.

## Area of the Rectangle and Square:

Area of a reetangle = length × width

$$= I \times w$$

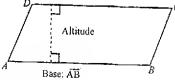
For a square

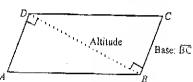
length = width i.e., w = l

Area of square=  $l \times l = l^2$ 

# Area of Parallelograms and Triangles:

Any side of a parallelogram may be called the base of the parallelogram. For each base, there is a corresponding altitude.





An altitude of a parallelogram is a perpendicular segment whose end points lie on opposite sides of a parallelogram.

In a parallelogram ABCD, let

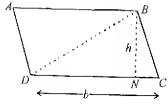
$$DC = b(base)$$
 and

distance between the parallel lines

AB and DC be h. Then

area of parallelogram = base × altitude

$$= b \times h = bh$$



### Area of Triangle:

Since a diagonal of a parallelogram divides it into two congruent triangles, also the area of the triangles are

equal, therefore

Area of 
$$BDC = Area of ABD$$

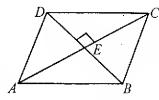
Area of 
$$BDC = \frac{1}{2}$$
 [Area of parallelogram  $ABCD$ ]

$$=\frac{1}{2}b\times c$$

## Area of Trapezium and Rhombuses:

In a rhombus, all sides are congruent and the diagonals are perpendicular to each other.

The area A of a rhombus is one-half the product of the lengths of its diagonals,  $d_1$  and  $d_2$ , that is



II

$$A = \frac{1}{2} d_1 d_2$$

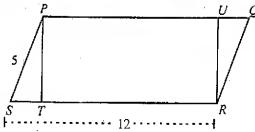
The formula for the area of a trapezium can be found by finding the areas of the triangles formed by drawing a diagonal.

Area of ABCD = Area of Triangle I + Area of Triangle II

Thus, the area A of a trapezium is one-half the product of its altitude and the sum of its bases, b and b'. That is Area of Trapezium ABCD =  $\frac{1}{2}bh + \frac{1}{2}b'h = \frac{1}{2}h(b+b')$ 



In the following figure, the area of parallelogram PQRS is 36. What is the area of rectangle Q1. PURT?



(A) 60

40 (B)

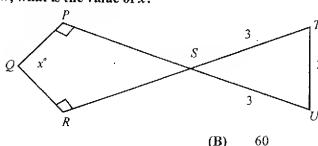
- (D) 36
- Q2. The length of a rectangle is twice its width. If the perimeter of a rectangle is the same as the perimeter of a square of size 9, what is the length of a diagonal of the rectangle?
  - 180 (A)

 $3\sqrt{5}$ **(B)** 

(C) 36

 $6\sqrt{5}$ (D)

Q3. In the figure below, what is the value of x?



(A) 120

**(B)** 

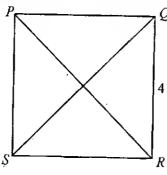
(C) 90

- **(D)** 30
- Q4. A triangle has sides, 5 inches, 12 inches and 13 inches, respectively. A rectangle equal in area to that of the triangle has a width of 4 inches. The perimeter of the rectangle, expressed in inches, is:
  - (A) 23

(B) 28

(C) 60

- **(D)** 32
- Q5. In the following figure, square PQRS has divided into four triangles by drawing diagonals PR and QS. What is the sum of the perimeters of triangles?



(A)  $2 + \sqrt{2}$ 

(B)  $4 + \sqrt{2}$ 

(C)  $4(1+\sqrt{2})$ 

- **(D)**  $16(1+\sqrt{2})$
- Q6. If the length of a rectangle is 4 times its width, and if its area is 196, what is its perimeter?
  - (A) 60

(B) 28

(C) 35

- **(D)** 70
- Q7. If the angles of a hexagon are in the ratio 2: 4:4:4:5:5, what is the degree measure of the smallest angle?
  - (A) 30

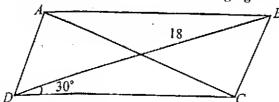
**(B)** 60

**(C)** 40

**(D)** 70

0

Questions 4-5 refer to the following figure



- Q8. What is the area of the rectangle ABCD?
  - (A)  $3\sqrt{3}$

(B) 36√3

(C) 81

- (D)  $81\sqrt{3}$
- Q9. What is the perimeter of the rectangle ABCD?
  - (A)  $81 + 81\sqrt{3}$

**(B)**  $18 + 18\sqrt{3}$ 

(C)  $12(1+2\sqrt{3})$ 

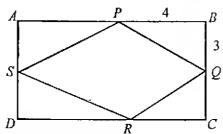
- **(D)**  $12 + 12\sqrt{3}$
- Q10. The length of a rectangle is 3 more than the side of a square, and the width of the rectangle is 3 less than the side of the square. If the area of the square is 58, what is the area of the rectangle?
  - (A) 40

(B) 20

(C) 39

**(D)** 49

Question 11-12 refer to the following figure, in which P, Q, R and S are midpoints of the sides of rectangle ABCD.



- Q11. What is the perimeter of quadrilateral PQRS?
  - (A)

40 (B)

(C) 60

- **(D)** 30
- Q12. What is the area of the quadrilateral PQRS?
  - (A)

**(B)** 24

**(C)** 40

96 **(D)** 

Question 13-14 refer to the following figure, in which P and Q are midpoints of two of the sides of square EFGH.



- Q13. What is the perimeter of the shaded region?
  - (A)  $2 + 3\sqrt{2}$

(B)

 $4 + 6\sqrt{2}$ 

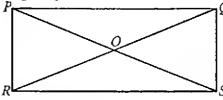
- $3 + 2\sqrt{2}$ **(D)**
- Q14. What is the area of the shaded region?
  - (A)

10

(B) 4.5

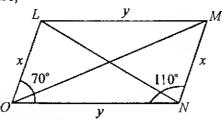
(C) 6

- **(D)**
- Q15. Refer to the following rectangle PQRS,



which of the following statements is true?

- Area of  $\triangle POR >$  Area of  $\triangle ORS$ (A)
- **(B)** Area of  $\triangle POR = \text{Area of } \triangle ORS$
- (C) Area of  $\triangle ORS >$  Area of  $\triangle POR$
- (D)  $\Delta POR \cong \Delta ORS$
- Refer to the following figure, Q16.



which of the following statements is true?

- Diagonal LN < Diagonal MO (A)
- **(B)** Diagonal LN < Diagonal MO



- **(C)** Diagonal MO = Diagonal LN
- (D) LA || MO
- Q17. What is the perimeter of a 30-60 right triangle whose longer leg is 2s?
  - $4S(2+2\sqrt{3})$ (A)

**(B)**  $S(4 + 2\sqrt{3})$ 

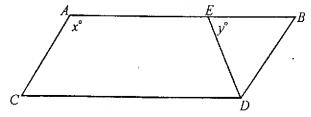
(C)  $S(2+2\sqrt{3})$ 

- **(D)**  $4S + 2S\sqrt{2}$
- Q18. If the area of a rectangle is 40, then its perimeter will:
  - (A) equal to 24

less than 24 **(B)** 

**(C)** greater than 24 **(D)** less than or equal to 22

Q19. In the following figure,

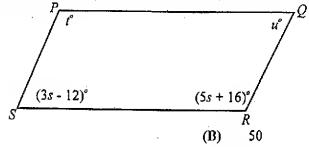


x =

(A)  $\boldsymbol{Y}$  **(B)** 

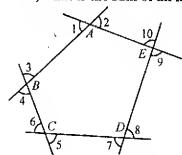
**(C)** 

- **(D)** 2y
- Q20, In the following parallelogram PQRS, what is the value of t - u?



- (A) 72
- 91 (C)

- 22 **(D)**
- Q21. In the following pentagon ABCDE, what is the sum of all marked exterior angles?

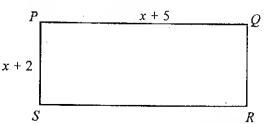


720 (A)

540 **(B)** 

360 **(C)** 

- **(D)** 300
- Q22. Following, two rectangles are given, the area of the rectangle PQRS is 90, what is the area of the rectangle UVWX?

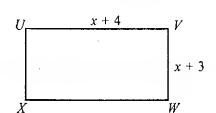


Q1

Q2

O3

Q4



(A) 90

**(B)** 

(C) 68

(D) 92

60

# Explanatory Answers

Q1. (C) Area of the parallelogram: A = bh, in the given figure,

$$A = 36$$
 and  $b = 12$ , therefore

$$36 = 12h \Rightarrow h = 3$$

Now, in 
$$\triangle PTS$$
,  $(SP)^2 = (PT)^2 + (ST)^2$ 

$$\Rightarrow$$
 25 = 9 + ST<sup>2</sup>

$$\Rightarrow$$
 16 =  $ST^2 \Rightarrow ST = 4$ 

Now 
$$TR = SR - ST \Rightarrow TR = 12 - 4 = 8$$

Now, Area of rectangle =  $A = I_W$ 

Hence, Area of rectangle  $PURT = 8 \times 3 = 24$ 



Since, Perimeter of square 
$$= 4(9)$$

$$= 36$$

Therefore, Perimeter of rectangle = 2(l + w)

$$\Rightarrow 2(l+w) = 36 \Rightarrow l+w = 18$$

But 
$$l = 2w$$
 (Given)

Putting the value of l in (i), we have

$$2w + w = 18 \implies 3w = 18$$

$$\Rightarrow w = 6$$

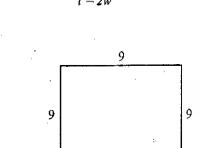
Also, since l = 2w, therefore

$$l = 2(6) = 12$$

the

Using Pythagorean theorem, to find the length of diagonal BC

$$(BC)^2 = (BD)^2 + (CD)^2$$
,  $\Rightarrow d^2 = (6)^2 + (12)^2$   
 $\Rightarrow d^2 = 36 + 144$   
 $\Rightarrow d = \sqrt{180} = 6\sqrt{5}$ 



l = 2w

Q3. Since,  $\triangle STU$  is equilateral, therefore, all of its angles measure  $60^{\circ}$ . Now, at S the two angles are vertical, and since vertical angles are equal, therefore, the measure of  $\angle S$  in quadrilateral PQRS is  $60^{\circ}$ .

Now, sum of the angles of PORS =  $360^{\circ}$ 

$$90^{\circ} + x^{\circ} + 90^{\circ} + 60^{\circ} = 360^{\circ}$$

$$\Rightarrow x^{\circ} + 240^{\circ} = 360^{\circ}$$

$$\Rightarrow \qquad \qquad x = 360 - 240$$

$$x = 120$$

Q4. The sides of the triangle are 5, 12 and 13 therefore, the given triangle is a right triangle.

Let h = 5 and b = 12, then its area

$$A = \frac{1}{2}bh \implies A = \frac{1}{2}(12)(5)$$
$$\implies A = 30$$

Now area of the rectangle is

Area = 
$$w \times h$$

Area = 
$$4 \times h$$

Since the area of the rectangle equals to area of the triangle, therefore

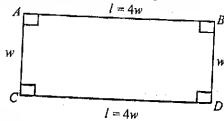
$$30 = 4 \times h \Rightarrow h = \frac{30}{4} \Rightarrow h = 7.5 \text{ cm}$$

The perimeter of the rectangle = 
$$2(w + h)$$

Q5. (D) Each of the four triangle is a right triangle having hypotenuse 4. Therefore, each leg = 
$$\frac{4}{\sqrt{2}} = \frac{2 \times \sqrt{2} \times \sqrt{2}}{\sqrt{2}} = 2\sqrt{2}$$

The perimeter of each small triangle is  $4 + 4\sqrt{2} = 4(1 + \sqrt{2})$  and the sum of the perimeter =  $4(4(1 + \sqrt{2}) = 16(1 + \sqrt{2})$ 

Q6. (D) According to the given condition, we draw a rectangle as shown in the figure



NowArea = 
$$A = Iw = 4w \times w = 4w^2$$

and 
$$196 = 4w^2 \Rightarrow w^2 = 49 \Rightarrow w = 7$$

Now 
$$w = 7 \Rightarrow l = 7 \times 4 = 28$$
, so its perimeter

Perimeter = 
$$2(7 + 28) = 2(35) = 70$$

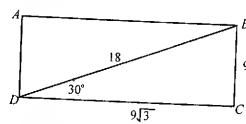
Q7. (B) The sum of the degree measures of the angles of a hexagon (six-sided polygon) is  $(6-2) \times 180^{\circ} = 4 \times 180 = 720$ 

Now, sum of the ratio = 
$$2 + 4 + 4 + 4 + 5 + 5 = 24$$

$$\frac{2}{24} \times 720 = 2 \times 30 = 60$$

Q8. (D) In the diagram, first we solve  $\triangle BCD$ 

$$\frac{BC}{DB} = \sin 30^{\circ} \Rightarrow \frac{BC}{18} = \frac{1}{2} \Rightarrow BC = 9$$



and 
$$\frac{DC}{BD} = \cos 30^{\circ} \Rightarrow DC = BD \cos 30^{\circ} \Rightarrow DC = 18 \times \frac{\sqrt{3}}{2}$$

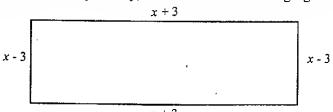
Area =  $l \times w = 9 \times 9\sqrt{3} = 81\sqrt{3}$ 

Q9. (B) The perimeter of the rectangle =2(l+w)

$$=2(9+9\sqrt{3})$$

$$= 18 + 18\sqrt{3}$$

Q10.(D) Let x be the length of the square, then according to the given condition, the length and width of the rectangle is x + 3 and x - 3, respectively, as shown in the following figure



Then, area of the rectangle A = (x + 3)(x - 3)

$$A=x^2-9$$

But, area of the square

$$x^2 = 58$$

A = 49

Now, area of rectangle

$$A = 58 - 9$$

Q11.(A) In triangle PBQ,  $PQ = \sqrt{(PB)^2 + (BQ)^2}$ 

$$=\sqrt{(4)^2+(3)^2}=\sqrt{25}=5$$

Hence perimeter of  $PQRS = 4 \times 5 = 20$ 

Q12.(B) The area of the triangle

$$=\frac{1}{2}(3)(4)=6$$

The total area of 4 triangles =  $6 \times 4 = 24$ 

Now, area of the triangle ABCD  $= 8 \times 6 = 48$ 

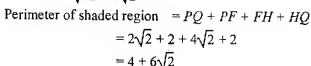
Thus, area of the rectangle PQRS = Area of rectangle ABCD – Total area of the triangle =48-24=24

Q13.(C) Since P and Q are the midpoints of the sides of length 4. Therefore, EP, EQ, PF and QH are all equal to 2.

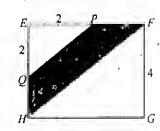
Also 
$$PQ = \sqrt{(2)^2 + (2)^2} = \sqrt{4 + 4} = 2\sqrt{2}$$

Area of 
$$\triangle PEQ = \frac{1}{2}bh = \frac{1}{2}$$
. 2. 2 = 2

In 
$$\triangle FEH$$
,  $FH = \sqrt{(EF)^2 + (EH)^2}$   
=  $\sqrt{16 + 16}$   
=  $\sqrt{32} = 4\sqrt{2}$ 



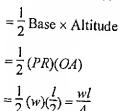
**Q14.** Area of 
$$\triangle EFH = \frac{1}{2}$$
. 4. 4 = 8

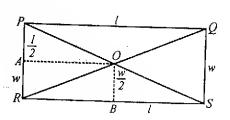


Area of 
$$\triangle PEQ = \frac{1}{2} \cdot 2 \cdot 2 = 2$$

Now area of shaded region = Area of  $\Delta FEH$  - Area of  $\Delta PEQ$ = 8 - 2 = 6

Q15. (B) The area of  $\triangle POR$ 





Also, the area of  $\triangle ORS = \frac{1}{2} \text{Base} \times \text{Altitude}$ 

$$= \frac{1}{2} (RS)(OB) = \frac{1}{2} (I)(\frac{w}{2})$$
$$= \frac{Iw}{4}$$

Q16. (B) Since angle O is acute (:  $m\angle O \angle 90$ ) and angle N is obtuse (:  $90 < m\angle O \angle 180$ ), thus  $(LN)^2 \angle x^2 + y^2$ , where  $(MO)^2 > x^2 + y^2$ 

 $\Rightarrow (MO)^2 > (LN)^2 \Rightarrow MO > LN$ 

Q17. (C) 30 - 60 Right Triangle theorem states, that, in any right triangle with acute angle measures of 30 and 60 and with hypotenuse of length x, the length of the leg opposite the angle with measure 30(shorter leg) is  $\frac{x}{2}$  and the length of the leg

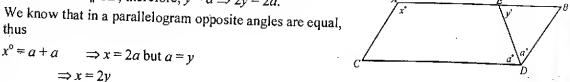


opposite the angle with measure 60 (longer leg) is  $\frac{x}{2}\sqrt{3}$ . Now the longer leg is given which is 25, therefore the hypotenuse will be  $\frac{4S}{\sqrt{3}}$  (:  $\frac{4S}{\sqrt{3}} \times \frac{\sqrt{3}}{2} = 2S$ ) and the perpendicular will be  $\frac{2S}{\sqrt{3}}$  (:  $\frac{4S}{\sqrt{3}} \times \frac{1}{2} = 2S$ )  $\frac{2S}{\sqrt{5}}$ ). Thus the perimeter of the triangle is

$$2S + \frac{2S}{\sqrt{3}} + \frac{4S}{\sqrt{3}} = \frac{2S\sqrt{3} + 2S + 4S}{\sqrt{3}} = \frac{6S + 2\sqrt{3}S}{\sqrt{3}}$$
$$= \frac{2 \cdot \sqrt{3} \cdot \sqrt{3}S}{\sqrt{3}} + \frac{2\sqrt{3}}{\sqrt{3}} \cdot S$$
$$= 2S + 2S\sqrt{3}$$
$$= S(2 + 2\sqrt{3})$$

Q18. (C) The perimeter of a rectangle of area 40 is smallest when the reetangle is a square (because all sides are equal). In that case, each side is  $\sqrt{40}$ , which is greater than 6, and so the perimeter is greater than 24(P=6+6+6+6=24)

Q19. (D) Given that ED is a transversal, which is cutting AB and CD, where  $AB \parallel CD$ , therefore,  $y = a \Rightarrow 2y = \overline{2a}$ . We know that in a parallelogram opposite angles are equal, thus



$$t = 5s + 16$$

$$u = 3s - 12$$

Now 
$$t-u = (5s+16) - (3s-12)$$

$$=5s+16-3s+12$$

$$t - u = 2s + 28 \dots (i)$$

Because, the sum of the measure of two consecutive angles of a parallelogram is 180, therefore

$$(3s-12)+(5s+16)=180 \implies 8s+4=180$$

$$\Rightarrow$$
 8s = 176

$$\Rightarrow$$
  $s = 22$ 

Now substituting the value of s in (i), we have

$$t - u = 2(22) + 28$$

$$t-u = 44 + 28 = 72$$

**Q21.** (A) The sum of the angles of *n*-gives = (n-2)180

$$\therefore$$
  $n = 5$ , thus sum of the angles in a pentagon

$$= (5-2)180 = 3 \times 180 = 540$$

Average of each angle in a pentagon =  $\frac{540}{5}$  = 108

Since each interior angle has three exterior angle, so the sum of two exterior angles is 72 + 72 = 144

Thus the sum of 5 pairs of exterior angles =  $5 \times 144$ 

$$= 720$$

O22. E The area of the rectangle = Iw

The area of the rectangle PQRS = 90 = (x + 5)(x + 2)

$$\Rightarrow x^2 + 7x + 10 = 90$$

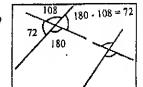
and the area of the rectangle, UVWX

Area = 
$$(x + 4)(x + 3) = x^2 + 7x + 12$$

Which is exactly 2 more than the area of PQRS

hence the Area of UVWX = 90 + 2

$$= 92$$



ides han

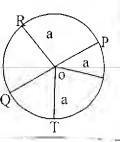
7<sup>B</sup>

### Chapter 4

#### **CIRCLES**

#### Circle.

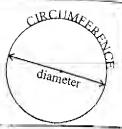
A circle is a set of all points in a plane at a given distance from a fixed point of the plane. The fixed point is the centre of the circle and the given distance is the radius. The adjacent figure is a circle of radius a unit whose centre is at the point O. The point P, Q, R, S and T lies on the circle, each a unit from O. Therefore, the following statement follows from the definition of a circle.



All radii (plural of radius) of the same circle are congruent.

#### Circumference:

The perimeter of a circle is called its circumference.



#### Note:

If "c" stands for the circumference of the circle and "c" is the diameter of the circle, then  $\frac{c}{d}$  (circumference + diameter) is the same for all circles. Its value cannot stated exactly.

The Greek letter  $\pi(pi)$  is used to stand for it.

$$\frac{c}{d} = \pi$$
$$c = \pi d$$

$$c = \pi \times 2 \times r$$

$$c=2\pi r$$

 $\pi$  is a special number and is equal to 3.14159..... or  $\frac{22}{7}$ 

### Angles and Circles:

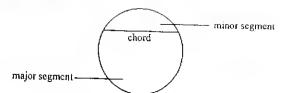
#### Chord:

A line joining two points on the circumference of a circle is called a chord.



#### Note:

A chord divides a circle into two segments.



Ar

Se A t Ta

A I the

AB

Exa In th

Solu OS i

Now

#### Diameter:

A chord which passes through the centre of the circle is a diameter.

#### Arc Length of a Circle:

Arc length of a sector of half a circle is



$$c = \frac{\pi d}{2}$$

Arc length of a sector of quarter of a circle is

$$c = \frac{\pi a}{4}$$



#### Semicireles:

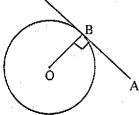
A diameter divides a circle into two congruent halves which are called semicircles.

### Tangent of a Circle:

A line that intersects the circle in exactly one point is a tangent to the circle. The point of intersection is called the point of tangency.

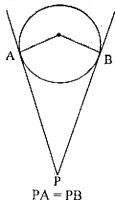
#### Note:

The radius from the centre to the point of tangency is perpendicular to the tangent. 1.



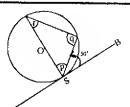
AB is tangent to the circle with centre O. OB is perpendicular to BA.

Tangents from the same point are equal



#### Example 1:

In the given figure, if AB is tangent to the circle. Calculate the sizes of angles, p, q, r.



#### Solution:

OS is the radius and AB is the tangent. By tangent – radius theorem  $\angle$ OSB

$$\angle p = 90^{\circ} - 50^{\circ} = 40^{\circ}$$

Now  $\angle q = 90^{\circ}$  because angle in a semicircle is right. Now angle p, q and r the angles of triangle.

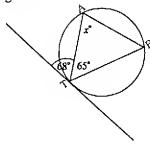
$$\angle p + \angle q + \angle r = 180^{\circ}$$

$$c. 40^{\circ} + 90^{\circ} + r = 180^{\circ}$$

$$c. r = 180^{\circ} - 130^{\circ}$$

Example 2:

What is the value of x in the following diagram?



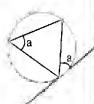
Solution:

In above diagram  $\angle TBA = 68^{\circ}$  because angles in alternate segment are equal

$$x^{\circ} + 65^{\circ} + 68^{\circ} = 180^{\circ} \Rightarrow x = 47^{\circ}$$

Theorems: Tangents and Secants

1. The angle between a tangent and a chord drawn to the point of contact is equal to the angles in the alternate segment.

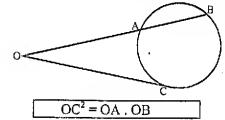


2. The products of the intercepts of two intersecting chords of a circle are equal.

That is:  $px \cdot qx = rx \cdot sx$ 

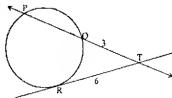
3. If a tangent and a secant intersect in the exterior of a circle, the square of the tangent segment equals the product of the secant segment and the external secant segment.





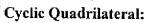
Example:

In the following figure. What is the value of TP?

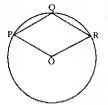


Solution:

$$(TR)^2 = TQ \cdot TP$$
  
 $(6)^2 = 3 \cdot TP$   
 $36 = 3 \cdot TP$   
 $TP = 12$ 



A quadrilateral which has all its vertices laying on the circumference of a circle is called a cyclic quadrilateral.



Note:

Opposite angles of a cyclic quadrilateral add up to 180°.

#### Common Arc Theorem:

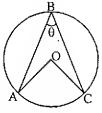
If four points on a circle are, in order and

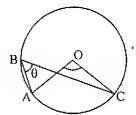
$$\widehat{PQ} \cong \widehat{RS}$$
 Then  $\widehat{PR} \cong \widehat{QS}$ 



### Central Angle Theorems:

1. The angle subtended at the centre of a circle by an arc is twice the angle subtended at the circumference by the same arc.





In above, angle AOC =  $2 \times$  angle ABC.

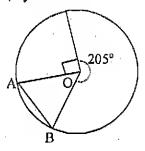
2. The angle measured in degree to complete one revolution in a circle is 360°.

#### Example:

What size angle is subtended at the centre (O) by chord AB?

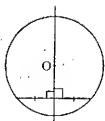
Solution:

$$\angle AOB + 90^{\circ} + 205^{\circ} = 360^{\circ}$$
  
 $\angle AOB + 295^{\circ} = 360^{\circ}$   
 $\angle AOB = 360^{\circ} - 295^{\circ}$   
 $= 65^{\circ}$ 



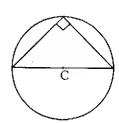
.. Chord AB subtends an angle of 65° at the centre.

Theorem: A line from the centre of a circle through the mid-point of a chord meets the chord at right angles.



### Theorem: Angle In a Semicircle:

An angle in a semicircle is a right angle.



#### Converse of Theorem:

If a circle passes through the ventricles of a right-angled triangle, then the hypotenuse of the triangle is a

diameter of the circle.

### More Angles and Arcs:

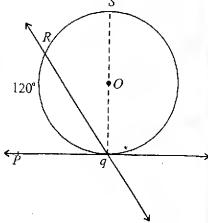
#### Theorem 1:

If a tangent and a secant (or chord) intersect in a point on a circle, the measure of the angle formed is one half the measure of the intercepted arc.

### **Explanation:**

In circle O as shown in the figure, secant QR and tangent PQ intersect at point Q on the circle, forming angle PQR. The above theorem focuses upon the relationship between the measure of this angle and the degree measure of the intercepted arc,  $\widehat{QR}$ .

According to this theorem, 
$$\angle PQR = \frac{1}{2}(120)$$
  
=  $\frac{1}{2}(Arc QR)$   
=  $60^{\circ}$ 



#### Theorem 2:

If two secants (or chords) intersect in the interior of a circle, the measure of an angle formed is one half the sum of the measures of he arcs intercepted by the angle and its vertical angle.

#### **Explanation:**

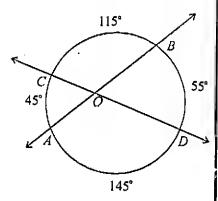
When two secants AB and CD intersect in the interior of a circle, as circle O shows to the right, two pair of vertical angles are formed. According to the given theorem

$$\angle AOC = \angle DOB = \frac{1}{2}(55^{\circ} + 45^{\circ})$$

$$= \frac{1}{2}(100) = 50^{\circ}$$
and  $\angle AOD = \angle COB = \frac{1}{2}(145^{\circ} + 115^{\circ})$ 

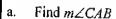
$$= \frac{1}{2}(260)$$

$$= 130^{\circ}$$



### Example 1:

Chord AC and DE intersect at T,  $\overrightarrow{AB}$  is tangent to the circle at A.  $m\widehat{AD} = 114$ ,  $m\widehat{EC} = 36^{\circ}$  and  $m\widehat{AE} = 75$ 



Find  $m \angle ATD$ 

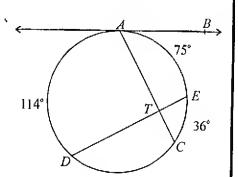
Solution: a. By theorem 1

$$m\angle CAB = \frac{1}{2}m\widehat{AC}$$

$$= \frac{1}{2}(m\widehat{SR} + m\widehat{RT})$$

$$= \frac{1}{2}(75^{\circ} + 36^{\circ})$$

$$= \frac{1}{2}(111)$$



Sol

b.

b. By theorem 2

$$m \angle ATD = \frac{1}{2} (m \widehat{EC} + m \widehat{AD})$$

$$= \frac{1}{2} (36^{\circ} + 114^{\circ})$$

$$= \frac{1}{2} (150)$$

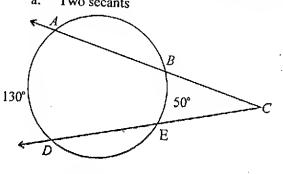
$$= 75$$

#### Theorem 3:

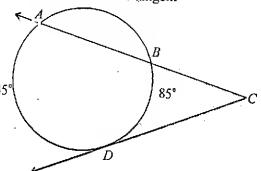
If two secants, a tangent and a secant, or two tangents intersects in the exterior of a circle, the measure of the angle formed is one-half the difference of the measures of the intercepted arcs.

**Example 2:** In each case of the following figure, find  $m \angle C$ .

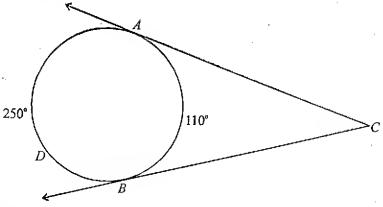
Two secants



One secant one tangent



Two tangents



#### Solution:

Applying theorem 3

$$m\angle C = \frac{1}{2}(m\widehat{AD} - m\widehat{BE})$$
$$= \frac{1}{2}(130 - 50)$$
$$= \frac{1}{2}(80) = 40$$

Applying theorem 3

$$m\angle C = \frac{1}{2}(m\widehat{AD} - m\widehat{BD})$$

$$= \frac{1}{2}(250 - 110)$$

$$= \frac{1}{2}(140)$$

$$= 70$$

Applying theorem 3

$$m\angle C = \frac{1}{2}(m\widehat{ADB} - m\widehat{AB})$$
$$= \frac{1}{2}(250 - 110)$$
$$= \frac{1}{2}(150)$$
$$= 75$$

- If the area of a circle is  $81\pi$ , then its circumference is: Q1.
  - **(A)**  $61\pi$

**(B)**  $20\pi$ 

(C)  $18\pi$ 

- **(D)**  $16\pi$
- If circumference of a circle is  $3\pi$ , then its area is: Q2.
  - (A)

**(B)** 

 $4\pi^2$ (C)

- (D)
- If a circle is inscribed in a square of area 4, then the area of the circle is: Q3.
  - (A)  $\pi$

**(B)** 

(C)

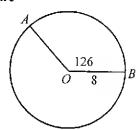
- (D)
- If a square of area 3 is inscribed in a circle, then the area of the circle is: Q4.
  - (A)

 $9\pi^2$ **(B)** 

**(C)** 

 $\sqrt{3}\pi$ **(D)** 

Questions 5 - 6 refer to the following figure



- Q5. What is the length of arc AB?
  - (A)  $2.6\pi$

**(B)**  $5.6\pi$ 

(C)  $7.6\pi$ 

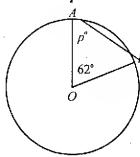
- **(D)**
- Q6. What is the area of the shaded sector?

(A)  $22.9\pi$ 

**(B)**  $22.4\pi$ 

(C)  $60\pi$ 

- $(\mathfrak{D})$  62.3 $\pi$
- Q7. In the following figure, what is the value of p?



**(A)** 49

**(B)** 39

(C) 59

- (D) 69
- Q8. If P represents the area and W represents the circumference of the circle, then P in terms of W is:
  - (A)  $\frac{2\pi}{W}$

(B)  $\frac{4\pi^2}{W}$ 

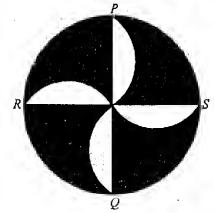
(C)  $\frac{2\pi^2}{W^2}$ 

- (D)  $\frac{W^2}{4\pi}$
- Q9. What is the area of a circle whose radius is the diagonal of a square whose area is 9?
  - (A)  $\sqrt{3}\pi$

(B)  $12\pi$ 

(C)  $4\pi$ 

- (D) 13π
- Q10. In the following figure, PQ and RS are perpendicular, and each of the unshaded regions is a semicircle. What is the ratio of the white area to the shaded area?



 $(\mathbf{A}) \quad \frac{4}{\pi}$ 

(B) -

(C)  $\frac{2}{3}$ 

- (D)  $\frac{1}{2}$
- Q11. If C is the circumference of a circle of radius r, then which of the following statement is true?
  - (A)  $\frac{C}{r} < 6$

(B)  $\frac{C}{a} = 6$ 

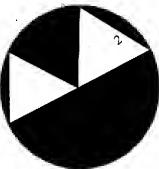
(C)  $\frac{C}{r} > 6$ 

- (D)  $\frac{C}{n} = \tau$
- Q12. If C is the circumference of a circular disk in centimeters, and A is the area of the same circular disk in square centimeter. Then  $\frac{C}{A} = \frac{A}{C}$ , iff r =



(A) 1

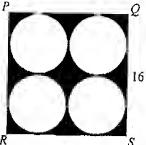
- **(B)** 2
- (C) (D)
- Q13. In the following figure, what is the area of the shaded region, if each of the triangle is equilateral?



(A)  $8\pi$  (B)

(C)  $3\pi$ 

- **(D)** 6π
- Q14. In the following figure, PQRS is a square, and all the circles are tangent to one another and to the sides of the squares. What is the area of the shaded region?

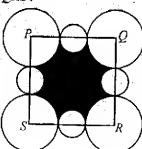


(A) 256

**(B)** 64π

(C) 256π.

- **(D)**  $64(4-\pi)$ In the following figure, the large circles have radius 4, and the small circles have diameter 4. Q15. What is the area of the square PQRS?

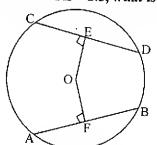


(A) 144

(B) 169

100 (C)

- (D) 64
- In the following figure, if AB = CD and OE = 2.5, what is the value of OF? Q16.



d to

r 4.

- (A)
- 6.25

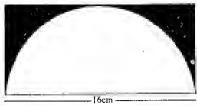
(B)

- **(C)** 
  - 1.58

2.5 **(D)** 

5

Q17. A semicircle is drawn inside a rectangle as shown.



The shaded area is closest to:

50

30

(A)

(B)

**(C)** 

45 (D)

40

In the following figure, if the radius of the outer circle is p and the radius of each of the circles Q18. inside the larger circle is  $\frac{p}{3}$ , then what is the area of the shaded region?



(A)  $\frac{2}{9}\pi p^2$ 

 $\frac{22}{9}\pi p^2$ 

- **(D)**
- A circle is inscribed in a square of area  $\sqrt{6}$ . What is the area of the circle?
  - (A)

**(B)** 6π

(C)

- **(D)**  $9\pi$
- Q20. A circle of radius 5 mm is removed from the centre of a circular piece of metal of radius 7 mm to make a washer as shown below:



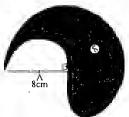
What is the area of the shaded region?

 $35\pi^2$ 

(A)  $25\pi$  **(B)**  $49\pi$ 

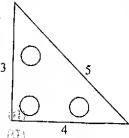
(C)

- (D)  $24\pi$
- In the following metal cam, A, B and C are the centres of the semicircles shown. What is the area Q21. of the cam?



- (A) 32.07 cm<sup>2</sup>
- (C)  $101.53 \text{ cm}^2$

- **(B)** 157.08 cm<sup>2</sup>
- (D)  $201.06 \text{ cm}^2$
- Q22. The sketch below shows a triangular copper plate with sides of 3cm, 4cm and 5cm. It has three small circular holes cut out of it. The radius of each circle is 3mm. What is the area of the copper triangle?



- $(A) \qquad 6 \text{ cm}^2$
- (C)  $5.9973 \text{ cm}^2$

(B) 5.16 cm<sup>2</sup>

Q4

Q5:

Q6.

Q7.

Q8. :

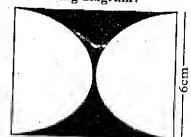
Q9. (

- **(D)**  $5.71 \text{ cm}^2$
- Q23. What is the shaded area in the following diagram?



- (A)  $50.29 \text{ cm}^2$
- (C)  $16.29 \text{ cm}^2$

- (B)  $16 \text{ cm}^2$
- (D)  $34.29 \text{ cm}^2$
- Q24. What is the shaded area in the following diagram?



- (A)  $36 \text{ cm}^2$
- (C)  $28.3 \text{ cm}^2$

- (B)  $7.72 \text{ cm}^2$
- **(D)**  $14.14 \text{ cm}^2$

# Explanatory Answers

Q1. (C) Area of a circle:  $A = \pi r^2 = 81\pi$   $\Rightarrow r^2 = 81 \Rightarrow r = 9$ 

Circumference of a circle:  $C = 2\pi r \Rightarrow C = 2\pi(9) = 18\pi$ 

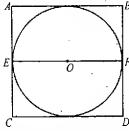
Q2. (D) Circumference of a circle:  $C = 2\pi r \Rightarrow 2\pi r = 3\pi$ 

$$\Rightarrow r = \frac{3}{2}$$

Area of a circle:  $A = \pi r^2 \Rightarrow A = \pi \cdot \left(\frac{3}{2}\right)^2 \Rightarrow A = \frac{9\pi}{4}$ 

Q3. (A) First of all, we draw the diagram

ree per



Since the area of the square is 4 (given), therefore AC = 2, as in a square all sides are equal, therefore AC = AB = BD = CD = 2.

: Diameter of the circle,  $EF = CD = AB \Rightarrow EF = 2$ 

and radius of the circle = r = OF = OE = 1 (half the diameter)

Hence the area of the circle with radius 1 is

$$\pi(1)^2 = \pi$$

Q4. (A) First we draw a diagram, because area of the square is 3, thus  $AC = \sqrt{3}$ , then diagonal  $BC = \sqrt{3} \times \sqrt{3}$ = 3, but BC is also the diameter of the circle, hence the diameter is 3 and radius is 1.5

Now, the area of the circle  $A = \pi r^2 \Rightarrow A = \pi (1.5)^2 \Rightarrow A = 2.25\pi = \frac{9}{4}\pi$ Q5: (B) Setting a proportion

> AB: OB:: 126:360  $\overline{AB} = \left(\frac{126}{360}\right) \times 2\pi r$  $\overline{AB} = \left(\frac{126}{360}\right) \times 2\pi \times 8$

$$\overline{AB} = 5.6\pi$$

Q6. (B) The area of shaded sector is  $\frac{126}{360}\pi(8)^2$ 

 $\approx (0.35)\pi(64)$  $= 22.4\pi$ 

Q7. (C) Because, the triangle is isosceles therefore, the angle B is also p, thus

 $p^{o} + p^{o} + 62^{o}$  $=180^{\circ}$  $2p^{\circ} = 118 \Rightarrow p = 59$ 

Since, P is the area, so  $P = \pi r^2$ , and

W is the perimeter, thus  $W = 2\pi r \Rightarrow r = \frac{W}{2\pi}$ 

 $\Rightarrow P = \pi \left(\frac{W}{2\pi}\right)^2$  $P = \pi \, \frac{W^2}{4\pi^2}$  $\Rightarrow P = \frac{W^2}{4\pi}$ 

Q9. (B) Since the area of the square is 9, so its each side is 3, and the length of the diagonal will be  $\sqrt{3} + \sqrt{3} = 2\sqrt{3}$ 

Thus area of the circle of radius  $2\sqrt{3}$  is

$$A = \pi r^2 \Rightarrow A = \pi (2\sqrt{3})^2 \Rightarrow A = 12\pi$$

Q10. (B) Let the radius of the big circle be r, then its area will be  $\pi r^2$ , also the radius of the semicircle becomes  $\frac{r}{2}$ , so area of the small eircle will be  $\pi \frac{r^2}{2}$  and the area of the each semicircle is

$$\left(\pi \frac{r^2}{4}\right) \times \frac{1}{2} = \frac{\pi r^2}{8}$$

Then the area of the four small semicircles is

$$=4\left(\frac{\pi r^2}{8}\right)=\frac{\pi r^2}{2}.$$

So, shaded area = Total area - White area

$$= \pi r^2 - \frac{\pi r^2}{2} = \frac{\pi r^2}{2}$$

Therefore the ratio of shaded area is

$$\frac{\pi r^2}{\frac{2}{\pi r^2}} = \frac{1}{1}$$

Q11. (C) Since  $C = 2\pi r \Rightarrow C = \pi(2r)$ , but 2r = d

Hence 
$$C = \pi d \Rightarrow \pi = \frac{C}{d} \Rightarrow \frac{C}{r} = 2\pi$$

$$\Rightarrow \frac{C}{2} = 2\left(\frac{22}{7}\right) > 6$$

Q12. (B) As  $C = 2\pi r$  and  $A = \pi r^2$ , so

$$\frac{C}{A} = \frac{2\pi r}{\pi r^2} = \frac{2}{r}$$

and 
$$\frac{A}{C} = \frac{\pi r^2}{2\pi r} = \frac{r}{2}$$

Thus 
$$\frac{C}{A} = \frac{A}{C}$$
, only possible, when  $r = 2$ 

Q13. (B) Because the triangles are equilateral, then the white central angles each measure  $60^{\circ}$ , so their sum = 60 + 60 = 120. Then, the unshaded area is  $\frac{120}{360} = \frac{1}{3}$  of the circle, so the shaded area of  $\frac{2}{3}$  of the circle.

As the area of the circle =  $\pi r^2 = \pi (2)^2 = 4\pi$ 

and the area of the shaded region  $=\frac{2}{3} \times 4\pi = \frac{8}{3}\pi$ 

Q14. (D) Since QS = 16, thus the diameter of each circle is 8, and radius of each circle is 4.

The area of each circle  $= \pi r^2 = \pi (4)^2 = 16\pi$ 

Thus, the area of four circles  $= 4(16\pi) = 64\pi$ 

Now, the area of the square=  $16 \times 16 = 256$ 

Area of the shaded region = Area of the square - Area of the circle

$$= 256 - 64\pi$$

$$= 64(4 - \pi)$$

Q15. (A) Since the radius of the large circle is 4, and diameter of the small circle is 4, so each side of the square is 4 + 4 + 4 = 12, so area of the rectangle =  $12 \times 12 = 144$ 

ircle

Q16. (D)

$$OF = 2.5$$

Because equal chords are equidistant from centre.

Q17. (C) Area of the rectangle =  $16 \times 8 = 128$ 

Area of the circle of radius  $8 \text{cm}^2 = \pi(8)^2$ 

$$= 64\pi$$

Area of the semicircle  $=\frac{64}{2}\pi = 32\pi$ 

$$=32(3.14)=100.48$$

Area of the shaded region = Area of rectangle - Area of the semicircle

$$= 128 - 100.48$$

which is closest to 30

Q18. (D)Area of the outer circle  $= \pi(p)^2 = \pi p^2$ 

Area of the inner circle =  $\pi \left(\frac{p}{3}\right)^2 = \frac{\pi p^2}{9}$ 

Total area of the inner circles

$$=\frac{\pi p^2}{9}+\frac{\pi p^2}{9}$$

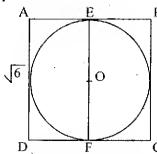
$$=\frac{2}{9}\pi p^2$$

Area of the shaded region =  $\pi p^2 - \frac{2\pi p^2}{9}$ 

$$=\frac{9\pi p^2-2\pi p^2}{9}$$

$$=\frac{7}{9}\pi p^2$$

Q19. (A) The inscribed circle in a square of area 6 is



The side AD =  $\sqrt{6}$  and also the diameter =  $\sqrt{6}$ . The radius of the circle O is OF =  $\frac{\sqrt{6}}{2}$   $\Rightarrow$  OF =

$$\sqrt{\frac{3}{2}}$$

The area of the circle of radius  $\sqrt{\frac{3}{2}}$  is

sum = ircle.

of the

Area = 
$$\pi \left( \sqrt{\frac{3}{2}} \right)^2 \implies Area = \frac{3}{2}\pi$$

Q20. (D)

Area of the washer removed  $= \pi r^2 = \pi (5)^2 = 25\pi$ 

Area of the metal 
$$= \pi r^2 = \pi (7)^2 = 49\pi$$

Area of the shaded region  $= 49\pi - 25\pi = 24\pi$ 

Q21. (C) When we shift the semicircle of diameter 8cm in the space the shape becomes semicircle of diameter 16cm

Area 
$$= \pi r^2$$
  
 $= \pi \times (8)^2 = 64\pi$   
Area of semicircle  $= \frac{64\pi}{2} = 32\pi = \boxed{101.53 \text{ cm}^2}$ 

Q22. (B) Area of the triangle  $=\frac{1}{2} \times \text{base} \times \text{Altitude}$  $=\frac{1}{2} \times 4 \times 3 = 6 \text{cm}^2$ 

Now 
$$3mm = 0.3cm$$

Area of the circle  $= \pi r^2 = 0.28 \text{cm}^2$ 

Area of 3 circles  $= 3 \times 0.28 = 0.84$ cm<sup>2</sup>

Area of copper in plate = 6 - 0.84 = 5.16cm<sup>2</sup>

Q23. (D) Diameter of the circle = 8cm

Area of the circle  $= \pi r^2 = \frac{22}{7} \times 16 = 50.29 \text{cm}^2$ 

Area of triangle =  $\frac{1}{2}$  bases × altitude =  $\frac{1}{2}$  × 4 × 4 = 8 cm<sup>2</sup>

Area of 2 triangles  $= 2 \times 8 = 16 \text{cm}^2$ 

Area of the shaded region =  $50 \cdot 29 - 16 = 34.29 \text{ cm}^2$ 

Q24. (B) Area of the semicircle  $=\frac{1}{2}\pi d$ 

$$=\frac{1}{2}.\pi.r^2=\frac{1}{2}\pi(3)^2$$

$$= 14.14 \text{ cm}^2$$

Area of the 2 same semicircles =  $2 \times 14.14 = 28.28$ cm<sup>2</sup>

Area of the square  $= 6 \times 6$ 

$$=36 \text{cm}^2$$

Area of the shaded region =  $36 - 28.28 = 7.72 \text{cm}^2$ 

: of

Chapter 5

#### AREA

#### Some Important Formulae

- (1) Area of a rectangle or square =length × breadth
- (2) Perimeter of a rectangle or square = 2 (length + breadth)
- (3) Area of a triangle =  $\frac{1}{2} \times \text{base} \times \text{height}$
- (4) Area of a triangle of sides a, b, and c =  $\sqrt{s(s-a)(s-b)(s-c)}$

where 
$$s = \frac{(a+b+c)}{2}$$

- (5) Area of a circle =  $\pi r^2$
- (6) Circumference of a circle  $= 2\pi r$
- (7) Area of four walls of a room =  $2(length + breadth) \times height$
- (8) Area of a parallelogram =base × height
- (9) Area of a trapezium  $= \frac{1}{2} \times \text{sum of two parallel sides} \times \text{width}$
- (10) Area of a regular hexagon of side  $a = 6a^{3}$

#### **Model Examples**

Q.1. The difference between the circumference of a circle and its diameter is 135 ft. Find the area of the circle.

$$\left(Take\pi = \frac{22}{7}\right)$$

Sol. Let r be the radius of the circle, then circumference of circle

$$=2\pi r$$

Diameter of circle = 2 r

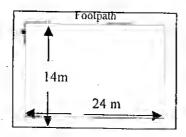
By the given condition

$$= 2\pi r - 2 r = 135$$

$$r = \frac{63}{2} \text{ ft.}$$

Area of circle = 
$$\pi r^2$$
  
=  $\frac{22}{7} \times \frac{63}{2} \times \frac{63}{2}$  sq. ft.  
= 3118.5 sq. ft. Ans

Q.2. How many tiles 20 cm. square will be required to have a foot path 1 metre wide carried round the outside of grass plot 24 meter long by 14 metres broad?



Sol. Area of the grass plot  $= 24 \times 14$ = 336 sq. m.

Length and breadth of the plot including the path is = 26 m and 16 m

Area of plot including path  $= 26 \times 16$ 

$$=416 \text{ sq. m.}$$

Area of path = 
$$416 - 336 = 80 \text{ sq. m.}$$

Area of one til = 
$$\frac{20}{100} \times \frac{20}{100} = \frac{1}{25}$$
 sq. m.

No. of tiles required 
$$=\frac{80}{\frac{1}{25}} = 80 \times 25$$

Q.3. If the length of a reetangular piece of land were 5 metres less and the breadth 2 metres more, the area would be 10 sq. m. less; but if the length were 10 metres more and breadth 5 metres more, the area would have been 275 sq. m. more. Find its length and breadth.

Sol. Let the length be 'l' breadth 'b'

area = 
$$l \times b$$

Then 
$$(l-5)(b+2) = lb-10....(i)$$

And 
$$(l+10)(b+5) = lb+275....(ii)$$

From (i)

$$lb + 2l - 5b - 10 = lb - 10$$

$$2l = 5b$$
  $\Rightarrow l = \frac{5}{2}b$ 

From (ii)

$$lb + 5l + 10b + 50 = lb + 275$$
  $\Rightarrow$   $5l + 10b = 225$ 

Putting

$$l = \frac{5}{2}b$$

$$\frac{25}{2}b + 10b = 225 \implies \frac{45}{2}b = 225$$

$$b = \frac{2 \times 225}{45} = 10 \text{ and } l = 25 \text{ m}$$

$$b = \frac{2 \times 225}{45} = 10$$
 and  $l = 25$  m

Q.4. The perimeter of one square exceeds the perimeter of another square by 120 metres and the area of the larger square exceeds twice the area of the smaller square by 900 square metres. Find the length of the sides of the squares.

Sol. Let the length of one side of larger square = x sq. m

Let the length of one side of smaller square = y mts.

Now by the given condition the primeter (4x) of larger exceeds the perimeter of smaller (4y) by 120 sq. m

.... (i)

*i.e.*, 
$$4x - 4y = 120$$

or 
$$x = 30 + y$$

Again by the second condition

$$x^2 - 2y^2 = 900$$

.... (ii)

Putting the value of x from (i) in (ii), we get

$$(30+y)^2 - 2y^2 = 900 \implies -y^2 + 60y = 0$$

or

y = 60

Putting the value in (i) we get x = 90

Larger square side length is = 90 sq. m

Smaller square side length is = 60 sq. m

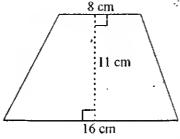


- Q1. The surface area of sphere of radius  $3\frac{1}{2}$  cm is:
  - (A) 130 sq.cm

(B) 69 sq.cm

(C) 154 sq.cm

- (D) 98 sq.cm
- Q2. The area of the following trapezium is:

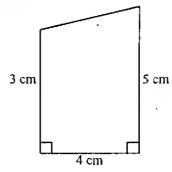


(A) 125 sq.cm

(B) 132 sq.cm

(C) 139 sq.cm

- (D) 97 sq.cm
- Q3. The area of the following figure is:



(A) 16 sq.cm

(B) 15 sq.cm

(C) 60 sq.cm

(D) None of these

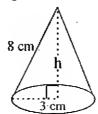
9 cm

- Q4.
  - The height of a triangle of base 3 cm and area 9 cm is:

    (A) 6 cm (B)
    - (B)

(C) 18 cm

- (D) 22 cm
- Q5. What is the surface of the following figure?



the

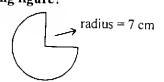
за /е Q6.

- (A)  $33\pi$
- (C) 25π

**(B)**  $24\pi$ 

**(D)** 

What is the area of the following figure?

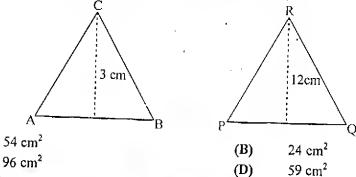


- **(A)** 125 sq.cm
- (C) 64 sq.cm

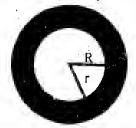
**(B)** 150.72 sq.cm

 $11\pi$ 

- (D) 56 sq.cm
- Q7. The following two triangles are similar. Find the area of PQR?



The area of the shaded region of the following figure is? Q8,



 $\pi^2(r^2 - R^2)$ (A)

(A)

(C) ·

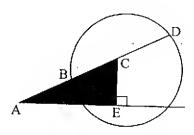
 $\pi^2(R+r)(R-r)$ (C)

- $\pi r^2 + \pi R^2$ **(B)**
- $\pi(R+r)(R-r)$ **(D)**
- The area of the sector which contains an angle of 60° of circle of radius 7 cm, is: Q9,
  - $25\frac{2}{3}$  cm<sup>2</sup> (A)

 $27\frac{2}{3}$  cm<sup>2</sup> **(B)** 

41 cm<sup>2</sup> (C)

- $\sqrt{3} \frac{5}{28} \text{ cm}^2$ **(D)**
- Q10. In the following figure, what is the area of the right triangle? If  $\overline{AE} = 16$  cm and  $\overrightarrow{BD} = 12 \text{ em}$



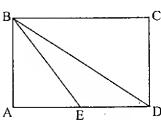
(A) 6

(B)

(C) 8

49 **(D)** Not possible Q11. In the figure below, ABCD is a rectangle and E is the mid point of one side, what is the area of triangle BCD?

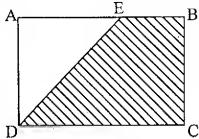
If  $\overline{BE} = 5$  cm and  $\overline{CD} = 3$ cm



- (A)  $12 \text{ cm}^2$
- (C) 9 cm<sup>2</sup>

- **(B)** 25 cm<sup>2</sup>
- **(D)**  $17.23 \text{ cm}^2$

Q12. In the figure below, given that AD = 6, CD = 8, AE = x. What is the area of the shaded region?



(A) 28 - 2x

(B) 4(14-4x)

(C) 48 - 3x

**(D)** 7(6-3x)

Q13. If the radius of the circle is decreased by 20%, what happens the area?

(A) 10% in crease

(B) 20% decrease

(C) 80% increase

(D) 36% decrease

Q14. A square, with perimeter 16, is inscribed in a circle, what is the area of the circle?

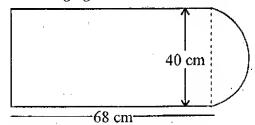
(A)  $3\pi$ 

(B)  $2\sqrt{2}\pi$ 

(C) 32π

(D) 8π

Q15. Calculate the area of the following figure which is consists of:



The rectangle is of 40 cm and 68 cm and half a circle of diameter 40 cm

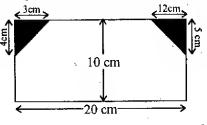
(A)  $2535 \text{ cm}^2$ 

**(B)**  $2720 \text{ cm}^2$ 

(C)  $3348 \text{ cm}^2$ 

**(D)**  $628 \text{ cm}^2$ 

Q16. What is the area of the following shake if the shaded areas are cut away?



(A) 100 cm<sup>2</sup>

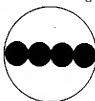
**(B)**  $125 \text{ cm}^2$ 

- 164 cm<sup>2</sup> (D)
- Q17. The length of rectangle is decreased by 15% and its width is increased by 40%. The area is:
  - (A) decreases by 25%

**(B)** no effect

(C) increases by 36%

- (D) increases by 19%
- In following figure equal circles lie along the diameter of the large circle. If the circumference of Q18. the circle is  $64\pi$ . What is the area of the shaded region?



- (A) 64π
- (C)  $16\pi$

- **(B)**  $256\pi$
- (D) None of these

Q1. (C) A = 
$$4\pi r^2$$
  
=  $\frac{4}{1} \times \frac{22}{7} \times \frac{7}{2} \times \frac{7}{2}$  sq.cm  
= 154 sq.cm

Q2. (B) A = Average width × Height  
= 
$$\frac{(8+16)}{2}$$
 × 11 sq.cm  
= 132 sq.cm

Q3. (A) 
$$A = \frac{(3+5)}{2} \times 4$$
  
= 16 sq.cm

**Q4.** (A) 
$$9 = \frac{1}{2} \times 3 \times h$$

$$\therefore \quad h = \frac{2 \times 9}{3}$$

Q5. (A) S = 
$$\pi rs + \pi r^2$$
  
=  $(\pi \times 3 \times 8) + \pi (3 \times 3)$   
=  $24\pi + 9\pi = 33\pi$ 

Q6. (B) The figure is 
$$\frac{3}{4}$$
 of the circle, Now

Area of the whole circle =  $\pi r^2$ 

$$\frac{3}{4}$$
 of the circle =  $\frac{3}{4}(3.14)(18)^2$ 

$$= \frac{3}{4} \times 200.96$$

$$= 150.72 \text{ cm}^2$$

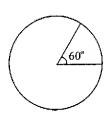
Q7. (A) 
$$\frac{AB}{DE} = \frac{\text{height of the triangle ABC}}{\text{height of the triangle DCP}}$$

height = 
$$\frac{36 \text{ cm}}{4}$$
 = 9cm

Area = 
$$\frac{1}{2} \times \text{base} \times \text{height} = \frac{1}{2} \times 12 \times 9$$
  
= 54 cm<sup>2</sup>

Q8. (D) Area= Whole - hole  
= 
$$\pi R^2 - \pi r^2$$
  
=  $\pi (R^2 - r^2) = \pi (R - r)(R + r)$ 

Q9. (A) Sector 
$$=\frac{\theta^{\circ}}{360^{\circ}} \times \pi r^{2}$$
  
 $=\frac{60}{360} \times \frac{22}{7} \times \frac{7}{1} \times \frac{7}{1} \text{ cm}^{2}$   
 $=25\frac{2}{3} \text{ cm}^{2}$ 



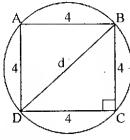
- Q10. (D) The area of the height triangle equals half the product of two legs. The point E is not on the circle, The length CE is given. We cannot find the exact value of CE. So tacking the length of CE, we cannot calculate the area.
- Q11. (A) In the given rectangle,  $\overline{AB} = \overline{CD} = 3$ cm. The length of the side AE of triangle BAE can be found with the Pythagorean theorem as:

$$(BF)^2 = (AB)^2 + (AE)^2 \Rightarrow 25 = 9 + (AE)^2$$
  
\Rightarrow (AE)^2 = 16 \Rightarrow AE = 4

As point E is the mid point of  $\overline{AD}$ , the length of the rectangle is twice  $\overline{AE}$  or 8 cm. The area of the right triangle BCD is half the product of the sides adjacent to the right angle

$$A = \frac{1}{2} bh = \frac{1}{2} (8)(3) = 12 cm^2$$

- Q12. (C) The difference between the entire rectangle and the white triangle is the shaded area. Thus  $(6 \times 8 = 48) \frac{6 \times x}{2} = 48 3x$
- Q13. (D) If the radius of a circle is 1, after reducing 20% it becomes 0.8. Since Area =  $0.8 \times 0.8 = 0.64 = 1 0.64 = 0.36 = \%$
- Q14. (D) Since the area of the square is 16.∴ caeh side of the square is 4. In ΔBCD



$$(4)^2 + (4)^2 = (BD)^2 \Rightarrow BD = \sqrt{32} = 4\sqrt{2}$$

The radius of the circle  $=\frac{d}{2} = \frac{4\sqrt{2}}{2} = 2\sqrt{2}$ 

Area of the circle = 
$$\pi r^2 = \pi (2\sqrt{2})^2 = \pi (4)(2) = 8\pi$$

Q15. (C) Area of the work surface = Area of the rectangle + area inside half a circle

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Area of the rectangle = 
$$68 \text{ cm} \times 40 \text{ cm} = 2720 \text{ cm}^2$$

Area of the circle = 
$$\pi r^2 = 3.14 \times \left(\frac{40}{2}\right)^2 = 3.14 \times (20)^2$$
  
= 628 cm<sup>2</sup>

Area of the shape 
$$= 2720 \text{ cm}^2 + 628 \text{ cm}^2$$

 $= 3348 \text{ cm}^2$ 

Area of rectangle 
$$= 20 \times 10 = 200 \text{ cm}^2$$

Area of first triangle 
$$=\frac{1}{2}(3)(4)=6 \text{ cm}^2$$

Area of second triangle = 
$$\frac{1}{2}(12)(5) = 30 \text{ cm}^2$$

Area of unshaded region = 
$$200 - 6 - 30 = 164 \text{ cm}^2$$

# Q17. (D) The 85%L shows a 15% decrease in length 140% W represents a 40% increase in width. The news rectangle will be

= 
$$(80\% \text{ L})(40\% \text{ W}) = \frac{85}{100} \text{L} \times \frac{40}{100} \text{W}$$

$$=\frac{119}{100} LW$$

# The area of new rectangle will increase (119% - 100%) = 19%

# Q18. (B) The circumference of big circle = $64 \pi$

We know circumference 
$$= 2\pi r$$

$$\Rightarrow$$
 64 $\pi$  = 2 $\pi$ r  $\Rightarrow$  r = 32

From given radius of the small circle = 8

Area of the small circle = 
$$\pi r^2 = \pi (8)^2$$

$$=64\pi$$

$$= 4(64\pi)$$

$$= 256\pi$$



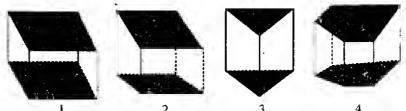
#### Chapter 6

#### SOLID GEOMETRY

#### Prism:

A prism is a solid figure bounded by plane faces, two of which (called the ends) are called congruent figures in parallel planes, and the others (called the sides) are parallel ogram.

The solids shown below are prisms. The parts of intersecting planes that determine each prism are its faces. Two faces, F and F', are bases of each prism. The other faces are lateral (side) faces. The intersections of the faces are called edges.



Prism	Name	Description
1	Rectangular solid	All six faces are rectangles.
2	Cube	A rectangular solid in which all edges are congruent.
2	Triangular prism	The bases are triangles.
4	Pentagonal prism	The bases are pentagons.

#### Right Prism:

The above four prisms in the figure are right prisms because a lateral edge is perpendicular to the plane of a base.

#### Oblique Prism:

A prism that does not have the right prisms property is oblique prism.

#### Altitude of a Prism:

An altitude of a prism is a segment that is perpendicular to the planes of the bases and that has an end point in each plane. In a right prism, any lateral edge is an altitude.

#### Surface Area of Prism:

The total surface area of prism is the sum of its lateral surface areas and its two bases.

#### Literal Surface Area:

The literal surface area of a prism is the sum of the areas of its lateral faces.

The lateral surface area L of a right prism is the product of the perimeter P of its base and its lateral edge, e. That is

$$L = Pe$$

Example: Find the total area of the following regular hexagonal prism

#### Solution:

Step 1: First, find the lateral area

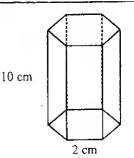
$$L = Pe$$

Here,  $P = 6 \times 4 = 24$  and e = 20

Hence  $L = 24 \times 20 = 480$ 

Step 2: Area of one base

Since, the area A of a regular polygon equals one half the product of its perimeter P and the apothem a



$$A = \frac{1}{2}ap$$

$$= \frac{1}{2} \cdot 2\sqrt{3} \cdot 24$$

$$= 24\sqrt{3}$$

Step 3: Total area

$$^{\circ}$$
 otal area (480 + 24 $\sqrt{3}$ ) cm<sup>2</sup>

#### Surface Area of Rectangular Solid:

The surface area of rectangular solid

=  $2(length \times breadth + breadth \times height + length \times height)$ 

$$=2(lb+bh+lh)$$



In the case of cube, l = b = h = e

... Surface Area of a cube 
$$= 2(e \times e + e \times e + e \times e)$$
  
 $= 2(e^2 + e^2 + e^2)$   
 $= 2(3e^2)$   
 $= 6e^2$ 

## Volume of Rectangular Solid:

The volume of a rectangular prism is the product of its altitude h, the length of the base l, and the width of the base w. That is

$$V = lwh$$

#### Volume of Prism:

The volume of a prism is the product of its altitude h and the area of the base, B.

$$V = Bh$$

#### Volume of Cube:

The volume V of a cube with edge e is the cube of e. That is

$$V = e^3$$



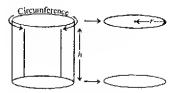
#### Cylinder:

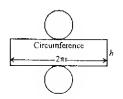
A right circular cylinder is formed by the revolution of a rectangle around one of its sides. The ends of a right circular cylinder are congruent circles and the line joining the centre of the circular is perpendicular to the plane of the ends.

#### Surface of a Cylinder:

The surface of a cylinder consists of two congruent circular ends and a curved surface between them. If the circles are removed from the ends, and the curved surface is cut, a rectangle is produced.









From analysis of cylinder, we conclude, that

The height of the rectangle is the same as the height of the cylinder.

The length of the rectangle is the same as the circumference of the circle at the end.

The area of the two circles is  $2\pi r^2$ .

The area of the curved surface is  $2\pi rh (l \times b)$  of the rectangle).

#### Surface Area of a Cylinder:

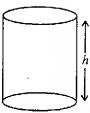
The surface area of a cylinder is double the area of one end plus the area of the curved surface.

Surface Area =  $2\pi r^2 + 2\pi rh$ 

here  $2\pi r^2$  is the area of the two circles

and  $2\pi rh$  is the area of the curved surface.

Thus Surface area =  $2\pi r(r + h)$ 



#### Example:

Calculate the total surface area of this cylinder.

#### Solution:

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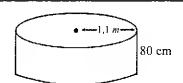
the

Surface area = 
$$2\pi r^2 + 2\pi rh$$

$$= 2 \times \pi \times (1,1)^2 + 2 \times \pi \times 1.1 \times 0.8$$

$$= 13,1318$$

$$= 13.13 \text{ m}^2$$



#### Volume of a Cylinder:

The formula for the volume of a solid cylinder is the same as the formula for the volume of a solid prism, that

$$V = Bh$$

where B is the area of the base and h is the height. Since, for a circular cylinder, the area B of the base is  $\pi r^2$ , this formula reduces in this case to

$$V = \pi r^2 /$$



- Q1. The surface area of a cube is 180, its volume is:
  - 125 (A)

**(B)** 30

(C) 164

- (D)  $30\sqrt{30}$
- Q2. The volume of a cube is 216, its surface area is:
  - (A) 64

216 (B)

(C) 25

- (D) 96
- Q3. A solid metal cube of side 5 inches is placed in a rectangular tank whose length, breadth and height are 5, 6 and 7 inches, respectively. What is the volume in cubic units, of water that the tank can now held?
  - 210 cubic units (A) `

**(B)** 85 cubic units

(C) 125 cubic units

- **(D)** 216 cubic units
- Q4. A cylinder and the cube have the same volume, if the height, h, of that cylinder is equal to the edge e of the cube, the radius of the cylinder is:

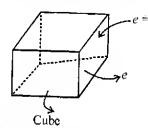
**(B)** 

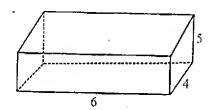
(D)

- Q5, If the height of a cylinder is double to its eireumference, what is the volume of the cylinder in terms of its circumference, C?
  - (A)

- Q6. Fatima and Maryium each roll a sheet of  $9\times18$  paper to form a cylinder. Fatima tapes the  $tw_0$ 9-inch edge together and Maryium tapes the two 18-inch edge together. Refer to this question and tell which of the following statement is true?
  - The volume of Fatima's cylinder is greater than Maryium's cylinder (A)
  - The volume of Fatima's cylinder is less than Maryium's cylinder **(B)**
  - The volume of Fatima's cylinder is equal to the Maryium's cylinder (C)
  - Both cylinders have the same-circumference **(D)**

Q7.





 $\mathbf{Q}_{i}^{r}$ 

Refer to the above figure, which of the following statement is true?

- Volume of the cube is less than the volume of the box
- Volume of the cube is greater than the volume of box **(B)**
- Volume of the cube is equal to the volume of box (C)
- The surface area of both cube and box are equal **(D)**



Q1. (D) :: Surface Area: A = 180

and Surface Area of the cube is  $6e^2 \Rightarrow 6e^2 = 180$ 

$$\Rightarrow e^2 = 180 + 6 \Rightarrow e^2 = 30 \Rightarrow e = \sqrt{30}$$

Therefore, edge =  $e = \sqrt{30}$ , hence its volume =  $(\sqrt{30})^3$ 

- $e^3 = 30\sqrt{30}$
- Q2. (B) The volume of the cube:  $e^3 = 216 \Rightarrow (e^3)^{1/3} = (216)^{1/3}$

$$\Rightarrow e = (6^3)^{1/3} \Rightarrow e = 6$$

Now Surface Area of a cube:  $A = 6e^2 \Rightarrow A = 6(6)^2$ 

$$\Rightarrow A = 216$$

Q3. (B) Volume of the tank =  $h \times b \times l = 5 \times 6 \times 7 = 210$  cubic units, but the volume of the solid cube,  $e^3 =$ 

 $\Rightarrow$   $e^3 = 125$  cubic units, therefore the tank can held 210 - 125 = 85 cubic unit of water.

Q4. (C) Volume of the cube  $= e^3$  and the

Volume of the cylinder =  $\pi r^2 h$ 

Since both are equal, therefore

$$\pi r^2 h = e^3$$
 also  $h = e$ 

$$\pi r^2 h = h^1 \Rightarrow \pi r^2 = h^2$$



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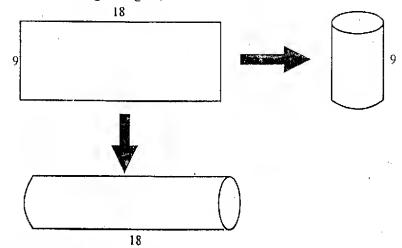
$$\Rightarrow r^2 = \frac{h^2}{\pi} \Rightarrow r = \boxed{\frac{h}{\sqrt{\pi}}}$$

Q5. (D) Since, volume of the cylinder =  $\pi r^2 h$ , according to the given condition h = 2C.

Now 
$$C = 2\pi r \Rightarrow r = \frac{C}{2\pi}$$
, therefore

$$V = \pi \left(\frac{C}{2\pi}\right)^2 \times 2C \Rightarrow V = \pi \left(\frac{C^2}{4\pi^2}\right) \times 2C$$
$$\Rightarrow V = \frac{C^3}{2\pi}$$

Q6. For sophistication, drawing the figure,



Now, the volume of the cylinder =  $\pi r^2 h$ 

Here, we know only height only, to calculate the radius of the cylinder, we proceed as The circumference of the cylinder made by Maryium is 9.

$$\therefore 2\pi r = 9 \Rightarrow r = \frac{9}{2\pi}$$

The circumference of the cylinder made by Fatima is 18.

$$\therefore 2\pi r = 18 \Rightarrow r = \frac{18}{2\pi} \Rightarrow r = \frac{9}{\pi}$$

Thus the volume of the cylinder made by Maryium is

$$V = \pi r^2 h \Rightarrow V = \pi \left(\frac{9}{2\pi}\right)^2 18 \Rightarrow V = \pi \times \frac{81}{4\pi^2} \times 18$$

$$\Rightarrow V = \frac{729}{2\pi}$$

and, volume of the cylinder made by Fatima is

$$V = \pi r^2 h \Rightarrow V = \pi \left(\frac{9}{\pi}\right)^2 \times 9 \Rightarrow V = \frac{729}{\pi}$$

Hence the volume of the cylinder made by Fatima is greater than the cylinder made by Maryium

**Q7. (B)** Volume of the cube :  $V_c = 5^3 = 125$ 

Volume of the cube :  $V_b = 4 \times 5 \times 6 = 120$ 

Thus the volume of the cube is greater than the volume of the box.

## Chapter 7

## COORDINATE GEOMETRY

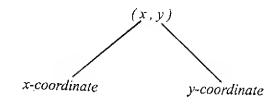
A French mathematician named Descartes invented a method of representing a pair of numbers as a point in a plane. The numbers are measured on a pair of axes which are at right angles to each other and which intersect

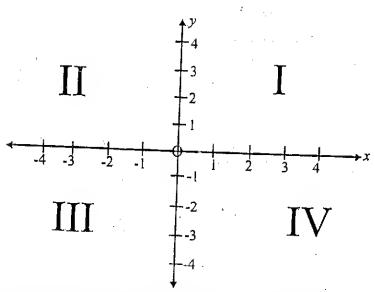
The plane is called the co-ordinate plane or the Cartesian plane.

#### Coordinates:

Coordinates are an ordered pairs of numbers. These ordered pairs give the position of a point using axes and an

The coordinates of any point P are (x, y), where





The figure above shows the (rectangular) coordinate plane. The horizontal line is ealled the x-axis and the perpendicular vertical line is called the y-axis. The point at which these two axis intersect, designated 0, is called the origin. The x-axis and y-axis divide the plane into four parts known as quadrants, I, II, III and IV, as

Since, the coordinates of any point P are (x, y). The first number is always 'across'. The across axis is the xaxis. So the first number is called the x-coordinate.

The second number is always 'up or down'. The 'up and down' axis is the y-axis. So the second number is

Thus, in a Cartesian plane, the two perpendicular distances of the point from these axes are called the coordinates of the point. The distance of the point from the y-axis is known as the x-eoordinate or the abscissa and that from the x-axis is known as the y-coordinate or ordinate of the point. Thus an order pair (3, 4) represents a point where abscissa is 3 and ordinate is 4.

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On (i)

(ii)

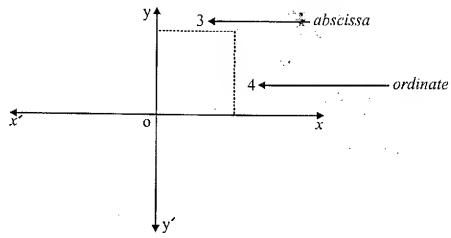
On t (iii)

(iv) Rem

(i) (ii)

(iii) . Exan

In the a (i.e., x -4), an



#### **Negative Coordinates:**

Coordinates can be positive or negative numbers. To plot or determine these points you must have both positive and negative numbers on the axes.

y  $\uparrow$ 

#### On the x-axis:

- (i) Values to the right of O are positive (+),
- (ii) Values to the left of O are negative (-).

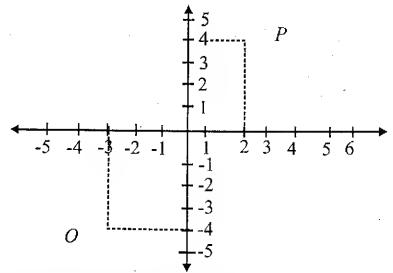
#### On the y-axis:

- (iii) Values above O are positive (+),
- (iv) Values below O are negative (-).

#### Remember

- (i) The coordinates of the origin are (0, 0).
- (ii) Any point on the x-axis has its ordinate zero.
- (iii) Any point on the y-axis has its abscissa zero.

#### Example 1:



In the above graph, the (x, y) coordinates of point P are (2, 4), it is because P is 2 units to the right of the y-axis (i.e., x = 2) and 4 units above the x-axis (i.e., y = 4). In the same way, the (x, y) coordinates of point Q are (-3, -4), and the origin Q has the coordinates (0, 0).

Column A

Column B

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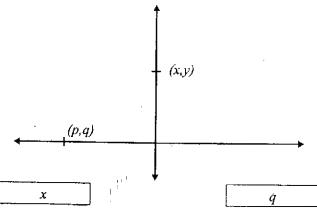
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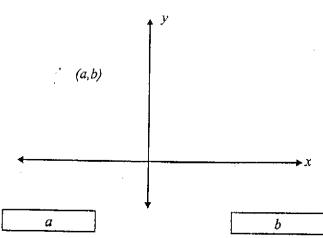
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Example 2:



Example 3:



Solution 2:

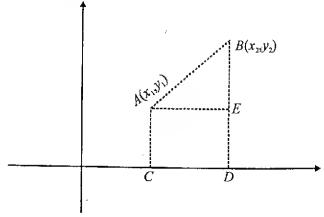
In the Cartesian plane, (p, q) lies on the x-axis, we know, on x-axis the y-coordinate of a point is zero, hence, q = 0. Similarly, on the y-axis, the x-coordinate of a point is zero. Now, because, point (x, y) lies on y-axis, hence x = 0. Thus, the correct answer is "=".

#### Solution 3:

In the second example, point (a, b) lies in the second quadrant and in second quadrant a is negative and b is positive, so a < b, is the correct answer. The answer is <.

# Distance between Any Two Points in A Cartesian Planc:

Consider two points A and B with coordinates  $(x_1, y_1)$  and  $(x_2, y_2)$ . Join A and B. Draw perpendicular



 $\overline{AC}$  and  $\overline{BD}$  on the x-axis from A and B respectively. Also from A, draw  $\overline{AE}$  perpendicular to  $\overline{BD}$ . Then from figure

$$AE = CD$$
 . .

$$= OD - OC$$

$$= x_2 - x_1$$

$$BE = BD - ED$$

$$= y_2 - y_1$$

In right-angled triangle ABE

$$AB^{2} = AE^{2} + BE^{2}$$

$$= (x_{2} - x_{1})^{2} + (y_{2} - y_{1})^{2}$$

$$AB = \sqrt{(x_{2} - x_{1})^{2} + (y_{2} - y_{1})^{2}}$$

Thus

The distance d between two points  $A(x_1, y_1)$  and  $B(x_2, y_2)$  is

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

The distance of a point P(x, y) from the origin is

$$OP = \sqrt{x^2 + y^2}$$

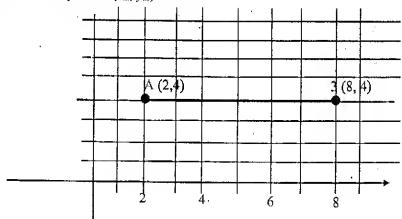
#### The Midpoint Formula

The coordinates  $(x_m, y_m)$  of the midpoint M of the segment whose endpoints are  $P(x_1, y_1)$  and  $P_2(x_2, y_2)$  are

$$x_m = \frac{x_1 + x_2}{2}$$
 and  $y_m = \frac{y_1 + y_2}{2}$ 

#### Example 4:

Find the coordinates of the midpoint  $M(x_m, y_m)$  of  $\overline{AB}$ .



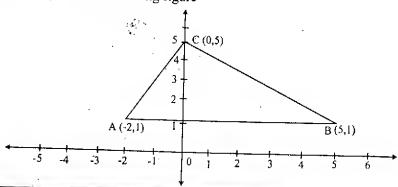
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#### Solution:

Since  $\overline{AB}$  is horizontal, the y-coordinate of any point on  $\overline{AB}$  is 4. Thus y coordinate of M is 4.

Now 
$$x_m = \frac{x_1 + x_2}{2}$$
$$= \frac{2 + 8}{2}$$
$$= \frac{10}{2}$$
$$= 5$$
$$\therefore M(x_m, y_m) = (5, 4)$$

Example 5-6 refer to a triangle in the following figure



#### Example 5:

What is the area of  $\triangle ABC$ ?

#### Solution:

The base of the triangle ABC is AB, and A(-2, 1), B(5, 1) lies on a same horizontal line so length of AB is,

$$AB = \sqrt{(5+2)^2 + (1-1)^2}$$

$$AB = \sqrt{7^2} = 7$$

Now, the altitude of the triangle is the distance between point C to line AB, Hence

Altitude = 
$$\sqrt{(0-0)^2 + (1-5)^2} = \sqrt{-4^2} = \sqrt{16}$$
  
= 4

Thus, the Area 
$$=\frac{1}{2}(Base)(Altitude)$$

$$=\frac{1}{2}(7)(4)$$

$$=(7)(2)$$

#### Example 6:

What is the perimeter of  $\triangle ABC$ ?

A. 
$$14 + \sqrt{41}$$

B. 
$$\sqrt{41} + 6\sqrt{5}$$

C. 
$$\sqrt{41} + 14\sqrt{5}$$

D. 
$$7 + \sqrt{41 + 2\sqrt{5}}$$

#### Solution:

The perimeter of the triangle ABC is AB + BC + CA.

From example, 5 AB = 7, Now we find BC and AC

$$BC = \sqrt{(0-5)^2 + (5-1)^2} = \sqrt{25+16} = \sqrt{41}$$

$$AC = \sqrt{(0+2)^2 + (5-1)^2} = \sqrt{4+16} = \sqrt{20} = 2\sqrt{5}$$

Hence .Perimeter = 
$$AB + BC + CA$$

$$=7+\sqrt{41}+2\sqrt{5}$$
 (D)

#### Slope of a Line:

The gradient is the slope of a line. A line that slopes upwards ▶ from left to right has a positive gradient, while a line that slopes downwards > from left to right has a negative gradient. In mathematics, the gradient or slope is represented by the letter m. Thus

Gradient (m) of a straight line =  $m = \frac{\text{Rise}}{\text{Run}} = \frac{\text{Difference in } y \text{ values}}{\text{Difference in } x \text{ values}}$ 

$$=\frac{y_2-y_1}{x_2-x_1}$$

#### Example 7:

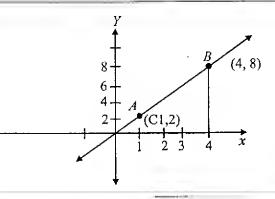
Find the gradient (slope) of line AB.

#### Solution:

Difference between y-coordinate Difference between x-coordinate

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$m = \frac{8-2}{4-1} = \frac{6}{3} = 2$$



#### Note:

- 1. The slope of any horizontal line is 0.
- 2. The slope of any vertical line is undefined.
- 3. Two non-vertical lines are parallel (||) if and only if they have the same slope.
- I wo non-vertical lines are perpendicular if and only if their slopes are negative reciprocals. 4. .

#### Column A

#### Column B

#### Example 8:

Line  $l_1$  passes through (1, 3) and (2, 4)

Line  $l_2$  is perpendicular to  $l_1$ 

The slope of 
$$l_1$$

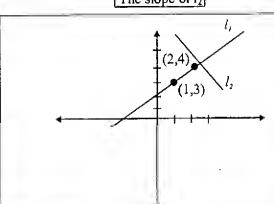
## The slope of $l_2$

#### Solution:

First we sketch the line  $l_1$ , and then draw line  $l_2$ perpendicular to  $l_2$ . The line  $l_1$  slopes upward so it has positive slope and the line  $l_2$  is sloped downward having negative slope, so

$$m_1 \geq m_2$$

where  $m_1$  is the slope of line  $l_1$  and  $m_2$  is the slope of line  $l_2$ .



# Multiple Choice Questions

- If A(-2, 3) and B(5, -1) are the endpoints of one side of a square ABCD, what is the area of the Q1., square?
  - 20 (A)

**(B)** 

- 35
- If A(3, 2) and B(7, 2) are two vertices of a rectangle, which of the following could not be the Q2. another vertices of that rectangle?
  - (A) (3, 7)

**(B)** (7, 3)

**(C)** (3, -7)

- **(D)** (-3, 7)
- Q3. A circle whose center is at (3, 4) passes through the origin. Which of the following points is not on the circle?
  - (A) (-1, 3)

**(B)** (-1, 1)

**(C)** (0, 0)

- **(D)** (7, 7)
- If a line passes through the points (x, y) and  $(\frac{1}{x}, y)$ , then its slope is Q4.
  - (A)

**(B)** 

 $(\mathbf{C}) \quad \frac{1-x^2}{x}$ 

- **(D)**
- Q5. The slope of the line passing through (-b, b) and (3b, a) is 1 and  $b \neq 0$ , which of the following is an expression for a in terms of b?
  - (A) 46

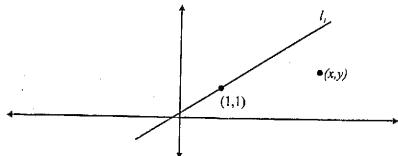
**(B)** 3*b* 

5*b* (C)

2b

**(E)** 46

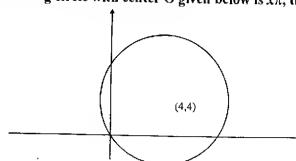
- **(D)**
- Q6. In the figure given below, x - y is



(A) positive

**(B)** negative

- less than zero ·(C)
- **(D)** less than or equal to zero
- **(E)** cannot find from the given information .
- If the area of the following circle with center O given below is  $x\pi$ , then x = ?Q7.



(A)  $28\pi$  **(B)**  $32\pi$ 

(C)  $9\pi$ 

**(D)**  $7\pi$  ıot

g is

Direction, Questions 8  $^-$  9 are referred to parallelogram ABCD, whose coordinates are A(-4, 2), B(-3, 6), C(4, 6), D(3, 2).

- Q8. What is the area of the parallelogram ABCD?
  - (A) 24

**(B)** 21

(C) 29

- **(D)** 28
- Q9. What is the perimeter of parallelogram ABCD?
  - (A)  $14 + \sqrt{17}$

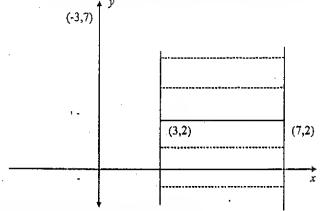
**(B)**  $16 + \sqrt{7}$ 

(C)  $2 + \sqrt{17}$ 

**(D)**  $2(7+\sqrt{17})$ 

Explanatory Answers

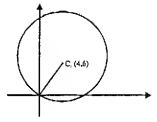
- Q1. (B)  $S = AB = \sqrt{(5+2)^2 + (-1-3)^2}$   $= \sqrt{(7)^2 + (-4)^2}$   $= \sqrt{49+16}$   $S = \sqrt{65}$   $S^2 = (\sqrt{65})(\sqrt{65})$  $S^2 = 65$
- Q2. (D) By drawing diagram as shown in the following figure, we find that any point whose x-coordinate is



3 or 7 could be another vertex, so (-3, 7) is not possible.

Q3. (A) First of all, we draw a diagram. Thus its radius is the distance from the origin to its center. By using distance formula

$$r = \sqrt{(3-0)^2 + (4-0)^2}$$
$$= \sqrt{9+16} = \sqrt{25} = 5$$



Since the distance of any point of a circle from the center of that circle is same, so any point whose distance is greater than 5 would not be on the circle. Now check these points given in the options:

A:  $(-1, 3) \Rightarrow r = \sqrt{(3+1)^2 + (4-3)^2} = \sqrt{16+1} = \sqrt{17}$  which is not equal to 5, hence (-1, 3) will not lie on the circle.

**B**: 
$$(-1, 1)r = \sqrt{(3+1)^2 + (4-1)^2} = \sqrt{16+9} = \sqrt{25} = 5$$

Since its distance from the center of the given circle is equal to the radius of the given circle, so given point will lie on the circle. Similarly, we can prove the options C, D & E.

Q4. (B) Slope of the given line =  $\frac{y_2 - y_1}{x_2 - x_1}$ 

Here 
$$y_2 = y$$
,  $y_1 = y$  and  $x_2 = \frac{1}{x}$ ,  $x_1 = x$ , thus

$$m = \frac{y - y}{\frac{1}{x} - x} = \frac{0}{\frac{1}{x} - x} = 0$$

Q5. (C) The slope of the line passing through two points  $(x_1, y_1)$  and  $(x_2, y_2)$  is given by

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

Here  $y_2 = a$ ,  $y_1 = b$  and  $x_2 = 3b$ ,  $x_1 = -b$ , m = 1

Hence,  $1 = \frac{a-b}{3b+b}$  $4b = a - b \Rightarrow a = 4b + b$  $\Rightarrow$  a = 5b

- Q6. Since the line l passes through origin (0, 0) and (1, 1), if any point (p, q), other than (1, 1) on the line *l*, then any point (p, r), below the point (p, q) will be less than (p, q). Thus  $a > b \Rightarrow a - b > 0$ 
  - Since the line segment joining (4, 4) and (0, 0) is the radius r of the circle  $r = \sqrt{(4-0)^2 + (4-0)^2} \Rightarrow r = \sqrt{16+16}$

$$\therefore r = \sqrt{(4-0)^2 + (4-0)^2} \Rightarrow r$$
$$\Rightarrow r = \sqrt{32} \Rightarrow r = 4\sqrt{2}$$

Since Area,  $A = \pi r^2$   $\Rightarrow A = \pi (4\sqrt{2})^2$  $\Rightarrow A = \pi(16(2))$  $\Rightarrow A = 32\pi$ 

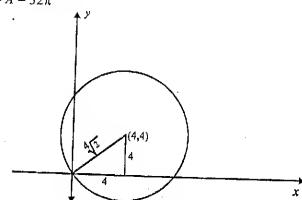
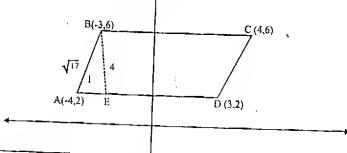


Diagram for solution question 8 and 9 is given below:



 $AB = \sqrt{(-4+3)^2 + (2-6)^2} = \sqrt{1+16} = \sqrt{17}$  $AE^{2} = AB^{2} - BE^{2} \Rightarrow AE^{2} = (\sqrt{17})^{2} - (4)^{2}$  $\Rightarrow AE^{2} = 1 \Rightarrow AE = 1$ 

 $AD = \sqrt{(-4-3)^2 + (2-2)^2} \Rightarrow AD = \sqrt{49+0} \Rightarrow AD = 7$ 

- Q8. (D) Since the base is 7 and the height is 4, thus Area =  $7 \times 4 = 28$  square unit.
- Q9. (D) Since AD and BC are each 7 and AB and CD both are equal to  $\sqrt{17}$ , thus the perimeter is  $7 + \sqrt{17} + 7 + \sqrt{17} = 14 + 2\sqrt{17} = 2(7 + \sqrt{17})$

#### COUNTING AND PROBABILITY

In mathematics, some questions begin with "How much, how many,......" In these type of questions you are being asked to count something: how many bananas Sonia bought, how many Rupees did Rizwan spend, how many pages did Fatima read, how many numbers are required to satisfy a certain formula, or how many ways are there to complete a given task. Usually these problems can be solved by simple arithmetic. Sometimes it helps to use basic probability rules, and Vann diagrams. In this chapter, we shall deal with such rules and counting principles that helps to solve such problems.

#### **Using Arithmetic to Count:**

This method is illustrated by the following three examples:

#### Example 1:

Osama bought some chocolates. If he entered the shop with Rs. 215 and left with Rs. 195, how much did the chocolates cost?

#### Example 2:

Usman was selling tickets for the magic show. One day he sold tickets numbered 98 through 111. How many tickets did he sell that day?

#### Example 3:

In a line outside the utility store, Hamza is the 29th person and Osama is the 38th person. How many people are there between Hamza and Osama?

#### Solution:

These questions require a simple subtraction. In example 1, Osama did spend (215 - 195 = 20) 20 on chocolates; in example 2, however, Usman sold 14 tickets; and in example 3, only 8 persons are on line between Hamza and Osama.

In example 1, we simply subtract the amount after purchasing and before purchasing. In example 2, you need to subtract and then add 1: 111 - 98 = 13 + 1 = 14. And in example 3, you need to subtract and then subtract 1 more: 38 - 29 = 9 - 1 = 8.

In these examples, the issue is that, whether or not the first and last numbers are included or excluded. From above examples, we find the following rules.

To find how many numbers there are between two numbers, apply following rules:

- 1. If exactly one of the endpoints is included, then subtract these values.
- 2. If both endpoints values is included, then subtract these values and add 1 in the answer.
- 3. If endpoints values are not included, then
  - (i) Subtract these values, and
  - (ii) Subtract 1 more from the answer.

#### The Counting Principle:

#### The Sum Rule

If a first task can be done in m ways and a second task in n ways, and if these tasks cannot be done at the same time, then there are m + n ways to do either task.

#### Example 1:

A student can choose a computer project from one of the three lists. The three lists contain 21, 13 and 17 possible projects, respectively. How many possible projects are there to choose from?

#### Solution:

The student can choose a project from the first list in 21 ways, from the second list in 13 ways, and from the first list in 17 ways. Hence there are 21 + 13 + 17 = 51 projects to choose from.

#### The Product Rule:

Suppose that a procedure can be broken down into two tasks. If there are m ways to do the first task and n ways to do the second task after the first task has been done, then there are  $m \times n$  ways to do the procedure.

The following examples illustrate how the product rule is used:

#### Example 1:

There are 28 computers in a computer center. Each computer has 22 parts. How many different parts to a computer in the center are there?

#### Solution:

The procedure of choosing a part consists of two tasks, first picking a computer and then picking a part on this computer. Since there are 28 ways to choose a computer and 22 ways to choose the part no matter which computer has been selected, the product rule shows that there are  $616 (28 \times 22)$  parts.

#### Example 2:

Sana has 6 different baskets in the basement. She is going to bring up 2 of them and placed 1 in her den and 1 in her bedroom. In how many ways can she choose which baskets go in each room?

#### Solution:

The first job was to pick 1 of the 6 baskets and place it in the bedroom. That could be done in 6 ways. The second job is to pick a second basket and place in the den. That could be done by choosing any of the remaining 5 baskets. So there are  $6 \times 5 = 30$  ways to place 2 of the baskets.

#### The Inclusion-Exclusion Principle:

When two tasks can be done at the same time, we cannot use the sum rule to count the number of ways to do one of the two tasks. Adding the number of ways to do each task leads to an overcount, since the ways to do both tasks are counted twice. To correctly count the number of ways to do one of the two tasks, we add the number of ways to do each of the two tasks and then subtract the number of ways to do both tasks. This technique is called the principle of inclusion-exclusion.

#### Permutations:

Each one of the total arrangements that can be made by taking some or all of a number of different objects is called permutation. This actually presents any arrangement of a set of objects in a definite order. Permutations of the set of letters a, b, c, d taken all at a time are abcd, acbd, bacd etc. An ordered arrangement of r elements of a set is called an r-permutation. For example, permutations of n = 4 letters a, b, c, d taken r = 2 at time are ab, ac, ad, bc, bd, ba, etc. Thus there are twelve permutation of four letters, taken two at a time.

The number of r-permutations of a set with n elements is denoted by  ${}^{n}p_{r}$  or P(n, r).

#### Note:

We can find  ${}^{n}p_{r}$  using the product rule.

#### Theorem:

The number of r-permutations of a set with n distinct elements is

$$^{n}p_{r}=n(n-1)(n-2).....(n-r+1)$$

#### Example 1:

How many different arrangements are there of the letters A, B, C, D and E?

A. 24

B. 20

C. 25

D. 120

#### Solution:

In this problem, the first job is to choose one of the five letters to write in the first position; there are 5 ways to complete that job. The second job is to choose one of the remaining 4 letters to write in the second position; there are 4 ways to complete that job. The third job is to choose one of the 3 remaining letters to write in the third position; there are 3 ways to complete that job. The fourth job is to choose one of the two remaining letters to write in the fourth position; there are 2 ways to complete that job. At last, the fifth job is to choose the only remaining letter and to write it.



#### **Using Permutation:**

The 5 letters can be written in

$${}^{5}P_{4} = 5(5-1)(5-2)(5-3)(5-4)$$
  
= 5 × 4 × 3 × 2 × 1  
= 120 ways

#### Example 2:

In how many different ways can 6 persons be seated on a bench?

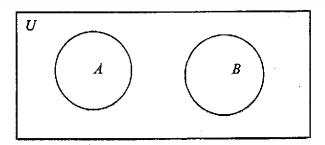
#### Solution:

Six persons can be seated in different position on a bench is

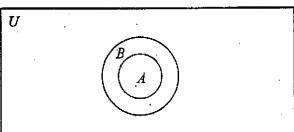
$$= 6 \times 5 \times 4 \times 3 \times 2 \times 1 = 720$$
 ways

#### Venn Diagrams:

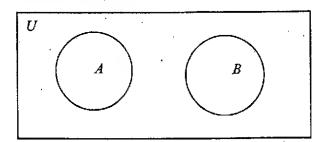
In a Venn diagram, a rectangular region represents a universal set and regions bounded by simple closed curves represent other sets, which are subsets of the universal set. In the following figure, the circular regions represents set A and set B and the remaining position of rectangle representing the universal Set U.



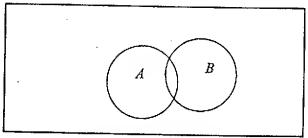
If  $A \subset B$ , then the circle representing A will be entirely within the circle representing B as shown in the following figure



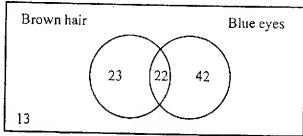
If A and B are disjoint, i.e., have no elements common, then the circle representing A will be separated from the circle representing B as shown in the following figure



However, if A and B are two arbitrary sets, then it is possible that some elements are in A but not in B, some are in B but not in A, some are in both A and B, and some are in neither A nor B; hence in general we represent A and B, as in following figure



Many verbal statements can be translated into equivalent statements about sets which can be determined by Vann diagrams. To illustrate this assume that department of Pharmacy of Punjab University has 100 students. The following diagram, which divides the rectangle into four regions, shows the distribution of these students in the brown hair and blue eyes.

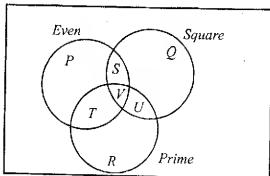


The 22 written in the part of the diagram where the two circles overlap represents the 22 students who have both brown hair and blue eyes. The 23 written in the circle on the right represents the 23 students who have brown hairs but not blue eyes, while the 42 written in the left circle represents the 42 students who have blue eyes but not brown hairs. At last, the 13 written in the rectangle outside the circles represents the 13 students who have neither brown hair nor blue eyes. The numbers in all four regions must add up to the total number of the students.

22 + 23 + 42 + 13 = 100. In this diagram, we see that, there are 64 students having blue eyes -22 who are also having brown hair and 42 not having brown hair. Similarly, there are 23 + 22 = 45 students having brown hair. Note that, if we add both brown hair and blue hair, then we find 64 + 45 = 109 students—more than the number of students in the department. That's because 22 names are on both lists and so have been counted twice. The number of students having brown hair and blue eyes are 109 - 22 = 87. Those 87 together with the 13 students who have neither brown hair nor blue eyes make up the total of 100.

#### Example:

If the integers from 1 through 25 are each placed in the following Venn diagram. Then identify the empty region.



A. Q only

B. Vonly

C. U and V only

D. R only

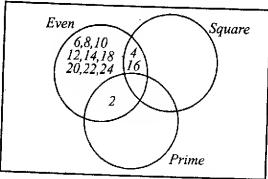
E. Q, V, U and R only

#### Solution:

Put each of the number from 1 through 25 in the appropriate region

Some





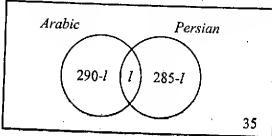
From above figure, we see that Q, V, U and R are empty regions. Hence the true choice is E.

#### Example:

There are 560 students of 10th class at Muslim High School, 290 of them study Arabic and 285 study Persian. If 35 students study neither language, how many study both?

#### Solution:

First of all, draw a Venn diagram. Let I represents the number of students who study both Persian and Arabic. Then the number of students who study only Arabic is 290 - l, and the number of



students who study only Persian is 285 - l.

The number of students who study at least one of the languages is 560 - 35 = 525, thus

$$525 = (290 - 1) + 1 + (285 - 1)$$

$$\Rightarrow 525 = 290 - l + l + 285 - l$$

$$\Rightarrow 525 = 575 - l \Rightarrow l = 575 - 525 \Rightarrow l = 50$$

Thus 50 students study both languages.

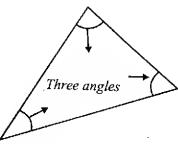
## Probability:

#### Definition:

Probability is the numerical evaluation of a chance that a particular event would occur.

Probability is about how likely something is to happen. We often use the word chance for probability.

Something always happen, we say they are certain to happen. For example, if you draw a triangle it has three sides and three angles. That's certainty!



Something will never happen. We say they are impossible. For example, if you roll an ordinary dice you will never get a 7 or 8. That's impossible.

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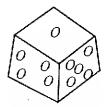
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Something are not certain, but not impossible either. They may or may not happen. For example, if you toss a coin it may land heads, or it may not.

#### Scale of Probability:

In mathematics when we talk about the probability of 'something' happening, we call the something an event. Probability is a measure of how likely an event is to happen. We use a number, not words, to describe its size. We can give a probability a number from 0 to 1.

Probability Scale 1
Impossible Certain

#### On this Probability Scale:

An event that is impossible is given a probability of 0. An event that is certain is given a probability of 1.

#### For example:

The probability that you get a 7 on an ordinary diee is 0, the probability that a triangle you draw will have three angles is 1.

All other probabilities on this scale are between 0 and 1. They must be less than 1. We write them as proper fractions or decimal fractions.

#### Remember:

In a proper fraction, the top number is smaller than the bottom.

To compare probabilities, we compare the sizes of the fractions. The less likely an event is to happen, the smaller the fraction. The more likely an event is to happen, the larger the friction.

#### Some Basic Definitions:

#### **Equally Likely Events:**

A set of events is said to be equally likely if none of them is expected to occur in preference to the other.

For example, when a fair coin is tossed, then occurrence of head or tail are equally likely events and there is no reason to expect a 'head' or a 'tail' in preference to the other.

#### **Exhaustive Events:**

A set of events is said to be exhaustive when a random experiment always results in the occurrence of at least one of them.

For example, if a die is thrown, then the events

$$E_1 = \{1, 2\}, E_2 = \{2, 3, 4\}$$

are not exhaustive as we cannot get 5 as outcome of the experiment which is not the member of any of the events  $E_1$  and  $E_2$ . While, if  $E_3 = \{1, 2, 3\}$  and  $E_2 = \{2, 4, 5, 6\}$ , then the set of events  $E_3$  and  $E_4$  is exhaustive.

#### Independent Events:

Two events are said to be independent, if the occurrence of one does not depend on the occurrence of the other.

For example, when a coin is tossed twice, the event of occurrence of head in the first throw and the event of occurrence of head in the second throw are independent events.

#### **Mutually Exclusive Events:**

A set of events is said to be mutually exclusive if occurrence of one of them precludes the occurrence of any of the remaining events.

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In other words, events  $E_1, E_2, \ldots, E_n$  are mutually exclusive if and if only

$$E_i \cap E_i = \emptyset \qquad (i \neq j)$$

#### Complement of An Event:

The complement of an event E, denoted by  $\overline{E}$  or E' or E', is the set of all sample points of the space other than the sample points in E.

For example, when a die is thrown, we get the sample space

$$S = \{1, 2, 3, 4, 5, 6\}$$

If 
$$E = \{1, 4, 5, 6\}$$
, then  $\overline{E} = \{2, 3\}$ 

It is noted that  $E \cup \overline{E} = S$ 

#### Calculating Probabilities:

When all the outcomes of an activity are equally likely, you can calculate the probability of an event happening.

Probability of an event =  $\frac{\text{Number of favourable outcomes for that event}}{T}$ Total number of possible outcomes

This is sometimes called the probability fraction.

To calculate the probability of an event, you may need to list all the outcomes and the favourable outcomes Lust,

#### Note:

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Outcomes which give the 'event' you are interested in are called favourable outcomes for that event, and, outcomes which have an equal chance of happening are called equally likely outcomes.

Sadaf throw an ordinary dice. Write down the probability that she gets

a) a four b) more than two c) a seven

Sample space: Possible outcomes =  $\{1, 2, 3, 4, 5, 6\}$ 

Total number of possible outcomes = 6

Event: get a four

Favourable outcome: 4

Number of favourable outcomes = I

Probability of getting a  $4 = \frac{1}{6}$ 

Event: get more than two

Favourable outcomes: 3, 4, 5, 6

Number of favourable outcomes = 4

Probability of getting more than  $2 = \frac{4}{6} = \frac{2}{3}$ 

Event: 'get a seven'

No. of favourable outcomes = 0

Probability of getting a seven  $= \frac{0}{6} = 0$ 

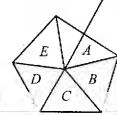
#### Example:

This spinner is made from a regular pentagon. When Fatima spins it once what is the probability that she get

- a) the letter B
- b) the vowel
- c) a consonant
- d) the letter F

#### Solution:

Sample space: Possible outcomes  $= (A P_1)$ 



C, D, E

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#### 212

# NTS Guide SECTION - 1: QUANTITATIVE ABILITY

Total number of possible outcomes = 5

a) Event: 'get a letter B'

Favourable outcomes = B

No. of favourable outcomes = 1

Probability of favourable outcomes =  $\frac{1}{5}$ 

b) Event: 'get a vowel'

Favourable outcomes = A, E

No. of favourable outcomes = 2

Probability of favourable outcomes =  $\frac{2}{5}$ 

c) Event: 'get a consonant'

Favourable outcomes: B, C, D

No. of favourable outcomes: 3

Probability of favourable outcomes =  $\frac{3}{5}$ 

d) Event: 'get a letter F'

Favourable outcomes: 0

Probability of favourable outcomes  $=\frac{0}{5}=0$ 

## Some Important Results on Probability:

- 1.  $0 \le P(E) \le 1$ , i.e., the probability of occurrence of an event is a number laying between 0 and 1.
- 2.  $P(\phi) = 0$ , i.e., probability of occurrence of an impossible event is zero.
- 3. P(S) = 1, i.e., probability of occurrence of a sure event is 1.
- 4.  $P(\overline{E}) = 1 P(E)$ , where  $\overline{E}$  is the event that will not occur.
- 5.  $P(\overline{E}) + P(E) = 1$
- 6. If A and B are mutually exclusive events, then

$$P(A \cup B) = P(A) + P(B)$$

#### **Product Rule:**

When more than one event occurs (e.g., tossing 2 coins, planting 5 seeds, choosing 3 people, throwing 2 die), multiply the probabilities together.

$$P(AB) = P(A) \cdot P(B)$$

## Tree Diagrams:

When using the product rule there may be more than one possible result. For example, the result when tossing two coins could be HT or TH (Head / tail or Tail / head).

When there is more than one possible result we add them together

$$P(A \text{ or } B) = P(A) + P(B)$$

This is called the additional rule of probability. A tree diagram helps to list all the possible  $\frac{1}{2}$  outcomes. Tree diagrams combine the addition and product rules.

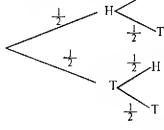
#### Example 1:

If 2 coins are tossed, find the probability of tossing a head and a tail.

#### Solution:

$$P(\text{head or tail}) = P(HT) + P(TH)$$

$$= \left(\frac{1}{2} \times \frac{1}{2}\right) + \left(\frac{1}{2} \times \frac{1}{2}\right)$$
$$= \frac{1}{4} + \frac{1}{4}$$
$$= \frac{1}{2}$$



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Solut First,

a) P

**b**) *P* 

Q1.

Q2.

Q3.

Q4.

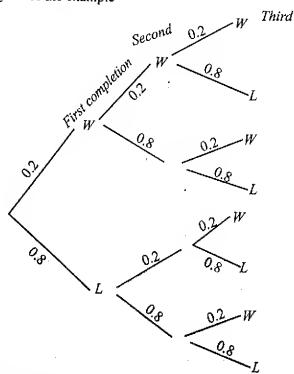
#### Example 2:

Fahad has probability of 0.2 of winning a prize in a competition. If he enters 3 competitions, find the probability of his winning:

- a) 2 competition
- b) at least 1 competition

#### Solution:

First, we construct a tree diagram of the example



a) Probability of losing = 1 - 0.2 = 0.8

P(2W) = P(WWL) + P(WLW) + P(LWW)

 $= (0.2 \times 0.2 \times 0.8) + (0.2 \times 0.8 \times 0.2) + (0.8 \times 0.2 \times 0.2)$ 

= 0.032 + 0.032 + 0.032

= 0.096

b) P(at least one W) = 1 - P(LLL)

 $=1-(0.8\times0.8\times0.8)$ 

= 1 - 0.512

= 0.488

# Multiple Choice Questions (MCQs)

Q1. Ayesha completed questions 4 – 18 of a mathematics exercise in 30 minutes. At this rate, how long, in minutes, will it take her to complete questions 27 – 55?

(A) 59

(B) 29

(C) 30

- **(D)** 58
- O2. Munir was born on August 14, 1934 and died on February 28, 1999. What was his age, in years, at the time of his death?
  - (A) 64

(B) 65

(C) 66

- $(\mathbf{D})$  68
- Q3. How many three-digit number have only even digits?
  - (A) 48

(B) 58

(C) 500

**(D)** 300

There are 28 players in a college cricket team. What is the probability that at least 3 of them

5 2 die),

tossing

ŀ

have their birthday in the same month?

**(A)** 0

(B)  $\frac{1}{5}$ 

(C) 1

**(D)**  $\frac{1}{2}$ 

Q5. A bag has 7 marbles, one of each of colours, green, blue, brown, yellow, red, white and pink, limarbles are removed from the bag, what is the probability that the red one was removed?

 $(\mathbf{A}) \quad \frac{1}{7}$ 

(B)  $\frac{4}{3}$ 

(C)  $\frac{2}{7}$ 

**(D)**  $\frac{6}{7}$ 

Q6. A bag contains 20 marbles: 6 green, 10 brown, and 4 white. If one marble is removed randomly, what is the minimum number that must be removed to be certain that you have at least 2 marbles of each colour

(A) 16

**(B)** 18

(C) 10

(D) 15

Q7. In a squash tournament that has 75 entrants, a player is eliminated whenever he loses a match. How many matches will be played in the entire tournament?

(A) 74

(B) 18

(C) 34

(D) 36

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# Explanatory Answers

Q1. (D) Ayesha completed 18-4+1=15 mathematics exercises in 30 minutes. It means that she complete one exercise every 2 minutes. Thus, to complete 55-27+1=29 questions would take  $29 \times 2=58$  minutes.

Q2. (A) Munir's last birthday was August 1998, when he turned 1998 - 1934 = 64.

Q3. (A) We use counting principle to solve this problem. The first digit can be chosen in any 3 ways (2, 4, 6) whereas the second, third can be chosen in any 4 ways (0, 2, 4, 6). Therefore the total number of 4 digit numbers all of whose digits are even is  $3 \times 4 \times 4 = 48$ .

Q4. (C) Suppose, there were no month in which at least 3 players had a birthday, then each month would have the birthdays of at most 2 players. But it is not possible. Now, if there were two birthdays in January, 2 in February, ..... and 2 in December, that would be 24 players only. Now, it is sure that with more than 24 players, (28 given) at least one month will have 3 or more birthdays. This is the sure event. The probability of the sure event is 1. Hence C is the correct choice.

Q5. (D) It is an equally likely event, any one of the 7 marbles will be the one that is not removed, so the probability that red one is left is  $\frac{1}{7}$  and the probability that it is removed is  $\left(1 - \frac{1}{7}\right) = \frac{6}{7}$ .

Q6. (B) You might have a chance to remove 10 brown ones in a row, followed by all 6 green ones. At that point you have removed 16 marbles, and you still wouldn't have even 1 white one. Now, the next two marbles must both be white. Hence the answer is 16 + 2 = 18.

Q7. (A) Since the winner never loses and the other 74 players each lose once. Since each match has exactly one loser, there must be 74 matches.

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# INTERPRETATION OF DATA

The Mathematical Reasoning section also include few questions about tables, charts and graphs. In these type of questions, you should know how to.

- Read and understand information that is given.
- Calculate, analyze and apply the information given. 2.
- Manipulating and predicting some future trends. 3.

Two types of questions are asked based on the same set of data.

- The first question is quite simple and easy. It requires only that you read the facts or information in the
- The second question is usually somewhat difficult, in which you are asked questions about Interpret, manipulate or predict data.

Let's start by looking at a pictogram.

#### Pictograms:

A pictograms uses simple symbols or pictures to show data. Pictograms gives you a quick impression of the

It is quite easy to compare data in a pictograms. In pictogram, you just compare how many pictures each item

#### Remember

When you look at a pictogram.

- Read the title carefully, it tells you what the pictogram is about. (i)
- (ii) Read and understand the key, the key shows you what each little picture stands for

In the following pietogram

Title → Trees in National Park

= 5  tree	← Key
3 1100	Key Key

Oak	學學學學
Pine	***
Birch	李李泰泰泰
Cypress	4
Sycamore	李泰泰

Each picture stands for 5 pieces of data.

#### Example 1:

What is the total number of trees in National Park.

#### Solution:

Just read the number of trees and multiply them by 5 i.e.,  $16 \times 5 = 80$ 

#### Example 2:

What percent of oak trees with respect to other trees in the park?

#### Solution:

There are,  $4 \times 5 = 20$ , trees of oak in the park and total number of trees is  $16 \times 5 = 80$ 

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The %age of each oak trees in the park =  $\frac{20}{80} \times 100 = 25\%$ 

# Number of Students Enrolled in M.A. (Languages) In Puniab University in 2005

AM A dujub Chiversity in 2005							
Urdu	Ť	•	•	t	İ	ŧ	
English	•	- #	İ	t			
Punjabi	İ	ŧ	ŧ	•	ŧ	ŧ	†
Arabic	Ŷ	ŧ	ŧ	ŧ	İ		
Persian	t	ŧ	ŧ				
Hindi	Ť	•					
Others	İ	ŧ	ŧ	ŧ	İ	ŧ	

Examples 3-5 refer to the above graph. Each † represents 30 students.

#### Example 3:

What is the total number of students enrolled language classes in Punjab University?

#### Solution:

Just read the pictogram and multiply the figure by 30,

$$33 \times 30 = 990$$

#### Example 4:

What is the average (Arithmetic Mean) number of students studying each language, if "other" category includes three languages.

#### Solution:

Total number of students 
$$= 33 \times 30 = 990$$
  
No. of languages  $= 6 + 3 = 9$   
Average  $= 990 \div 9$   
 $= 110$ 

#### Example 5:

If the number of students studying English next year is the same as the number taking Arabic this year, by what percent will the number of students taking English increase?

#### Solution:

The number of students taking English next year = number of students taking Arabic this year = 150

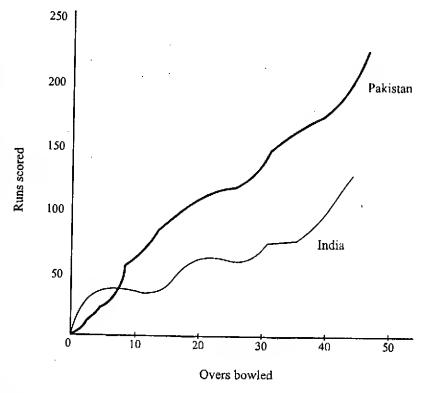
Increment = 
$$150 - 120 = 30$$
  
%age increase =  $\frac{30}{120} \times 100 = 25\%$ 

#### Line Graphs:

A line graph specifies how one or more quantities change over time. These types of graphs appear on the television screen during one-day cricket matches. The graph shows the accumulation of runs by each team as the match progresses. In this graph, Pakistan have already finished batting. India is still batting.

From graph, many questions could be asked. Here are some





Example 6:

How many scores did Pakistan score in his innings?

The solid line in the graph represents Pakistan inning. You can see that at the end of 50 overs the grey line is at 250.

Hence, Answer is 250

Example 7:

How many runs have India scored so far?

Solution:

India have scored 125 in 40 overs.

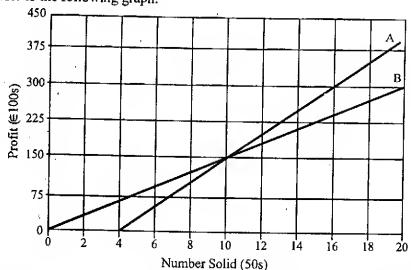
Example 8:

How many runs had Pakistan scored at the same stage in their innings?

Solution:

175

Examples 9 - 11 refer to the following graph.



A firm produces 2 products. Product A makes a profit only when more than 200 items are sold; after that a

steady profit is made. Product B makes a steady profit of  $\in$  10 on each item. Use the above graph to solve the following examples.

#### Example 9:

What is the profit for selling 1000 items of A?

#### Solution:

Since the product A starts its profit when more than 200 items have been sold, thus its profit is  $= 300 \times 100 = 30,000 €$ 

#### Example 10:

What does the profitability of A reach that of B?

#### Solution:

When 500 items of A are sold.

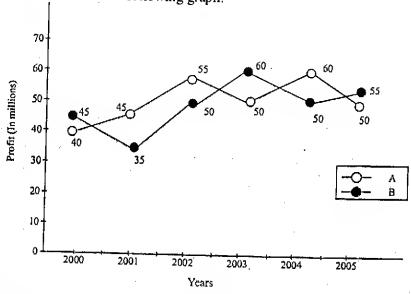
#### Example 11:

What is the profit from selling 800 items of B?

#### Solution:

€ 230,00

Directions: Examples 12-14 refer to the following graph:



#### Example 11:

Firm  $\hat{A}$  spent 3,50,000 in the year 2002. What is the income of Firm A in that year?

**A.** 15,42,500

B. 20,00,000

C. 15,25,000

**D.** 90,00,000

#### Solution: D

Profit of firm A in 2002 is 60,00,000

Income = Profit + Expenditure =3,50,000+55,00,000=900000

#### Example 12:

If the expenditure of both the firms A and B in the year 2004 was equivalent, then what was the ratio between the income of firm A to firm B?

A. 15:6

**B**. 6 : 15

C.6:5

**D.** 16:5

#### Solution: C

Let X be the expenditure of the firm A, since expenditure of the firms A and B are equivalent, then set the ratio

Firm A Firm B

$$X + 60,00,000$$
 $\Rightarrow x + 60,00,000 : x + 50,00,000 \Rightarrow \text{ ratio is }; 6:5$ 

#### Example 13:

In which of the following years was the maximum percentage of growth/decline with respect to the previous

years in case of company B?

A. 2000 - 2001

B.2001 - 2002

C. 2002 - 2003

D. 2003 - 2004

Solution: Pr

Profit in 2000 = 450000

Profit in 2001 = 350000

Decline = 450000 - 350000 = 100000

$$= \frac{100000}{350000} \times 100 = 29\%.(approx.)$$

#### **Bar Charts:**

A bar chart uses bars, side by side, to display data. The bars can go up or across the page. The length of a bar stands for the size of the data it shows. This makes the data easy to compare. Just compare the lengths of the bar.

#### Reading Bar Charts:

To read information from bar charts, here are some points to remember:

#### ■ Title

Make sure that you know what the bar chart is about.

#### ■ Axes

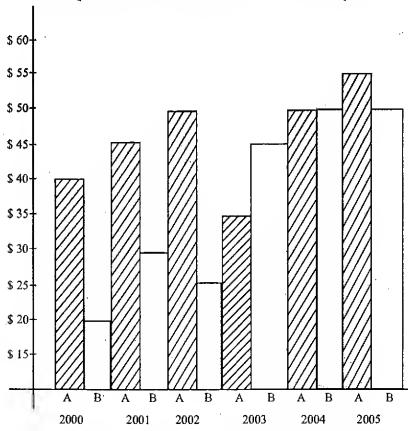
Carefully, check the labels on the axes.

#### ■ Scale

Carefully, look at the scale on the number line.

Directions: Examples 14 - 18 refer to the following graph.

#### Price per share of Stocks A and B on June 5 of 6 years



#### Example 14:

What is the difference, in dollars, of a share of stock A, between the highest and lowest value?

A. \$10

B. \$15

C. \$20

D. \$25

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ous

#### Solution:

According to the bar graph, the highest value of the share of stock A was \$55 in 2005 and the lowest value the share of stock A was \$35 in 2003. Thus

Difference = 
$$55 - 35 = $20$$
. (C)

#### Example 15:

In which year, there was the greatest difference between the values of the share of the stock A and a share of

#### Solution:

According to the bar chart, clearly in 2002. There is greatest difference between the share of stock A and B.

#### Example 16:

In which year, the ratio of the value of a share of stock A to the value of a share of stock B the greatest?

Solution: According to the bar chart, period from 2003 to 2005, the values of the shares of two stocks are very close, so we neglect these years. Now, there is a greatest difference between the shares of stock A and B in 2002, which is  $50:25 \Rightarrow 2:1$ .

Answer is option A.

#### Example 17:

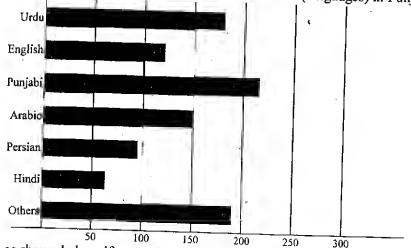
n which year was the percent increase in the value of a share of stock B the greatest?

iolution: According to the bar chart, the gradient of the line emerging in case of stock B in 2002 is the

#### lote:

1 a bar graph, the taller the bar, the greatest is the value of the quantity.

he following bar graph shows a numbers of students enrolled in M.A.(languages) in Punjab University.



is is a same graph as shown below, if we replaced bars with symbols.

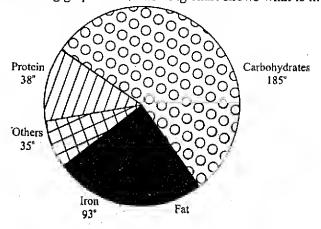
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Punjabi	Ť	İ	İ	İ	İ	Ť	†			···	
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Others	÷	•	•	i	•	i			 		

#### Pie Chart:

A pie chart is a circular diagram used to display data. It shows how the data are divided into group, so it looks like a pie cut into slices.

Example 17-18 refer to the following graph. The following chart shows what is in cereal.



#### Example 17:

Calculate the angle for fat on the diagram.

Solution: 
$$360^{\circ} - 185^{\circ} - 37^{\circ} - 35^{\circ} - 93^{\circ} = 10^{\circ}$$

#### Example 18:

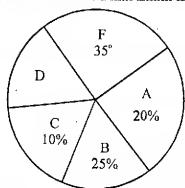
An average 'serving' of this cereal weights 45g. How much protein is in this?

Solution: 
$$\frac{37}{360}$$
 of 45 g = 45  $\times \frac{37}{360}$  = 4.625 g

# Multiple Choice Questions (MCQs)

Direction: Question 1-2 refer to the following graph.

Grades achieved on the Final Exam in Physics.



Q1. If 250 students took the exam, how many earned grades of D?

0

Q9

- (A) 35
- **(C)** 10

- **(B)** 25.
- **(D)** 29
- If 500 students took the exam, how many earned the grades of C? Q2.
  - (A) 50

(B) 20

(C) 35

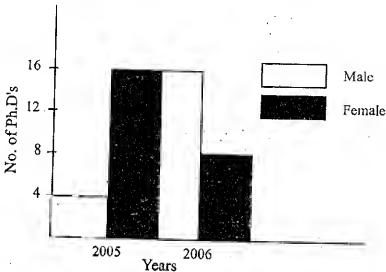
- **(D)** 10
- What percent of the students who failed the exam would have had to pass it, in order for percent Q3. of students passing the exam to be at least 77% out of 500?
  - (A) 15%

(B) 21%

(C) 23%

(D) 27%

Direction: The following bar chart shows the number of male and female who earned Ph.D's in physics at Punjab University in 2005 and 2006:



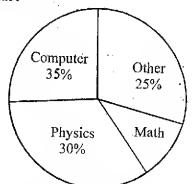
- From 2005 to 2006 the number of male earning Ph.D.'s increased by 5%, and the number of Q4. female earning Ph.D's decreased by t%. What is the value of s-t?
  - (A) 225 (C) 275

200

250

**(D)** 

Q5. Refer to the following pie chart

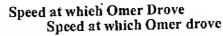


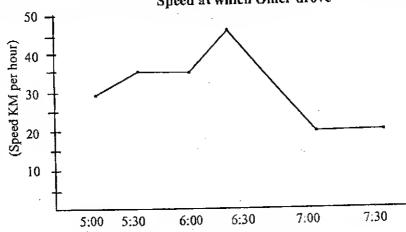
every student at Crescent High School is taking exactly one science subject. This distribution has been illustration in above circular diagram. If the "other" category in order of number of students taking each subject, consists of biology, geology and astronomy. Then which of the following statement is true?

- Number of students taking math is equal to the number of students taking astronomy. (A) **(B)**
- Number of students taking math is less than the number of students taking astronomy. (C)
- Number of students taking math is greater than the number of students taking astronomy.
- Cannot find from the given information. (D)

Direction: Questions 6 - 8 refer to the following graph.







Time Q6. How far, in KM, did Omer drive between 5 : 30 and 6 : 00?

(A) 20

**(B)**  $17\frac{1}{2}$ 

(C) 35

**(D)**  $12\frac{1}{2}$ 

Q7. What was Omer's average speed, in KM per hour, between 5:30 to 6:30?

(A) 25.25

**(B)** 36.5

(C) 42.5

**(D)** 35

Q8. For what percent of time was Omer driving at 35 km per hour or faster?

(A) 35

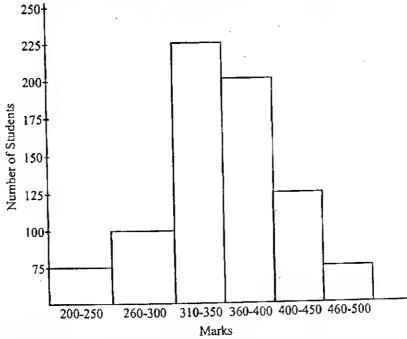
 $(\mathbf{B})$  25

(C) 27

**(D)** 50

Question 9-11 refer to the following graph.

Marks obtained by the students in Admission Test at Central Model High School



Q9. How many students took the admission test?

(A) 400

**(B)** 375

(C) 600

**(D)** 800

as of

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he

**Q7** 

Q8.

Q9.

Q10

Q11

Q10. What percent of the students had scored of less than 400?

(A) 50

**(B)** 75

(C) 25

(D) 65

Q11. How many candidates had scored between 250 to 350?

(A) 325

(B) 225

- (C) 125
- (D) cannot be exactly determined from the given information

Explanatory Answers

Q1. (B) In the given pie diagram

$$A\% + B\% + C\% + D\% + F\% = 100\%$$

$$20\% + 25\% + 10\% + D\% + 35\% = 100\%$$

$$\Rightarrow$$
 90% + D% = 100%

Now, 10% of 250 is = 
$$250 \times \frac{10}{100} = 25$$
.

**Q2.** (A) 
$$10\%$$
 of  $500 = 500 \times \frac{10}{100} = 50$ .

Q3. No. of passed students = 
$$500 \times \frac{77}{100} = 385$$
.

Thus for the passing rate to have been at least 77%, no more than 115 students, which is 23% of 500.

Q4. (D) No. of male students in 2005 = 4

No. of male students in 2006 = 16

Increase = 
$$16 - 4 = 12$$

% Increase 
$$=\frac{12}{4} \times 100\% = 300\%$$

$$\Rightarrow s = 300$$

During this period, the number of female students fell from 16 to 8, a decrease of 8.

$$\therefore \text{ %age decrease } = \frac{8}{16} \times 100\% = 50\%$$

$$t = 50$$

$$s - t = 300 - 50$$

$$= 250$$

Q5. (B) Let m = number of students taking math

Then:

$$25\% + 35\% + 30\% + m\% = 100\%$$

$$\Rightarrow$$
 90% +  $m\%$  = 100%

$$\Rightarrow$$
  $m\% = 10\% \Rightarrow m = 10$ 

which is less than the number of students taking astronomy.

Q6. (B) Since Omer is driving at constant rate 35 km/hour during. 5:30 to 6:00. Thus in half hour he drove

$$\frac{1}{2} \times 35 = 17\frac{1}{2} \,\mathrm{km}$$

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Q7. (D) From the graph, we see that, clearly from 5:30 to 6:00 Omer's average speed was clearly 35 km/hour, and from 6:00 to 6:30 Omer's speed steadily increased from 35 to 40 km/hour, so during 6:00 to 6:30 his average speed was  $\frac{35+40}{2} = \frac{75}{2} = 37.5$  km/hour.

Thus, in the given hour, his average speed was

$$\frac{37.5+35}{2}$$
 = 36.25 km/h

Q8. (D) From the graph, we see that from 5:30 to 6:45  $\left(1\frac{1}{2}\text{ hour}\right)$  the car is driven 35 or more than 35 km/hour which is half time of the total time (5:00 to 7:30)  $2\frac{1}{2}$  hours.

Hence, the answer is 50%.

Q9. (D) Just add the number of candidates by reading the graph carefully

$$75 + 100 + 225 + 200 + 125 + 75 = 800$$
.

Q10.(B) Number of students who scored less than 400

$$= 75 + 100 + 225 + 200 = 600.$$

Thus, 600 students had scored below or equal to 400 out of 800 candidates. Hence

$$\frac{600}{800} \times 100 = 75\%$$

Q11.(D) We cannot find exact number of students who scored between 250 to 350, because in every interval (260 - 300, 200, 250, etc.) every lower term is included in the previous term.

\*\*\*\*\*\*\*

**5**00.



Each analytical reasoning question is designed to test the analytical skills. Usually, each logical reasoning question is a logical puzzle, based on given conditions. These questions have only one correct answer, which is asked to be selected.

Analytical reasoning questions consist of groups of four or five questions. At begging, a short passage followed by a set of conditions is given. Sometimes, graphs and tables are given instead of passage. To understand this type of questions, we define some logical terms and their applications with examples.

#### Preposition:

A declarative statement which may be true or false but not both is called a preposition. For example, the statement x = y can be either true or false and there could not be any other possibility.

#### Symbols Used in Logic:

Capital letters are used to represent specific statements.

#### For Example:

A: A triangle has four angles.

B:  $\sqrt{17}$  is an irrational number.

C: 20 + 18 = 36

Solution: B is true; A and C are false.

Lower case letters, such as p, q are used to refer the preposition that are not specific. The following table is a brief list of the symbols which can be used:

Symbol	Meaning	Expression	How to read
~	not	~p	not p; negation of p
Λ ,	and	$p \wedge q$	p and $q$
V	or .	$p \vee q$	p or q
<b>→</b>	lfthen, implies	$p \rightarrow q$	If p then q p implies q
$\leftrightarrow$	If and only if is equivalent to	$p \leftrightarrow q$	p if and only if $q$ $p$ is equivalent to $q$

#### Explanation:

#### 1. Negation:

The negation of a statement has the opposite truth value of the statement. The symbol for negation is  $\sim$ , thus,  $\sim p$  is read: "not p", "the negation of p" or "it is false that p". The adjoining table called the truth table, gives the possible truth values of p and  $\sim p$ . Thus



p	~p
Т	F
F	T

The negation of true statement is a false statement.

The negation of false statement is a true statement.

#### 2. Conjunction:

Conjunction of two statements p and q is denoted by  $p \land q$  (p and q) and it is considered to be true only if both of its components are true.

#### 3. Disjunction:

Disjunction of p and q is p or q. It is symbolically written  $p \vee q$ . The disjunction  $p \vee q$  is considered to be true when at least one of the components p and q is true, and false if both components are false.

## 4. Implication or Conditional:

A compound statement of the form if p then q, also written p implies q, is called an implication or conditional. In the conditional statement below, p is called the antecedent or hypothesis, and q is called the consequent.

 $p \rightarrow q$ 

#### Examples:

- (i) If he works hard, then he will got through.
- (ii) If he wastes time, then he will fail.
- (iii) If a = 3, then  $a^2 = 9$ .
- (iv) If a = -3, then  $a^2 = 9$ .

#### 5. Biconditional:

If  $p \to q$  and  $q \to p$ , then the preposition p and q are said to be biconditional and shortly written as "p if and only if q". Symbolically, it is written as:

$$(p \to q) \land (q \to p) = p \to q$$

## Examples:

- (i) If an triangle is an isosceles triangle then, its two angles are congruent.
- (ii) If x = y, then ax = ay, where a, x and y are real numbers and  $a \ne 0$ .

**Note:**  $p \leftrightarrow q$  is true only when both p and q are true or both p and q are false.

## Model Example:

At All-Pakistan Weightlifting Championship, seven college athletes...M, N, O, P, Q, R and S... are being weighted. In order to make categories, the coach has given the following information:

- (i) Each athlete has not exactly the same weight as another athlete.
- (ii) R is heavier than S, but lighter than O.
- (iii) P is heavier than S.
- (iv) Both M and N are heavier than O.
- 1. Which of the following could not be true?
  - (A) M is the heaviest.
- (B) N is the heaviest.
- (C) P is the heaviest.
- (D) More than three athletes are heavier than R.
- (E) More than three athletes are lighter than R.
- 2. Which of the following, if true, would be sufficient to determine the lightest athlete?
  - (A) P is the heaviest.
- (B) P is lighter than R.
- (C) R is heavier than O.
- (D) Q is heavier than R.

<b>(E)</b>	Five candidates	are lighter	than M.
------------	-----------------	-------------	---------

- If Q is heavier than M, how many different ranking by weight, of the athletes are possible? 3.
  - (A)

**(B)** 

(C)

- **(D)**
- **(E)**
- If O is heavier than P, which of the following cannot be true?
  - P's weight is equal to the average of R's weight and S's weight. (A)
  - Q's weight is equal to the average of R's weight and S's weight. **(B)**
  - (C) P's weight is equal to the average of M's weight and N's weight.
  - **(D)** Q is the second lightest.

Solution: First of all, we decompose the given information, symbolically:

- $M \neq N \neq O \neq P \neq Q \neq R \neq S$ (i)
- (ii) R > S, R < O
- (iii) P > S
- (iv)  $M > O \land N > O$
- 1. (E) From above, we find the exact answer.

Take false option, "M is the heaviest"

From the given information,  $M \ge O$  and  $N \ge O$ , also  $R \le O$ . Thus option A must be true.

Now, take second option, "N is the heaviest"

From above conclusion, it may be possible that N is the heaviest.

Third option is, "P is the heaviest". We solve it symbolically:

$$R > S \land R < O \Longrightarrow S < R < O$$

also  $P > S \Rightarrow P \land R > S$ 

But 
$$M \land N > O \Rightarrow R < M \land N$$

From above, we cannot deduct that option "P is the heaviest" is wrong.

In third option, more than three athletes are heavier than R. Since, from the given information, R > SBut R < O also M > O and  $N > O \Rightarrow M, N > O$ .

 $\Rightarrow$  M, N, O > R. Because the information about Q not given, therefore, Q may be greater than R. This option may be true. Now we take the option E, according to this option, more than three athletes are lighter than R, Here we analyze it. Information (i), (ii) and (iv) can be written symbolically, as

M, N > O> R > S

Since, from above the three circled athletes are heavier than athlete R, and athlete R is heavier than only S. Suppose if the remaining two athletes P and Q are lighter than R. In this condition only three athletes are lighter than athlete R. Thus it is impossible that more than three athletes are lighter than R.

Thus the answer is "Choice E".

- 2. (D) The first option is "P is the heaviest". Suppose P is the heaviest, then P > S, also R > S
  - $\Rightarrow P > R$ , But  $R < O \Rightarrow P > O$  (given)
  - $\Rightarrow P > M$ , N, from this evaluation we cannot determine the lightest.

Take a look at the second option, "P is lighter than R", Suppose P is lighter than R, the  $R > P \land R > S$  $\Rightarrow R > P \land S$ .

This is also unsufficient to find the lightest weight.

In option C, R is heavier than Q, if R is heavier than Q, then, symbolically

$$R > Q \land R > S$$
  $O > R \Rightarrow O > R, Q, S$ 

Hence it is not possible to find the lightest weight. In option D, Q is heavier than R. If this is true, then

$$Q > R \land R > S \Rightarrow Q > R > S$$

But R < O, therefore, Q > O > R > S, also

$$\Rightarrow Q > M, N > O > R > S$$

$$\Rightarrow Q > M, N > O > R, P > S$$

Thus, we can find the lightest weight after accepting this option.

Hence, the correct choice is choice D.

3. (C) If Q is heavier than M, then

$$Q > M \Rightarrow Q > O$$

$$O > R \Rightarrow Q > O > R$$

$$R > S \Rightarrow Q > Q > R > S$$

Thus, the three categories are possible, which are

- (i) Q > O
- (ii) O > R
- (iii) R > S
- 4. If O is heavier than P, then according to the first option which says that, P's weight is equal to the average of R's weight and S's weight.

$$P > S \land O > P \Rightarrow O > S$$
, i.e.,  $O > P > S$  also  $R < O$ . But  $R > S \Rightarrow O > R > S$ 



#### Questions 1-3:

A chemist is preparing a nutriment using eight different vitamins and minerals...A, B, C, D, E, H, F (Ferric), and Z (Zinc). According to the recipes, the following requirements apply to the use of ingredients:

- (i) If B is used, both C and Z must also be used.
- (ii) E and H must always be used together.
- (iii) If C is used, at least two of A, B and F must also be used.
- (iv) C and H cannot be used together.
- (v) E, F and Z cannot all be used in a same nutrient.
- (vi) A, D and Z cannot all be used in the same nutriment.

#### **Question 1:**

- I. Which of the following is a suitable combination of vitantins and minerals for a nutriment?
  - $(A) \qquad A, B, C, F$
- **(B)** D, E, H, Z
- (C) A, D, E, Z
- (D) C, D, E, F
- (E) E, H, F, Z
- 2. Which of the following cannot be included in a nutriment that contains E?
  - (A) B

 $(\mathbf{B})$  D

(C) H

- $(\mathbf{D})$  F
- $(\mathbf{E})$  Z
- 3. By the addition of exactly one more mineral, which of the following could make an acceptable combination of vitamins and minerals?
  - (A) A, D, Z
- **(B)** B, H, E
- (C) C, D, H
- (D) C, E, Z
- (E) E, H, F

Questions 4-6: A railway track from Lahore to Islamabad consists of six main stations, P, Q, R, X, Y and Z. Trains run only according to the following condition:

- (i) From P to Q
- (ii) From Q to P and from Q to R
- (iii) From R to X
- (iv) From X to Q and from X to Y
- (v) From Z to P, from Z to Y and from Z to R.
- (vi) From Y to X.
- (vii) It is possible to transfer a station for another train.

r	<del></del> -				<del></del>				
23	0			NTS Guid	de SECT	ION - II: ANALYTICAL REA	SONING		Γ.
4.	The	e complete and acc	rurate listina o	f tha stations				ı	
	one	transfer, is:	muc usung o	ine stations	s from whi	ch it is possible to reach R w	ith exactly	1	
	(A)		<b>(B)</b>	P and $X$				- 1	L
_	(C)	<del>-</del>	(D)	X and $Z$	<b>(E)</b>	X, P and $Z$			Q
<i>5</i> .	The	greatest number o	f stations that	can be visite	d without v	isiting any station more than	once. is:	- 1	a
	(A) (C)		( <b>D</b> )	5					OI
6.		6	<b>(D)</b>	3	<b>(E)</b>	2			CC
Ü	(A)	trip which require  P to R	s greatest num		ers, is:				(i)
	(C)	Z to $Q$	(B) (D)	Q to $Y$	. <del></del>				(ii
7.	3, -		(D) declare that th	Z to R	(E)	Z to Y			(ii
				e principai vi lovers declari	rtae of the e that the r	dog is its general friendlines rincipal virtue of the cat is its	s towards		$\begin{cases} (iv) \\ (v) \end{cases}$
							у ресинат		(vi
	(A)	ch of the following	is true of the c	laims of both	li dogs and	cats lovers?	1		(vi
	(B)	Animals have n	of a sense to ur	iderstand hun	nan behavi	our,			11.
	(C)	Groups of anima	al lovers are fri	endly.		$\cdot$			
	(D)	Friendliness is a	and the second s		•				
	(E)	They apply the s							1
8.		Uncommon virti	ue of friendline	SS.			- 1		12.
	that p	erson's ninth birth ify, which is the be	iday, except the	at the positio the assertion	r be the sai n of the dig s made abo	old. If we per use this exan ne as the last two digits of th gits will be reversed. we.	e year of		
						digit of their birth years is gre			13.
	(B)	The generalization	on is applicable	only for thos	se birth yea	rs that do not end in two zeroe	es.		
	(C)	This example is	not best illustra	tion of the fa	ct.				
	<b>(D)</b>	*				n which the difference of the	last two		
	<b>(E)</b>	The generalizatio	n is valid only	for those birt	h years tha	t ends with 6			
electe gion quir	tions 9-1 ed from al econ- ements:	three different par	versity, Studer	nts of Econo	mics must	complete a total of twelve omics, environmental econom t the following course dist	courses ics, and ribution		
)	At leas	st six of the required	d twelve course	s must be fro	un the envi	ronmental economics.			
i)	110 104	at the of the tedi	ulfed twelve c	Olireec muset	ha funna	comparative economics and rome comparative economics.	cgional		QI. (
	The m require	inimum number o	of regional eco	onomics cou	rses requi	m comparative economics. red to fulfil the course distr	ibution		
	(A)	1	(77)	•					
	(C)	5	(B) 3 (D) 2		(ID)				
	If the s course, least:	student lias compl the possible group	eted six envir	anmontal ac		4 ourses and one regional eco oution requirements must inc	nomics Iude at		Q2. ( <i>i</i>
	(A)	One Environmenta	l Economics C	ourse .					
	<b>(B)</b>	Three Regional Ec						1 1	

(C)

One Regional Economics Course

Q3. **(**E)

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- (D) Two Comparative Economics Courses
- (E) Three Comparative Economics Courses

Questions 11-15: Six candidates.....Ali, Amin, Omer, Hamza, Saleem and Osama are being interviewed for a job. The interview will take place over four consecutive days, starting on Thursday. Each candidate will have only one interview. The day on which the different candidates will interview must confirm to the following conditions:

- (i) At least one interview will take place each day.
- (ii) No more than two interviews will take place on any day.
- (iii) No more than three interviews will take place on any two consecutive days.
- (iv) Ali's interview must take place on Saturday.
- (v) Amin's interview must take place on the same day with another interview.
- (vi) Saleem's interview must take place on the day before Osama's interview.
- (vii) Omer's interview must take place on a day after Hamza's interview.
- 11. If only one interview takes place on Thursday which candidate could have that interview?
  - (A) Ali

- (B) Amin
- (C) Omer
- (D) Saleem
- (E) Osama
- 12. If the director decides to take two interviews on Thursday and two on Sunday, how many candidates would be eligible to interview on Friday?
  - (A) 1

**(B)** 2

(C) 3

(D) 4

- (E) 5
- 13. If Hamza and Osama have their interviews on the same day which of the following must be true?
  - (A) Hamza's interview will take place on Thursday.
  - (B) Saleem's interview will take place on Friday.
  - (C) Amin's igraview will take place on Saturday.
  - (D) Osama's interview will take place on Saturday.
  - (E) Amin's interview will take place on Sunday.

# Explanatory Answers

Q1. (B) Take first option, which is A, B, C, B. By the first condition,  $B \to (C \land Z)$ . But D has not given, so this combination is not suitable. Now take the second combination, which is D, E, H, Z. This option is a correct choice, since it satisfies all the given conditions.

The third option is rejected due to the sixth condition. According to this condition, A, D and Z cannot be used altogether in a nutriment. Since H is not present with E, thus we reject option D due to second condition. The fourth condition is rejected due to fifth condition. So the correct answer is choice B.

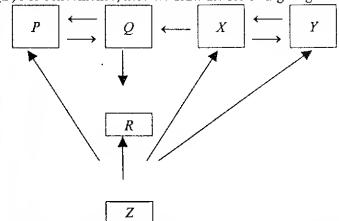
Q2. (A) If nutriment contains E, then according to second condition,  $E \leftrightarrow H$ . But according to fourth condition  $H \rightarrow \sim C$ .

If we include B in the nutriment, then according to first condition  $B \to (C \land Z)$  i.e., C and Z must also be used. But if we use C then H must be absent in the nutriment. But E and H must always be used together. Thus we cannot include B in the presence of E. The correct choice is option A.

Q3. (E) Since A, D and Z cannot all be used in a nutriment, so we reject option A. The option B is, B, H, E, Since, C and Z must also be used with B (first condition) so we reject option B. Since C and H cannot

be used together, so we reject option C. Since E and H must always be used together, so we reject option D. So the correct choice is option E. Which satisfies all the given conditions.

Q4. (B) For convenience, here we draw the following diagram:



It is clear from the diagram that from P to R, there is one transfer, but from Q to R, there is not any transfer, the track is direct. Thus, the option A is not possible. Now, from P to R these is only one transfer and same is the case from X to R. Thus option B is the correct choice.

Q5. (C) Here, the following list shows the track of trains that can be visited without visiting any station more than once:

$$R \rightarrow X$$

$$Q \rightarrow R$$

$$Z \rightarrow R$$

$$Z \rightarrow P$$

$$Z \rightarrow Y$$

$$Q \rightarrow X$$

The stations used in above tracks on

R, X, Q, Z, Y, P

Thus option (C) is the correct choice.

- Q6. (B) From  $P \rightarrow R$ , there is only one transfer, *i.e.*,  $P \rightarrow Q$ . From  $Q \rightarrow Y$ , there are two transfers, *i.e.*,  $Q \rightarrow R$  and  $R \rightarrow X$ . From Z to Q, there is only one transfer *i.e.*,  $Z \rightarrow P$ . From Z to R, there is not any transfer. At last, Z to Y there is not any transfer. Thus the correct choice is option B, *i.e.*, 2.
- Q7. (C) This question asks you to identify the main point of both dog and cat lovers. According to first option, animals have not a sense to understand human behaviour. Since animals have a great sense to understand human behaviour, like, love, anger, etc., so we reject this option. It is not sufficient that only the pet lovers should be friendly, the animals (cats, dogs etc.) should also be friendly. Thus, option B is not a the best choice. The best choice is option C, since it focusses upon the characteristic of animals and their lovers, which they require.
- Q8. (D) The given generalization is true only if the difference of the last two digits of birth year is 1. Suppose a man was born in 1959 and so in 1995, he was 36 years old. This is a same example as given, the only difference is the, difference of the last two digits of birth year which is not 1. Now, suppose that a man was born in 1956 and so in 1965 he was 9 years old. This is so because the difference of the last two digits of the birth year in 1 i.e., (6-5=1). Thus the correct answer is the option D.
- Q9. (D) Since at least five courses must be from comparative and regional economics, with at least one, but no more than three selected from comparative economics. Thus if we select three courses from comparative economics, we must select two courses from regional economics group. Thus the correct choice is option D.

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Q10(C) 
$$\frac{C}{6} = \frac{R}{6}$$
  
 $\frac{3}{3} + \frac{7}{7} + \frac{2}{2} = 12$ 

From above, we took 1 regional economics which is least. Thus if we take 3 from comparative and one Q(11).D Here first we assure that the requirement.

Q(11).D Here, first, we express the given conditions symbolically. Name of candidates Ali, Amin, Omer, Hamza, Saleem and Osama.

Days: Thu, Fri,

Each days condition: 1 o

1 or 2 interviews

2 consecutive days:

2 or 3 interviews

Ali's interview = Saturday

According to condition (iv), Ali's interview will take place on Saturday. According to condition (v), Amin's interview must take place on the same day, an another interview. Thus choices C and E are impossible. Since Omer's interview must take place on a day after Hamza's interview and Osama's interview must take place on a day after Saleem's interview, cannot take place on Thursday. Thus the correct choice is choice D.

Q(12). According to third condition, no more than three interviews will on any two consecutive days. Thus only one interview can take place on Friday. Therefore according to fifth condition, it cannot be Amin. Since Ali's interview is on Saturday. Thus, it cannot be Ali. Any of the other four candidates could be interviewed on Friday as indicated in the following points:

(i)	Thu	Fri.		
	Hamza/Saleem		Sat	Sun
A. 1		Omer	Ali	Amin/Osama
(ii)	Thu	Fri	Sat	Sun
	Amin/Saleem	Hamza		
(ili)	Thu		Ali	Omer/Osama
/		Fri	Sat	Sun
	Amin/Hamza	Saleem	Ali	Omcr/Osama
iv)	Thu	Fri	<del></del>	
	Hamza/Saleem		Sat	Sun
- 41	Traniza Saleem	Osama	Ali	Amin/Omer

Thus the correct choice is D.

Z

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m ct Q13. (E) The possible schedule to fulfil this condition is:

Thu	Fri	Sat	Sun
Saleem	Hamza/Osama	Ali	Amin/Omer

Thus the correct choice is choice (E).



# Verbel Ablig

Verbal means 'pertaining to words' and ability means 'power of mind to do things', so in verbal test questions are stated in the form of words (language). The eandidates are supplied with a question paper which contains variegated exercises designed to test their knowledge and intelligence. The purpose of the 'Verbal Test' is to evaluate and analyze candidate's English comprehension and understanding towards the language. These tests can be of various kinds but the questions about sentence completion and analogy testing will be asked randomly. There will be also a question about critical reading (comprehension) that will be asked separately. The brief explanation about these questions will be given on the next pages. This section is consisted of following types of questions:

1. Sentence Completion

. 2. Analogy Test

3. Critical Reading

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(C)

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Ex:





In such type of questions, one or two blanks are given in a sentence, each blank indicates that something has been omitted. Four or five lettered words or sets of words are given below the sentence. The candidate is asked to choose the word or set of words, when inserted in the sentence, best fits the meaning of the sentence as a whole. Various choices i.e., (A) (B) (C) (D) are provided in these kinds of questions. The candidate is asked to complete the sentence by filling in the blanks with the most suitable choice. These questions are designed to determine the candidate's ability to recognize the following areas:

- Correct Sentence Structure
- Correct Choice of Vocabulary
- Applied Grammar (Rules)

The questions about sentence completion can be related to any of the other areas of study i.e., science, geography, general knowledge, history, literature etc., but the subject matter would not hinder the candidate's language ability. The knowledge of correct grammar and vocabulary is required to complete the sentence.

In this test, words and their correct use is judged. This test gives a good idea of the memory and the power to apply it at an appropriate time.

In sentence completion questions, you are given a sentence containing one or more blanks. A number of words or pair of words are suggested to fill the blank spaces. You must select the word or pair of words that will best complete the meaning of the sentence as a whole.

In a typical sentence completion question, if any of the answer choices is inserted into the blank spaces, the resulting sentence will be technically correct, but it may not make sense. Usually, more than one choice makes sense, but only one completely carries out the full meaning of the sentence. There is one best

answer	

## HOW TO ANSWER SENTENCE COMPLETION QUESTIONS

- Read the sentence carefully. Try to understand what it means. 1.
- Consider the blank or blanks with relation to the meaning of the sentence. Is a negative connotation 2. called for or a positive one? If there are two blanks, should the pair be comparative, contrasting, or complementary? Are you looking for a term that best defines a phrase in the sentence?
- Eliminate those answer choices that do not meet the criteria you established in step two. 3.
- Read the sentence to yourself, trying out each of the remaining choices, one by one. Which choice is 4. the most exact, appropriate, or likely considering the information given in the sentence? Which of the choices does the best job of completing the sentence?

<ol><li>First answer the questions</li></ol>	s you find easy. If you	have trouble with a que	stion, leave it and go back to it
later. If a fresh look does	not help you to come	un with a sure answer ma	ake an educated guess.
EXAM	PLES WITH EXP	LANATORY ANSWI	FDS
Direction: Select appropriate	e word from the choice	es to fill blanks.	SING
Example 1. My father	me that I should have	informed him	•
(A) said (I	B) told	(C) asked	M toll
	The sentence is the in	ndirect parration so 'said'	cannot be used. Asked cannot
be used in the indirect narration 'i	if or what where etc.	must need	Cannot be used. Asked cannot
Example 2. He was of	all the valuable posses	ecions	•
(A) robbed (1	R) stolen	(C) pinched	(D) established
The correct answer is (A)	Stolen cannot be use	ed because a man canno:	t be stolen, only goods can be
stolen; Similarly 'pinched' has no s	cense of 'denrive'	za occause a man camor	be storen, only goods can be
Example 3. Those who feel th	not war is stunid and us	management think that to	lie en the bettlefield is
(A) courageous (I	.41 was is stupiu and as R) prefentions	(C) useless	The on the pattieriety is
The correct answer is (C)	The bay to this and	(C) usciess	ssed that war is stupid and
unnecessary Those who are antag	for the Acy to the anathropist forward was and	wer is the attitude expre-	ssed that war is stupid and
unnecessary. Those who are antag is true that giving one's life in the	field of bottle is court	Juid consider a pattierier	death to be useless, while it
is true that giving one's life in the sentence. Choice (B), pretentious	magning "affectedly (	igeous (A), mat is not un	answer in the context of this
scntence. Choice (B), pretentious, that war is stupid. Choice (D) does	meaning antectomy g	grand or ostentations, or	bes not go along with the idea
Example 4. If you hear the	of a cun don't wor	.ation to a patticing ucas	th.
(A) burst (E	OI a guii, doir i worr	'y', it's only my car backing	iring,
The correct answer is (B)	report The sound of	(C) retort	(D) Hash
report. 4	report. The sound of	an expression, whether in	rom a gun or a car, is called a
Example 5. He demanded	ahadianga from us	and was always talling	· · · · · · · · · · · · · · · · · · ·
(A) total foolish (F	obcatence from us,	, and was always terming t	is we must be subjects.
(A) total, foolish (E)	b) partial, cringing	(C) format, rigorous	(D) complete, compliant
The correct answer is (D). You matthe best adjective for subjects.	ay assume mai no one	demands partial or marg	ginal obedience. Compliant is
		4.6 a. a. a. a. a.	·
Example 6. We are going (A) finally worthless (B)	g to have to race the re	ality that the resources o	f Earth are
(A) finally, worthless (B)	) gradually, limitiess	(C) eventually, tinite	(D)quickly, unavailable
(C) logically completes this senten	. As the Earth's resour	rees are not limitless, we	orthless, or unavailable, only
Evample 7 One reunion was	.ce.	4	the second of the second
<b>Example 7.</b> One reunion was flight?	completely wh	o'd have guessed we w	ould have booked the same
_	2) Cartaltana	200	
(A) illogical (B) The correct answer is (B)	i) fortunous	(C) expected	(D) abandoned
was fortuitous.	fortuitous, the senter	acc implies that the reun	nion occurred by chance so it
	1 1		
•	med guards us	from doing anything disr	uptive.
(A) defeated (B)	i) excited	(C) irritated	(D) prevented
Answer (D) is the only legisle	prevented. Armed gu	tards are intended to pre	event any kind of disruption.
Answer (D) is the only logical and	grammatical choice.		
Example 9. Held up only by a	steel cable, the	e chairlift was to c	carry only two people.
(A) siender, instructed (B	3) single, intended	(C) sturdy, obliged	(D) massive, designed
The correct answer is (13).	. This sentence is conc	cerned with the design o	of the lift. As it says "beld up

only by", you may assume that the cable is not large, which eliminates (C) and (D). Of the three remaining

Everyone should \_\_\_ limself against illness since medical care has now become expensive.

(B)

**(D)** 

**(B)** 

Ensure

Insure

Estimate

**(E)** 

(A)

**(C)** 

**(E)** 

(A)

7.

8.

Established

Brace

Cost

Vaccinate

Inoculate

How much did it \_\_\_\_\_ to reach Bombay by car?

1!

2(

	***************************************	Dogar's Unique Fully Solve			23
	(C) (E)	Charge Pay	(D)	Price	
9.	In the de	partmental inquiry, it we	as denied that the poli	ce had committed any	AH Dean
		cholody.	•		on peopl
	(A)	Blunder	(B)	Beatings	
	(C)	<u>Injuries</u>	$(\mathbf{D})$	Crime	
40	(E)	Excesses	•		
10.	The petiti	on before the Court praye	d for the appoi	ntment orders issued by the	management
	()	1 0041115	(B)	Quashing	80,,,,,,
	(C)		(D)	Removing	
4	(E)	Dismissing		S	
1.	Man powe	er is the means of	converting other resou	rces to mankind's use and	benefit.
	` /		(B)	Indispensable	o cincy cin
	(C)	Insuperable	(D)	Inimitable	
2.	(E)	Inequitable	, ,		
۷.	1 am giver	that you are g	oing abroad.		
	(A)	rredict	(B)	Understand	
		Learn	· (D)	Think	
3,		Apprehend			
J,	<i>by</i>	people's perception it see	ms that democracy has	succeeded in Pakistan.	
	(A)	Making	(B)	Planned	
	(C)	Following	6 (D)	Going	
A	(E)	Liked		•	
4.	the passer	ngers and crew members	of the aeroplane liad	a escape when it w	as taking off
	J. 0110 1110 7	ere retty.			
	(A)	Little	(B)	Brief	
	(C)	Narrow	(D)	Large	
5.	(E)	Better			
•	ite very su	ccessfully all the a	illegations leveled agai	nst him.	
	(A)	Retaliated	<b>(B)</b>	Rebutted	
		Extricated	<b>(D)</b>	Eradicated	
	(E)	Protected			
	A giue proc	luced by bees tot	teir hives appears to co	utain antibiotic substances.	
	(4)	Duna	(B)	Decorate	
	(C)	Collect	(D)	Design	
	(E)	Structure			
•		for and waslegal	aid by the Labour Min	istry.	
		Allowed	(B)	Awarded	
	(C)	Offered	· (D)	Granted	
3.	(E)	Implemented			
•	ine aejenai	ing champion justified his	s top by clinchin	ng the title.	
	(A)	recimique	<b>(B)</b>	Supremacy	
	(C)	Skill	(D)	Form	
	(E)	Billing			
•	He has	people visiting him	at his house because	e he fears it will cause di	isconifort to
	neighbours.			,	arengen io
	(A)	Stopped	<b>(B)</b>	Warned	
	(C)	Curtailed	( <b>D</b> )	Requested	
	(E)	Forbidden		·	
	There are	views on the issue o	of giving bonus to the e	niployees.	
	(A)	Modest	(B)	Adverse	
	(C) (E)	Independent Valuable	( <b>D</b> )	Divergent	
		3 ( - 1 - 1 - 2 )			

**(D)** 

**(B)** 

(D)

\_ gentleman and soldier you are, leave at once before he finds you here?

Borrowed

Luminous

Ostentatious

**(C)** 

(A)

(C)

Will you, like the

5.

Finished

Chivalrous

Barbarous

17

18

15

20

**(B)** 

**(D)** 

**(B)** 

Sabotage

Villainy

Agree

part of a (A)

21.

(C)

(A)

Conspiracy

\_ a car to be absolutely necessary these days.

Game

Consider

(A) Hampered, shortage (B) Prevented, supply (C) Held, non-availability (D) Denied, restrictions (E) Completed, disappearance  10. The bandit	NI	SGuide Do	ogar's Unique Fully Solved "NEW 1	resting sy:	STEM" GUIDE	241
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(E) Candidature, inappropriate  He is so that everyone is always to help him in his work.  (A) Adamant, enthusiastic (B) Miserly, ignorant  (C) Helpful, reluctant (D) Aloof, cooperative  (E) Magnanimous, eager  14. The activities of the association have from the objectives set for it in the initial years.  (A) Details, grand (B) Emerged, total  (C) Grown, simple (D) Deviated, original  (E) Increased, perverse  15. The leaders were needed by those to they were addressed.  (A) Scarcely, whom (B) Rarely, where  (C) Angrily, who (D) Readily, which  (E) Joyfully, when			Claim, unrealistic			
13. He is so that everyone is always to help him in his work.  (A) Adamant, enthusiastic (B) Miserly, ignorant  (C) Helpful, reluctant (D) Aloof, cooperative  (E) Magnanimous, eager  14. The activities of the association have from the objectives set for it in the initial years.  (A) Details, grand (B) Emerged, total  (C) Grown, simple (D) Deviated, original  (E) Increased, perverse  15. The leaders were needed by those to they were addressed.  (A) Scarcely, whom (B) Rarely, where  (C) Angrily, who (D) Readily, which  (E) Joyfully, when				(-)	, , ,	5
(A) Adamant, enthusiastic (B) Miserly, ignorant (C) Helpful, reluctant (D) Aloof, cooperative (E) Magnanimous, eager  14. The activities of the association have from the objectives set for it in the initial years.  (A) Details, grand (B) Emerged, total (C) Grown, simple (D) Deviated, original (E) Increased, perverse  15. The leaders were needed by those to they were addressed.  (A) Scarcely, whom (B) Rarely, where (C) Angrily, who (D) Readily, which (E) Joyfully, when	<b>13.</b>	He is so		to help him	in his work.	
(C) Helpful, reluctant (E) Magnanimous, eager  14. The activities of the association have from the objectives set for it in the initial years.  (A) Details, grand (B) Emerged, total (C) Grown, simple (D) Deviated, original (E) Increased, perverse  15. The leaders were needed by those to they were addressed.  (A) Scarcely, whom (B) Rarely, where (C) Angrily, who (D) Readily, which (E) Joyfully, when		(A)				
(E) Magnanimous, eager  14. The activities of the association have from the objectives set for it in the initial years.  (A) Details, grand (B) Emerged, total (C) Grown, simple (D) Deviated, original (E) Increased, perverse  15. The leaders were needed by those to they were addressed.  (A) Scarcely, whom (B) Rarely, where (C) Angrily, who (D) Readily, which (E) Joyfully, when		(C)	Helpful, reluctant			
14. The activities of the association have from the objectives set for it in the initial years.  (A) Details, grand (B) Emerged, total (C) Grown, simple (D) Deviated, original (E) Increased, perverse  15. The leaders were needed by those to they were addressed.  (A) Scarcely, whom (B) Rarely, where (C) Angrily, who (D) Readily, which (E) Joyfully, when		<b>(E)</b>	-	( )		
years.  (A) Details, grand (B) Emerged, total (C) Grown, simple (D) Deviated, original (E) Increased, perverse  15. The leaders were needed by those to they were addressed. (A) Scarcely, whom (B) Rarely, where (C) Angrily, who (D) Readily, which (E) Joyfully, when	14.	The activity	ies of the association have	from the	objectives set fo	r it in the initial
(A) Details, grand (B) Emerged, total (C) Grown, simple (D) Deviated, original (E) Increased, perverse  15. The leaders were needed by those to they were addressed. (A) Scarcely, whom (B) Rarely, where (C) Angrily, who (D) Readily, which (E) Joyfully, when			<del>-</del>			
(C) Grown, simple (E) Increased, perverse  15. The leaders were needed by those to they were addressed.  (A) Scarcely, whom (B) Rarely, where (C) Angrily, who (D) Readily, which (E) Joyfully, when		•	Details, grand	(B)	Emerged, total	
(E) Increased, perverse  The leaders were needed by those to they were addressed.  (A) Scarcely, whom (B) Rarely, where  (C) Angrily, who (D) Readily, which  (E) Joyfully, when			•			
15. The leaders were needed by those to they were addressed.  (A) Scarcely, whom (B) Rarely, where (C) Angrily, who (D) Readily, which (E) Joyfully, when			•	(2)	2	
(A) Scarcely, whom (B) Rarely, where (C) Angrily, who (D) Readily, which (E) Joyfully, when	15.			they we	re addressed.	
(C) Angrily, who (D) Readily, which (E) Joyfully, when						
(E) Joyfully, when		. ,	- ·			
				(1)	readily, milen	
	16.			something.		

1 jun Pro

42			NTS 4	SECTION - III: VERBAL ABILITY
	(A)	Worrying, paying	*	
	(C)	Begging, demanding	(B)	0,
	(E)	Donating, demanding	(D)	Talking, doing
7.	Due to	rainfall this was the	,	
	(A)	rainfall this year, there и Sufficient, no	vill be cut	in water supply.
	(C)	Enough, substantial	(B)	. ,
	(E)	Abundant, considerable	<b>(D)</b>	Meager, least
8.	We must e	explore sources of ana-		44
	(A)	xplore sources of ener Natural, exhausted	gy as our supply	of fossil fuel has been
	(C)	Alternative, depleted	(B)	,
	(E)	Innovative, augmented	(D)	Guaranteed, over
9.		inaged to several times	a 1	
	(A)	Escape, arrested		
		Deceive, cheated	(B)	
		· Abscond, kidnapped	<b>(D)</b>	Defend, acquitted
0.		re more		
	(A)	Conservative, seen in	their q	uickness in learning a new language.
	• /	i ati i o i socii ili	(B)	Susceptible, demonstrated in
	(E)	Intelligent, disproved by	<b>(D)</b>	Adaptable, reflected in
1.	The Educa	Resourceful, proportionate t	'A	
••	(A)	Suppression with the second	need to discover a	andeach student'stalents.
	` '	- "PP-400, Potontial	(B)	Flourish, hidden
	(C)	Enlarge, dormant	(D)	Belittle, concealed
2.	(E)	Develop, intrinsic		
••	aze is usual	ly, but today he appear	rs rather	
	(A)	Quiet, caim	(B)	Happy, humorous
	(C)	Strict, unwell	(D)	Tense, restless
,	(E)	Calm, disturbed		
	The war	inunediately after the cea	ase-fire proposal v	was bilaterally
	(A)	Dogati, Histarion	(B)	Extended, mitigated
	(C)	Receded, exchanged	(D)	Started, prepared
	(E)	Ended, accepted	(-)	- mired, propared
•	Yousaf	another feather hi	s cap by his wond	erful performance in the one day match.
	(A)	,	(B)	Created, for
	· ( <b>C</b> )	Kept, by	(D)	Captured, from
	<b>(E)</b>	Added, to	(1)	Capturou, HOIII
• ,	Any system .		of support from ti	ha nuklia
	(A)	Fail, want		
	(C)	Survive, lack	(B)	Finish, failure
	(E)	Launch, paucity	<b>(D)</b>	Succeed, reason
	. ,		ICINEDO	
	F		ISWERS	
	-	1. <b>(E)</b> 2. <b>(E)</b> 3.	(B) 4.	(A) 5. (B)
	11	6. <b>(B)</b> 7. <b>(C)</b> 8.	(B) 8.	(A) 10. (B)
	11-	11. <b>(A)</b> 12. <b>(D)</b> 13.		(D) 15. (A)
		16. <b>(D)</b> 17. <b>(A)</b> 18.		<del></del>
		21. <b>(E)</b> 22. <b>(E)</b> 23.	tioner & Tonica Comment	Charles and the second
	-	(E) 23		(E) 25. (A)
		T	YPE-II	
		SENTENCE COMPLE	TION USING	GRAMMAR
,		Learn	hy Evamela	
(	Jenius does	what it must, and talent does when	hat it	
	(A) C	an (B) Would		
	(C) N	1-7 11 0 41 41		

1!



# Multiple Choice Questions (MCQs)

The passengers were very happy the friendly and warm treatment given to them.							
	(A)	From	(B)	To ·			
	<b>(C)</b>	Ву	( <b>D</b> )	About			
	The higher	you go, the more difficult it					
		Is becoming	(B)	Became			
	(C)	Has become		Becomes			
	The childre	n were disappointed because they h					
	(A)		(B)	To had gone			
	(C)	To have gone	( <b>D</b> )	To go ,			
		Ahsan, but could not utter a .		-			
	(A)	About	(B)	Before			
	• •	For	(D)	То			
	` '	Towards	(2)	•			
		iend I-trust most.					
	(A)	Which	(B)	Who			
	(C)	Him	(D)	Whom			
		ispense his service.	(D)	W Hom			
	(A)	With	<b>(B)</b>	Of			
	(C)	In	• •	· · · · · · · · · · · · · · · · · · ·			
			(D)	At			
		one several times before I an		Nava nimaina			
	(A)	Has rung	(B)	Was ringing			
		Would ring	(D)	Had rung			
		desert him all the world.	49-	•			
	(A)	By	<b>(B)</b>	For *			
	(C)	With	<b>(D)</b>	From			
	L bought a i	new.car last year, but I nuy o	ld car yet, so	at present I have two cars.			
		Have sold	<b>(B)</b>	Did not sell			
		Could not sell	<b>(D)</b>	Have not sold			
		tid he go iu he came out.					
	(A)	Than	(B)	And			
	(C)	Then	<b>(D)</b>	When			
	The judge a	equitted the prisoner the ch	arge of murd	ler.			
	(A)	About •	(B)	From			
	<b>(C)</b>	Of .	<b>(D)</b>	With			
	An argume	nt between the two friends.					
		Broke out	(B)	Broke in			
	( <b>C</b> )	Sprang up	(D)	Rose up			
		a child, I to school everyda					
	(A)	Had walked	(B)	Have walked			
	(C)	Walked	(D)	Have been walking			
		come to see us we bought to		_			
	(A)	Since	(B)	For			
	(C)	When	(D)	Till			
	He : an	N Hell	(D)				
			( <b>D</b> )	So quickly			
	(A)	Quickly	(B)	So quickly			
	(C)	Quick	(D)	So quick			
		addam was up more than his		P			
	(A)	Into	(B)	For			
	(C)	То	(D)	Against			
	The doctor (A)	advised him to go several m Through					
			<b>(B)</b>	Into			

244	NTS Guide SECTION - III: VERBAL ABILITY	N.
	*	
18.	(C) Under (D) About	
10.	If you persist in telling lies to me I shall sue you slander.	
	(A) For (B) On (C) With (D) To	
19.		
	The waiter hasn't bought the coffee I've been here an hour already.  (A) Up (B) Till	4.
	(C) (C) 1 III	
20.		
	The modern club is simply a more refined substitute the old fashioned tavern.  (A) For With	5.
	(b), with	4
21.		
J	After the advice of his father, he was recouciled his wife.  (A) With To	
	(C) Into	
22.		6.
	The doctor tried both penicillin and sulphanilamide; the penicillin proved to be the effective drug.	
	(A) Most (B) Bad	
	(C) Very (D) More	7.
23.	However honest he, I do not trust him.	1 4
	(A) Might be (B) Could be	1917
	(C) In	8.
24.	He became the Governor of a Province (D) May be	1 1
	(A) In course of time (B) At times	
	(C) Link I that	Ž
25.	(C) Little by little (D) By and large  the rain stopped, the play had to be suspended.	
	(A) When (B) Since	9.
	(C) While (D) Until	1 1
	ANSWERS	
	1. (C) 2. (D) 3. (D) 4. (B) 5. (D) 6. (A) 7. (D) 8. (P) 9. (D) 10. (A)	10.
	(b) (c) (d) 9. (d) 10. (A)	1 1 10.
	11. (C) 12. (C) 13. (C) 14. (A) 15. (A)	
	16. (D) 17. (A) 18. (A) 19. (D) 20. (A)	
	21. (B) 22. (D) 23. (D) 24. (A) 25. (D)	
	TYPE-III	
	SENTENCE COMPLETION USING APPROPRIATE FILLER	111.
	Learn by Example	1 7 "
	The notice at the petrol pump should be	111.
.* .	(A) All engines need to be switched off	1111
	(B) All engines have to be switched off	12.
	(C) All engines must have to be switched off	
	(D) All engines must be switched off.	11
Answei	r: (D)	13.
	Man all a man and a second	11
	Multiple Choice Questions (MCQs)	
Directio	best one which can complete the incomplete statement followed by some fillers is given. Pick	
out the l	best one which can complete the incomplete statement correctly and meaningfully.	100
1.	If they share burden alternately, they	
	(A) World and the 1	14.
	(b) Will get latigued	
	(E) Don't get tired	17 6.5
2.	When I saw him through the window	1 15.
	(A) I ran out to open the door (B) I have run out to open the door	
	(C) I should run out to open the door (D) I am running out to open the door	
	1	

#### NTS Guide Dogar's Unique Fully Solved "NEW TESTING SYSTEM" GUIDE 3. Every person must learn\_ That his time needs a wise use (A) (B) Wise ways in his time's use **(C)** To make wise use of his time **(D)** To using his time in a wisely manner That how wisely his time can be used **(E)** 4. The income tax raid was too sudden (A) So that the man escaped **(B)** For the man escaping **(C)** Then the man escaped **(D)** For the man to escape 5. Many people have law degrees But not all of them practice law (A) (B) However it isn't practised by all And some of them do have practice **(C)** But some of them do not practice it **(D) (E)** Yet some are not undergoing practices 6. He passed the examination in the first class because he Worked hardly for it (A) (B) Was hard working for it Was working hard for it **(C) (D)** Had worked hard for it 7. 'Where are my spectacles?' (A) There are they, on your nose! (B) There they are, on your nose! (C) Here are they, on your nose! **(D)** Here they are, on your nose! 8. With great difficulty, (A) He could keep his cool **(B)** He could get annoyed (C) He could not tolerate his nonsense **(D)** He could lose his temper He could perform his usual functions **(E)** 9, He always stammers in public meetings, but his today's speech Was not liked by the audience (A) **(B)** Was not received satisfactorily (C) Was surprisingly fluent Was fairly audible to everyone (D) present in the hall **(E)** Could not be understood properly The Chairman rejected the proposal of increasing employee's salary because: 10. The company had already gained three thousand crore profit (A) **(B)** The company did not have sufficient funds to afford the rise (C) The number of employees in the company was very small (D) The employees had been demanding it for a long time **(E)** It was not difficult for the company to bear additional burden 11. To succeed in a difficult task, (A) You need a person of persistent (B) One needs to be persistent · (C) One needs to be persistence **(D)** Persistent is needed **(E)** Persistent is what one needs 12. I shall not be late for dinner Unless the train will be late (A) **(B)** Unless the train will not be late If the train is late **(C) (D)** Unless the train is late 13. I would not have kelped such an ungrateful man.

(A)

**(B)** 

**(C) (D)** 

**(E)** 

(A)

**(C)** 

(A)

(C)

**(E)** 

Unless you work very hard,

14.

15.

Had I been in your place

Had I asked him for his help

You are not being successful

You ought to be successful

The more we looked at the piece of modern art, We liked it less

It looked better

Better we liked it

Even after knowing that he was ungrateful

Though he did not deserve any help at all

**(B)** 

**(D)** 

**(B)** 

(D)

You will not be successful

You be not successful

The loss we liked it

The more we like it

If he had shown due respect to me

6

7.

10

13.



# Multiple Choice Questions (MCQs)

# (Sentence Completion)

## TEST NO. 1

•	Choose the word which best completes each ser		
1.	We lost confidence in Salim because he never		the grandiose promises he had made.
(A)	lired of	(B)	Delivered on
(C)		(D)	Forgot about
2.	The driver suddenly applied the brakes when he	e saw a	truck alread of him.
(A)	Stationary	(B)	Moving
(C)		(D)	Immobile
3.	Knowledge is like a deep well fed by		
	drop in it.	7 0	,
(A)	External	(B)	Perennial
(C)	Immortal	(D)	Inehaustible
4.	Salma is much tooto have anything to	do with	
(A)	Noble	(B)	Proud
$(\mathbf{C})$		(D)	Difficult
<i>5</i> . `´	There is no incentive for America to sign the tr	roπtv sin	
	nation intends to honour its provisions.	Emejo Dane.	te there is every reason to
(A)	Regret	(B)	Inform
(C)	Believe	(D)	Occupy
6.	A legislation was passed to punish brokers who	n (10)	their clients funds.
(A)	Defalcate	(B)	Devastate
(C)	Devour	(D)	·
7.	Normally, an individual thunderstorm	whom A	EHRUGZZIG  Finduction
(A)	Lasts		
(C)		(B)	Ends
8.		(D)	Continues
(A)	The task seemed impossible but somehow Jalil Pulled it up		very skuljuny in the ena.
(C)	Pulled it away		Pulled it off
9,	The unruly behaviour of the childrentl	(D)	Pulled it out
(A)	Aggrieved 11		
(C)	Incensed	(B)	Impeached
10.		(D)	Tempered
l U.	We were amazed that a man who had been here	etofore u	he most of public speakers could, in
(A)	a single speech, electrify an audience and bring Pedestrian		
		(B)	Accomplished
(C)	Masterful	(D)	Auspicious
[].	The chairperson is a scintillating speaker whose		
(A)	Entertain		Absorb
(C) 12.	Enthrall	(D)	Alienate
	Ali force himself to work on till late in t		
(A)	Would	(B)	Would be
(C)	Could	(D)	Used to
13.	The officers threatened to take reprisals if the natives.	lives of	their men were by the conquered
(A)	Destroyed	(B)	Endangered
(C)	Enhanced	(D)	Irritated
	His moral decadence was marked by his		he ways of integrity and honesty.
(A)	Obsession .	_ <i>from u</i> _ (B)	Declivity
(C)	Departure		Opprobrium
( - ,	- opinion	(D)	Opprobrium

48		,			NTS	Guide SECTION - III	: VERBAL ABILITY
5.	Her reaction	ı was not tl	te only	one			
(A)	Workable				(B)	Possible	
(C)	Likely				. (D)	Good	
6.	After a perio	od of protra	cted disuse	, a muscle	will atrop	ty, both its stre	ngth and the ability to
	perform its j	function.			<i>r</i>		
<b>(A)</b>	Insuring				<b>(B)</b>	Regaining	
<b>(C)</b>	Sustaining	,			( <b>D</b> )	Losing	
7.	True health	and true su	iccess go to	gether for i		separably in t	he thought realm.
(A)	Interwined	i		<b>.</b> ,	(B)	Tied up	we mongin remin
(C)			1.191		<b>(D)</b>	Inter-related	
•	If you are	trying to n	nake a stri	ong impres	รion on	your audience you ca	unot do so by being
	unaerstatea,	tentative, f	or	~ .		•	,
(A)	Passionate				(B)	Authoritative	
(C)					(D)	Argumentative	
	Although, I	lıad pledged	l not to tell	anyone of t	the previo	us evening's trauma, t	he compulsive urge to
	unburden m	yself becam	ıe		<del>.</del> .	•	. 0
(A)	•	us			(B)	Overwhelming	
C)	Impassive				<b>(D)</b>	Irresistible	
	The	arguments	put forth f	or not discl	osing the	facts did not impress a	ny body.
<b>A</b> )	Specious				<b>(B)</b>	Intemperate	
C)	Spurious				<b>(D)</b>	Convincing	
				ANSV	VERS		
		1	(B)	2.	(A)	3. (B)	
		4,	(A)	<b>5.</b> (0.1.)	(C)	6. (D)	
		7.	(A)	. 8.	(D)	9. (C)	
		10.	(A)	11.	(C)	12. (A)	
		13.	(B)	14.	(C)	15. (B)	
		16.	. (D)	17.	(A)	18. (C)	
		19.	(D) '	20,	(A)	1	
	• •			· · · · · · · · · · · · · · · · · · ·			J
				nameda.	NIO 0	4	
	Chassatha			TEST	NO. 2		
	Some officer	ora wnich,	when inser	rted in the s	sentence,	est fits the meaning of	f sentence.
	the contra aid		their j	previous sta	itements	lenying any involveme	nt on their part with
<b>(</b>	Recanted	л петмогк.			(T)\	÷	
Ž)	Justified				(B)	Protracted	
-)		t haaamaa			<b>(D)</b>	Repeated	
<b>(</b> )	Well	i oecomes .		npetitive, so	ome conų	anies will make larger	profits.
) )	Less				(B)	More	
-)		e condition	a dec endadado	n/ i	( <b>D</b> )	Fully	
	to worthwhil	: conunions	i in which charachart	Kiaz choos	es to live	suggest that he is mise	rly, his contributions
<b>4</b> )	Intolerant	e charmes .	snow inai n	ie is	1	0.1	
) ()	Generous				(B)	Stingy	
7	He suggests t	hat the second	ed lana		· (D)	Thrifty	
.)	Be	nui ine mee	ung	postpone		T	
)	Must				(B)	Is	
-,/		itecture lini	discondad	tha	(D)	Would be	
	life.	-cease mus	uiscurueu	me	_ irimmiii	g on buildings and emp	onasises stinplicity of
<b>(</b>	Flamboyani	t			<b>(D)</b>	Plabbanes - +time	
Z)	Gaudy		•	•	(B)	Flabbergasting	
,	Can he see hi	s wife agai	n2 No be		<b>(D)</b>	Gaunt	
.)	Could	s mye ugun	110, ne _	<del></del> '	(D)	Con	·
-) ])	Will not	·			(B)	Cannot	
						LASTOT	

. . .

NIS	Guide Dogar's Unique Fully Solved "NEW TE	STING	SYSTEM" GUIDE 249
7.	A man is one of those blessed artists who comb	ine nra	fundity and
(A)	Fun	(B)	Education
(C)	Depth	(D)	Wisdom
8.	The accused was released on pending	haarina	n of his case
(A)	Bond Penuing	пеш інд (В)	Bale
(c)	Bail	(D)	Deposit
9. ` ´	Sadiq's in his family's position is great	hut ha	does not hoost about it
(A)	Status	(B)	Proud
(C)	Pride	(D)	Presumption
10.	There are many dialects of English with radic		ferent pronunciations of the same word had
1	the spelling of these words is		ferent prominentations of the same word, our
(A)	Shortened	(B)	Inconstant
(C)	Contemplated	(D)	Uniform
<i>11</i> .	New concerns about growing religious tension		
	and Muslinis.		man were mas week betweek ilmans
(A)	Dispersed	(B)	Fucled
(C)	Invalidated	(D)	Restrained
12.	Wasim was so good at Mathematics that his frie		
(A)	Prodigy	(B)	Prodigal
(C)	Primeval	(D)	Profligate
13.	The majority report issued by the committee w		inletely extalling in great detail the
	plan's strengths but failing to mention at all its	shortco	ominos
(A)	Skewed	(B)	Unbiased
(C)	One-sided	(D)	Comprehensive
14.	I decided to sell a piece of land when I was offe	red a n	nore price
(A)	True	(B)	Realistic
(C)	Exact	(D)	Correct
<i>15</i> .	The enemy paid a large sum as	(D)	Contect
(A)	Punishment	<b>(B)</b>	Reward
(c)	Restitution	(D)	Compensation
16.	Despite the mixture's nature, we found	d that h	ou laurarina its tournarature in the laborators
	we could reduce its tendency to vaporize.	a mu o	y towering us temperature in the haboratory
(A)	Homogeneous	<b>(B)</b>	Resilient
(C)	Volatile	(D)	Acerbic
17.	Many boys were at street corners for the	o coffee	har to onen
(A)	Hanging upon	(B)	Hanging about
(C)	Hanging back	(D)	Hanging on
18.	His monotonous voice acted like and hi	s audie:	nce was soon asleen
(A)	An emetic	(B)	An anacsthetic
(C)	A sedative	(D)	A purgative
19.	My finger is still where I caught it in the	a door i	A purgative
(A)	Sore	(B)	Wounded
(C)	Injured	(D)	Bruised
20.	The flood water pushed against the river wall an	d (D)	from a sudden break made by it.
(A)	Ran out	(B)	Serged up
(C)	Gushed out	(D)	Flowed
ì	ANSWE		110,000
	1. (A) 2.	(B)	3. (C)
	4. (A) 5.	(C)	6. (D)
	7. (A) 8.	(C)	9. (A)
	10. <b>(D)</b> 11.	(B)	12. (A)
	13. <b>(C)</b> 14.	(B)	15. (D).
	16. (C) 17.	(B)	18. (C)
:	19. <b>(D)</b> 20.	(B)	

#### TEST NO. 3

		TOI MO'	•	
•	Complete the sentences by given choice	?s.		
<i>1</i> .	Measurentent is, like any other humai	t eudeavour, a	complex activity, subj	ect to error, not always
	, una frequently nustulern	reted and wisi	mderstood.	ser to enough not unways
(A)	rioperly	(B)	Innovatively	,
(C)		(D)	Systematically	
2,	Non-violence is the law of saints as viol	leuce is the law	v of the	
(A)	Coward	<b>(B)</b>	Foolish	
(C)		(D)	Ignorant	
3.	His injury was very painful but not inc	apacitating an	id he managed to	the game in onits of
	it.		in managea to	ine game in spite of
(A)	Interrupt	(B)	Concede	
(C)	Abandon	· (D)	Finish	,
4.	They have some difficulty all the	(D) Le employees 2	rimon renacially the engaller o	**************************************
	the adopted scale of wages.	ic employees, e	especially the straiter of	nes to confirm
(A)	Getting, to	(B)	In catting upon	
(C)	To get, over	(D)	In getting, upon	
<i>5</i> .	This contract was; it was not va	did now	To getting, with	
(A)	Nullified		A	
(C)		(B)	Annulled	
6. ` ´		(D)	Canceled	
	To the dismay of the student body, the co	iass president i	was berated by	the principal,
(C)	2	(B)	Magnanimousiy	
<i>7</i> .	We never believed that the	(D)	Ignominously	
	We never believed that he would resort him as an honest man.	to in c	order to achieve his end	l, we always regarded
(A)	Logic	ì		
(C)	Charm	(B)	Subterfuge	•
8. °		<b>(D)</b>	Diplomacy	
(A)	It was the help he got from his parents we Boosted		him through the traged	ly.
(C)	Helped	<b>(B)</b>	Supported	
g. (C)		<b>(D)</b>	Parked	
,	The plot of the play was extremely complete or control events	licated and inc	luded many minor-cha	racters to the
(4)	Total Crents.			**************************************
(A)	Tangential	(B)	Contemporary	
(C)	Essential	(D)	Momentous	
10.	It is a marble wall, no bills.			
(A)	Stick	<b>(B)</b>	Affix	· ·
(C)	Paste	(D)	Attach	
<i>II.</i>	You will have to catch the morning flight	, so you	better get ready.	
(A)	Would	(B)	May	
(C)	Had	(D)	Should	
12.	The controversy is likely to create	between the	two rivals.	
(A)	Doubt	(B)	Amity	
(C)	Bitterness	(D)	Revenge	
13.	The authority of voice in Faraz writing st	rikes many rec	iders today as	colonialism,
(A)	Cognizant of	(B)	Detrimental to	coroniauşm,
(C)	Consonant with	(D)		
4.	Beauty is to ugliness as adversity is to	( <i>D</i> )	Independent of	
(A)	Prosperity	(B)	Cowardice	İ
(C)	Miser	(D)		j
	Whenever Imran refers to his favourites	(D) Lia je valukla	Happiness	Literatura de la constitución de
		ne is voidble,	vui when he taiks of	uis adversaries he is
(A)	Rough	/D)	Datiaant	
		<b>(B)</b>	Reticent	

4.	A good lawyer will argue only what	is central to an is	sue, elimiuating information	n whic
	might jeopardize the client.		, <u>, , , , , , , , , , , , , , , , , , </u>	
(A)	Extraneous	(B)	Prodigious	
(C)	Seminal	(D)	Erratic	
5.	Ali got the company car for a	price as he was th	e senior most employee in the comp	any.
(A)	Nominal	(B)	Fixed	
(C)	Discounted .	(D)	Reduced	
s. ·	His novel is both so eloquent in its pa	ssion and so séarc	ching in its candor that it is bound to	,
	any reader.		ŭ	
(A)	Bore	(B)	Disappoint	
(C)	Unsettle	(D)	Embarrass	
7.	We felt as if the ground was b	eneath our feet.		



Т	<b>EST</b>		$\cap$		5
1		1.4	v	٠	J

	Didn't you	tell me that you would com	te to see nie? No. I	
	(A)	Didn't	(B)	Had not
	(C)	Have not	$(\mathbf{D})$	Could not
		the tickets for the mo	vie in advance.	
	(A)	Remove	(B)	Take
	(C)	Draw	(D)	Buy
	Only	_ were present at the semin	nar	Duy
		A few people	(B)	A little people
		A few people	(D) (D)	The little people
		rapher is very efficient, He	is to bis firm	The mae people
	(A)	An asset	(B)	A boon
	(C)	A credit	(D)	A blessing
		are so alike that I cannot_	oue from the off	A Olessing
	(A)	Say	one from the on (B)	Notice
		Discern		
		_ the files on my table.	<b>(D)</b>	Tell
	(A)	_ the jues on my table.  Let	<b>(D</b> )	T
	` '		(B)	Leaves
	(C)	Stay	(D)	Leave
	1 never mis	s a cricket match. I		childhood.
	(A)	Am	(B)	Has been
	(C)	Have been	(D)	Will be
	An of us sn	ould abide the laws		_
		By	(B)	In .
	(C)	То	<b>(D)</b>	With
	Tue period	of the fall of the Roman Er	upire was a dark perio	od for as well as for other arts.
		Aesthetics	(B)	Gastronomy
		Astrology	· (D)	Histrionics
•		a very hot climate.		
	(A)	Has	(B)	Have
	(C)	Has been	(D)	With
	That profes	sor enjoys teaching and	*	
	(A)	Writing	(B)	Written
	(C)	To write	(D)	Write
•	She came_	with me to see the ci	rcus.	
	(A)	After	(B)	Across
	(C)	Along	(D)	Off
	The police i	has been looking for him_	four weeks.	
	(A)	During	(B)	For
	(C)	Since	(D)	Till
		covery of insulin, it was not		
	(A)	Prior	(B)	Before to the
	$(\mathbf{C})$	Prior to the	(D) ·	To prior the
	Do no hank			To prior the
	(A)	For .	(B)	Towards
		After	(D)	About
	(C)		(D)	
	(C) In vartuers.		oreg on Motos	Wan
	In partuers.	hip with Pakistan, South Ke		-
	In partuers. (A)	hip with Pakistan, South Ko Helped worked	(B)	Helping work
	In partuers. (A) (C)	hip with Pakistau, South Ko Helped worked Helped working		-
	In partuers. (A) (C) He is too di	hip with Pakistan, South Ko Helped worked Helped working dl the problem.	(B) (D)	Helping work To help working
	In partuers. (A) (C)	hip with Pakistau, South Ko Helped worked Helped working	(B)	Helping work

254	NTS Guide SECTION - III: VERBAL ABILITY			MI:
	(A) Between (B) Among		A STATE OF THE PROPERTY OF THE	11.
ľ	(C) To . (D) In	1		(A)
19.	Thank you for me your book.	1		(C)
	(A) Borrowing (B) Lending	1	450	12.
	(C) Borrowed (D) Had lent	1	1	(A)
20.	Although he is blind, he is very fast calculations.		18	(C) 13.
	(A) At (B) About		200	15.
	(C) In (D) With		C	(A)
	ANSWERS			(C)
	1. (C) 2. (D) 3. (A) 4. (A) 5. (D)		1	14.
	6. <b>(D)</b> 7. <b>(C)</b> 8. <b>(A)</b> 9. 10. <b>(A)</b>		1	(A)
	11. (A) 12. (C) 13. (B) 14. (C) 15. (C)	- 1	3	(C)
	16. (C) 17. (D) 18. (B) 19. (B) 20. (A)		91	15.
	TEST NO. 6		- 1	
<b>*</b>	Select the word that best completes each of the following sentences:	1		(A)
<i>1</i> .	The reasoning in this editorial is so that we cannot see how anyone can be deceived by it.		7	(C)
(A)	Dispassionate (B) Cogent		1	16.
(C)	Specious (D) Coherent			(A)
<i>2</i> .	Sometimes, it is necessary for an author to know what is going on in the minds of his characters.			(C) 17.
	This is called .			
(A)	Omniscience (B) Omnipotence			(A) (C)
(C)	Truclence (D) Omnipresence			18.
3.	The press conference did not clarify many issues since the president responded with obfuscation			243
	and rather than clarity and precision.			(A) (C) 19.
(A)	Lucidity (B) Vagueness	ı		19.
(C)	Formality (D) Humor			(A) (C)
4.	Sri Lanka, for the present, is deeply in economic difficulties, but, the Government has taken	- }	- 1	(C)
(A)	a pledge to set everything right within 2 years.  Ruined (B) Swamped	1	1	20.
(A) (C)		ı		(A)
5.	Saturated (D) Engrossed  I don't know to value your qualities.			(C)
(A)	Only how (B) Flow		1	
(C)	So how (D) That how			ł
6.	The of evidence was on the side of the plaintiff since all but one witness testified that		ł	ı
,	Salim's story was correct.			
(A)	Brunt (B) Accuracy			
(C)	Propensity (D) Preponderance		. 1	
<i>7</i> .	Patriotism, like so many other objects of this imperfect world, is a web of good and evil.			
(A)	Tangled (B) Entrapped			
(C)	Entangled (D) Complicated			
8.	It is difficult for a modern audience, accustomed to the minutiae of film and TV; to appreciate			
(4)	opera with its grand spectacle and gestures.  Subtle (B) lnane			<b>♦</b>
(A) (C)	\mu_/			Ī.
9.	Monotonous (D) Extravagant  She should continue to remain cold towards her lover till the latter has taken to move her			(A)
	heart to kindness.			(C)
(A)	Suffering (B) Pain		,	<i>2</i> .
(C)	Trouble (D) Pains			( <b>A</b>
10.	Though Akram was theoretically a friend of labour, his voting record in party that	ļ		(C)
	impression.			3.
(A)	Belied (B) Confirmed			,,,
(C)	Maintained (D) Implied			(A
			'	

manufacturers continue to \_\_\_\_\_ their prices at an astonishing rate.

(A)

Control

Cursory

Indigent

Write

Written

Obedience

Faithfulness

**(D)** 

(B)

**(D)** 

**(B)** 

**(D)** 

Progress in government, literature, art, religiou, science and philosophy \_\_\_\_\_ great civilisations

(A)

**(C)** 

(A)

**(C)** 

(A)

**(C)** 

17.

18.

19.

Assiduous

Lethargic

Allegiance

Loyalty

Wrote

To write

The courtiers had to swear \_\_\_\_\_ to the new king.

He never \_\_\_\_\_ to her in the near past.

from inere groups of society.

Ì.

2.

3.

4.

5.

6

7

rs,	Guide Dogar	's Unique	Fully Solve	d "NEW T	ESTING	SYSTEM" GU	JIDE		
4)	Relinquish				(B)	Distinguish			
)	Describe					Extol		•	
,		tenuna ele	aida	<b>.</b>	(D)		L <i>C</i> .:		
)	The pin	unce in	e wiaow rec	eives from		y cannot keep . Munificont	uer from	i poverty.	
, )	Niggardly				(B)	Magnanimou			
,	ruggardry			4 37 61	(D)	Magnammot	ıs	•	
		1	(4)		WERS	1 3 1	(D)	٦.	
		1. 4.	(A)	2.	(C).	3.	(B)	4	
		7.	(C)	5.	(B)	6	(D)	4	
	_		(A).	8.	(B)	9.	(D)	- ·	
		10.	(C)	11.	(B)	12.	(D)	-	
		13.	(A)	14.	(B)	15.	(C)	4	
		16.	(A)	17.	(D)	18.	(A)	_ · -	
		19.	(B)	20.	(C)				
	•			TEST	NO. 8	· 145			
	Complete the s	entences	by given cl	toices:		1.9			
	For Arshad, ar				er and pe	ncils were holy	obiects	to him.	
( <i>l</i>	Futile			, <i>, ,,</i> -	(B)	Fascinating	,		
c) _	Sacred				(D)	Superficial			
	Since there was	s adequa	ite grazing o	area for the			por	pulated.	
k)	Sparsely	-	0 0	,	(B)	Disproportio			
2)	Rustically				(D)	Inadequately			
	It istl	ıat stude	nts do not r	epay their i					
(Y	Laudable				(B)	Unfortunate	•		
C)	Unforgivable				(D)	Regrettable			
	The tapeworm		unple of	orga					
<b>(</b> )	Parasitic		<u>.</u>		(B)	Protozoan			
Ď.	Exemplary					Hospitable	• •		
	He said that th	ere was i	no coine ba	ck becausè					
<b>(</b> )	Palatable	, , , , , , ,	. Barring Str	on occambe	(B)	Peremptory			
j (	Premeditated				(D).	Revolutionar	v		
	Although his in	nitial suc	cess was	by t				of a famous ac	ctor.
	critics later acc	laimed I	iim as a sta	r in his owi	n riolu.				,
k)	Refuted				(B)	Superceded		4	
2)	Enhanced				(D)	Trivialized			
	That was an	a	ddition of tl	ris book	(**)				
()	Summarized		amenion of n	. is 200m	(B)	Abbreviated			
Ć	Shortened				(D)	Abridged			
-	Shy and hypoc.	hondriac	al Akbar w	สรามมะกามร์			ias bis i	character mad	le lu
	mosti	lawmake	r and practi	icina naliti	riuric ui Anu	puone gumern	153, 1115 €	multiple man	
<b>(</b>	Fervent		. una praen	icing point	(B)	Effective			
Ó	Unlikely				(D)	Gregarious			
-	The event came	o	as he had	nradicted.		Gregarious		·	
)	Up		_	premicien	 (B)	Off			
)	$_{\mathrm{By}}$				(D)	About			
	Moeen is	onno	Went voa n	uuet roenar			10		
)	Craven			insi respect	(B)	Redoubtable	.J.		
, )	Insignificant						r		
-	Now she feels t	lia falli.	a <b>.</b>	Line	(D)	Disingenuous	3		
)	Quarreling w			nım.	(D)	Oursel an		•	
)	Quarreling to				(B)	Quarrel on			
			¥		(D)	Quarreling a	gainst		
`	His answer was	s sucn _	1 ex	pected lum	_	т 11.			
)					(B)	Like			
)	Whieh				(D)	That			

\*

CC) Marginal  (C) Marginal  (D) Normal  Wooden surface was glued	AITC	De de la Colonia		250
5. Wooden surface was glued the steel surface.  (A) Within (B) Agains (C) Onto Into Into Into Into Into Into Into I	NIS	Carde Dogar's Unique Fully Solved "NEW 1ES	TING :	SYSTEM" GUIDE 259
5. Wooden surface was glued the steel surface.  (A) Within (B) Agains (C) Onto Into Into Into Into Into Into Into I	(C)	Marginal	(D)	Normal
(A) Within (B) Against (C) Onto (D) Into (C) Onto (D) Into (C) Onto (D) Into (C) Onto (D) Into (D) Into (D) Into (D) Into (D) Into (D) Into (D) Into (D) Intervention (D) Interv				Willian
CC   Onto   CD   Into				Against
6. His			. ,	_
(A) Offensive (B) Dilatory (C) Infamous (D) Confiscatory (A) Over (B) At (C) On (D) About (C) On (D) About (E) Valuable (D) Worthless (D) Worthless (E) Valuable (D) Worthless (D) Should not (C) Can (D) Should not (D)		•		
(C) Infamous  7. In the world of today, nuaterial values take precedence  A) Over  (B) At  (C) On  8. The supposedly impregnable defenses of the country's southern border became when the officer discovered that the defenses could be circumvented by an approach from the east.  (A) Useless  (B) Flexible  (C) Valuable  9. Work hard lest you fail.  (A) Will  (B) Should  (C) Can  (D) Should not  10. Usman is not attracted by the peripatetic life of the always wandering through the countryside.  (A) Vagabond  (B) Mendicant  (C) Almsgiver  (D) Philosopher  11. For Anna, each new school year was an experience, but her brother awaited the coming of attunum with dread.  (A) Exhausting  (B) Illuminating  (C) Exciting  (C) Exciting  (B) Philistine  (D) Exhilarating  (C) Chauvinist  (C) Chauvinist  (B) Philistine  (D) Dilettante  (C) Chauvinist  (D) Dilettante  (A) Reticent  (B) Make up of  (C) Altruistic  (D) Made up  15. The legal system of Russia can no longer regard itself as and standing apart from those of other countries.  (A) Receant  (B) Arbitrary  Independent  (C) Suppliant  (C) Suppliant  (D) Damaging  (B) Arbitrary  Independent  (C) Suppliant  (C) Suppliant  (D) Comen  (D) Reward		Offensive		
In the world of today, material values take precedence   Spiritual values.			• ,	_
(A) Over (B) About  (C) On (D) About  8. The supposedly impregnable defenses of the country's southern border became when the officer discovered that the defenses could be circumvented by an approach from the cust.  (A) Useless (B) Flexible  (C) Valuable (D) Worthless  9. Work hard lest you fall.  (A) Will (B) Should  (C) Can (D) Should not  10. Usman is not attracted by the peripatetic life of the head officent in the countryside.  (A) Vagabond (B) Mendicant  (C) Almsgiver (D) Philosopher  11. For Anma, each new school year was an experience, but her brother awaited the coming of auttumn with dread.  (A) Exhausting (B) Illuminating  (C) Exciting (D) Exhilarating  12. is a person who dabbles in art and letters.  (A) Philosopher  (B) Philistine  13. Faced with these massive changes, the government keeps its own counsil, although generally benevolent, it has always been regime.  (A) Acticent (B) Indifferent  (C) Altruistic (D) Unpredictable  14. Train is of different bogeys.  (A) Made of (B) Make up of  (C) Made with (B) Made up  15. The legal system of Russia can no longer regard itself as and standing apart from those of other countries.  (A) Damaging (B) Arbitrary Independent  (C) Binding (C) Binding (D) Litigant  15. The members of the religions sect ostracized the who had abandoned their faith.  (C) Suppliant (B) Called  (C) Cried ou (B) Called  (C) Cried ou (C) Cried ou (D) Shouted  (A) Threat (B) Fluke  (D) Comen (D) Reward				•
(C) On		· Over		
8. The supposedly impregnable defenses of the country's southern border became when the officer discovered that the defenses could be circumwented by an approach from the cast.  (A) Useless (C) Valuable (D) Worthless  9. Work hard lest you				
officer discovered that the defenses could be circumvented by an approach from the cast.  (A) Useless (B) Flexible (C) Valuable (D) Worthless  9. Work hard lest you fail.  (A) Will (B) Should (C) Can (D) Should not  10. Usman is not attracted by the peripatetic life of the always wandering through the countryside.  (A) Vagabond (B) Mendicant (C) Almsgiver (D) Philosopher  11. For Anna, each new school year was an experience, but her brother awaited the coming of attumn with dread.  (A) Exhausting (B) Illuminating (C) Exciting (D) Exhilarating  12 is a person who dabbles in art and letters. (A) Philosopher (B) Philistine (C) Chauvinist (D) Dilettante  13. Faced with these massive changes, the government keeps its own counsil, although generally benevolent, it has always been regime. (A) Reticent (B) Indifferent (C) Altruistic (D) Unpredictable  14. Train is of different bogeys. (A) Made of (B) Make up of (C) Made with  15. The legal system of Russia can no longer regard itself as and standing apart from those of other countries. (A) Damaging (B) Arbitrary (C) Binding (D) Independent  The members of the religious sect ostracized the who had abandoned their faith. (A) Recreant (B) Called (C) Cried out (D) Shouted  17. Saina my name from across the river. (A) Cried (C) Cried out (D) Shouted  18. After having worked in the soup kitchen feeding the hungry, the volunteer began to see her own good fortune as a (A) Threat (B) Fluke (C) Omen (D) Reward				
(A) Useless (C) Valuable (C) Valuable (D) Worthless  9. Work hard lest you	ŭ.			
(C) Valuable (D) Worthless  9. Work hard lest you fail.  (A) Will (B) Should (D) Should not  10. Usman is not attracted by the peripatetic life of the always wandering through the countryside.  (A) Vagabond (B) Mendicant (D) Philosopher  11. For Anna, each new school year was an experience, but her brother awaited the coming of autumn with dread.  (A) Exhausting (B) Illuminating (C) Exciting (D) Exhilarating  12 is a person who dabbles in art and letters.  (A) Philosopher (B) Philistine (C) Chauvinist (D) Dilettante  13. Faced with these massive changes, the government keeps its own counsil, although generally benevolent, it has always been regime.  (A) Reticent (C) Altruistic (D) Unpredictable  14. Train is of different bogeys.  (A) Made of (B) Make up of (C) Made with (D) Made up  15. The legal system of Russia can no longer regard itself as and standing apart from those of other countries.  (A) Damaging (B) Arbitrary  (C) Binding (D) Independent  (C) Suppliant (D) Litigant  17. Saina my name from across the river.  (A) Cried (C) Cried out (D) Shouted  18. After having worked in the soup kitchen feeding the hungry, the volunteer began to see her own good fortune as a (B) Fluke  (C) Omen (D) Reward	(A)	Useless		
9. Work hard lest you fail. (A) Will (B) Should (C) Can (D) Should not  10. Usman is not attracted by the peripatetic life of the always wandering through the countryside. (A) Vagabond (B) Mendicant (C) Almsgiver (D) Philosopher  11. For Anna, each new school year was an experience, but her brother awaited the coming of autumn with dread. (A) Exhausting (B) Illuminating (C) Exciting (D) Exhilarating  12 is a person who dabbles in art and letters. (A) Philosopher (B) Philistine (C) Chauvinist (D) Dilettante  13. Faced with these massive changes, the government keeps its own counsil, although generally benevolent, it has always been regime. (A) Reticent (B) Indifferent (C) Altruistic (D) Unpredictable  14. Train is of different bogeys. (A) Made of (B) Make up of (C) Made with (D) Made up  15. The legal system of Russia can no longer regard itself as and standing apart from those of other countries. (A) Damaging (B) Arbitrary (C) Binding (D) Independent (C) Suppliant (D) Litigant  17. Saima my name from across the river. (A) Cried (C) Cried (D) Shouted  18. After having worked in the soup kitchen feeding the hungry, the volunteer began to see her own good fortune as a (B) Fluke (C) Omen (D) Reward				
(A) Will (C) Can (D) Should not  10. Usman is not attracted by the peripatetic life of the			127	Workings
(C) Can			(R)	Should
10. Usman is not attracted by the peripatetic life of the always wandering through the countryside.  (A) Vagabond (B) Mendicant (C) Almsgiver (D) Philosopher  11. For Anna, each new school year was an experience, but her brother awaited the coming of autumn with dread.  (A) Exhausting (B) Illuminating (C) Exciting (D) Exhilarating  12 is a person who dabbles in art and letters. (A) Philosopher (B) Philistine (C) Chauvinist (D) Dilettante  13. Faced with these massive changes, the government keeps its own counsil, although generally benevolent, it has always been regime.  (A) Reticent (B) Indifferent (C) Altruistic (D) Unpredictable  14. Train is of different bogeys. (A) Madc of (B) Make up of (C) Made with (D) Made up  15. The legal system of Russia can no longer regard itself as and standing apart from those of other countries. (A) Damaging (B) Arbitrary (C) Binding (D) Independent (C) Suppliant (D) Litigant  17. Saina my name from across the river. (A) Cried (C) Cried out (D) Shouted  18. After having worked in the soup kitchen feeding the hungry, the volunteer began to see her own good fortune as a (A) Threat (B) Fluke (C) Omen (D) Reward		·	. ,	
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(A) Threat (B) Fluke (C) Omen (D) Reward		good fortune as a	g me n	ungry, the volumeer begins to bee not been
(C) Omen (D) Reward	(A)		(R)	Fluke

**(B)** 

(D)

\_\_\_\_\_, because he aspired to stand first in the examination.

Integrity

Sincerity

staffers, the new aid seemed very presumptuous.

**(A)** 

**(C)** 

Energy

Humility

He worked\_

(,

3

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	*					
13.	Or	D) And	-1.			
	In many countries, the proponents of a centrally to constitute a powerful political force.	ontrolled economy, altho	oagn in, continue			
(A)		B) Restart				
(C)	Disarray	D) Error				
14,	Ralieela spoke that it was applauded by a	!, *				
(A).		B) As well				
15.	Very well  Studded starfish are well protected from most	D) So well	ou surface whose			
1 ~ ~	studs are actually modified spines.	reuniors una parastics a	y surface whose			
( <u>A</u> )	A fragile	B) An obtuse				
(C)		D) A brittle				
16.	The committee censured the member, noting to conduct.	at his behaviour was th	e very of ethical			
(A)	Essence	B) Embodiment				
(C)	Nature	D) Antithesis				
17.	Stand here, I speak.					
(A)	While	B) As	, '			
18.	When We need more men of culture and enlightenmen	D) The time	амана ис			
(A)	Students	B) Philistines	_ uniong us.			
(C)	Philosophers	D) Visionaries				
19.	The successful of a novel or a poem requ	res fluency in two langua	iges.			
(A)	Publication Writing	B) Reproduction				
20.	Let us wait	D) Translation				
(A)	So little	B) Little				
(C)	A little	D) The little				
, ,	ANSWE	,				
	1. (A) 2.	(B) 3. (B)				
	4. <b>(D)</b> 5.	(C) 6. (A	)			
	7. <b>(C)</b> 8.	(A) 9. (D				
	10. (C) 11.	(B) 12. (C	)			
	13. <b>(B)</b> 14.	(D) 15. (C	)			
	16. <b>(D)</b> 17.	(A) 18. (B)				
	19. <b>(D)</b> 20.	(C)				
	TEST NO	. 11				
	ion: The following sentences are given with blanks	o be filled with prepositi	ons. Four alternatives are			
	sted. Choose the correct option.					
1.	The party had to struggle the wet grass f		reached dry land.			
	(A) along; before (B) through;	efore				
,	(C) across; till (D) along; un		I . I I I I'CC . I			
2.	the weight of the elephant the old brid	e collapsed, and the elep	nant had much difficulty			
:	getting the bank of the river.  (A) under; for; at (B) beneath;	m to				
	(A) under; for; at (B) beneath; (C) under; in; to (D) with; in;					
3.	I was dead time; you are the one who wa					
	(A) on; over (B) within; for	an noun				
	(C) in; for (D) on; by					
4.	half an hour all those who were trappe	the building v	vere rescued the			
	brave firemen.					
'	(A) within; near; by (B) before; w		•			
	(C) after; outside; with (D) within; in	ide; by				
5.	The man was measure rich, but he was _		the poor.			
	(A) beyond; for; for (B) within; w					
!	(C) without; for; to (D) beyond;	thout; for				

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1:

14

18

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	(4)	44	<b>(D</b> )	at a standard			
	(A)	•		action; intention			
6.	(C)	the church; the fro	(D)	crime; sin			
°		closer; further	nn Goa. (B)	nearer; farther			
		holier; nearer		greater; closer			
7.	The	is not steel, but it	(D)	greater, croser			
	(A)			word; pricks			
		mouth; hurts		mouth; eats			
8.		in cases of, deaths from					
				operations; rare			
			. ,	infection; frequent			
9.	Scient	tists and tracking down g	erms ha	ve shown in their fight against disease.			
	(A)	doctors; heroism	<b>(B)</b>	surgeons; boldness			
	(C)	dentists; courage	(D)	artists; skill			
10.	Hydro	gen balloons, which were much		surgeons; boldness artists; skill than hot-air balloons became very lighter; popular			
	(A)	smaller; cheap cheaper; fashionable	(B)	lighter; popular			
	(C)	cheaper, fasinonable	(D)	original, common			
11.		ea was coming after me as high a	s a great	t hill and as as a enemy.			
	(A)	furious; charging	(B)	dreadful; advancing			
				angry, attacking			
12.		s I looked about me in fear, I felt					
		quite; very		more; less			
1,	(C)	extremely; quite		less; more			
13.	Every	where, the Iron Horse replaced the	e living	g to pull trains carrying and goods.			
		animals; passengers	(B)	horses; passengers			
l 4 4	(C)	horses; labourers	(D)	horses; passengers animals; men			
14.	2011	horses; labourers ne are and some are wise; otherwise		clever; cheats			
		foolish; stupid	(D)	good; saintly			
15.							
'`	(A)	to hell is with goo road; made	(B)	highway; lined			
	, ,	road; paved	• 4	path; filled			
	(-)	. van-, parva	(20)	Panis antes			

## **ANSWERS**

1.	(B)	2.	(C)	3.	(D)	4.	(D)	5.	(D)
6.	(B)	7.	(A)	8.	(B)	9.	(A)	10.	(B)
11.	(A)	. 12.	(B)	13.	(B)	14.	(A)	15.	(C)

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T

2.



The word analogy means "an agreement or correspondence in certain respect between things otherwise different ---- a resemblance of relations, as in the phrase, "knowledge is to the mind, what light is to the eye": relation in general: likeness: correspondence of a word or a phrase with the genius of a language, as learned from the manner in which its words and phrases are ordinarily formed: similarity of derivative or inflectional processed."

The Urdu meaning of the word analogy is

Example 1: interesting the missing word.

Days is to night as truth is to falsehood.

Answer: In the above sentence, the word falsehood has been inserted.

Example 2: which choice gives the answer?

1. Man is to run as bird is to

Choices: (i) fly, (ii) run, (iii) weak.

Answer: (i)

Example 3: ring is to finger as watch is to \_\_\_\_\_

Choices: (i) arm, (ii) wrist, (iii) leg.

Answer: (ii)

#### TYPES OF ANALOGY TESTS

First Type: The first type is that in which two words which have some relationship with each other are presented. These are followed by another word and a number of choices. One word from the choices is to be picked up to establish the same relation with the third word as the first two have. For example----

Day is no Night as Cold is to?

(A) Ice

(B) Wet

(C) Warm

(D) Snow

The correct answers is (C).

Day and Night bear the relation of the opposites. As cold is opposite of warm.

Second Type: Part relationship---- In this type of relationship, the two words represent the parts of a bigger thing. For example----

Lyric is to Ode as

Head is to legs

Sky is to earth

Bomb is to science

Newspaper is to journalist

The correct answer is (A).

In the above quoted example, Lyric and Ode are two types of poems. Similarly, head and legs are two parts of the human body.

Third Type: Another type of analogy is in which one of the four relationship element is not given. One out of the choices is selected. Example----

Ship is to Fish as

(A) Kite

(B). Feather

(C) Tree

(D) Chirp

is to bird

The correct answer is (A).

Explanation ---- Both ship and fish are found in water. This is the relationship between the two words. For bird, we will have to pick up kite because both are seen in air.

#### HOW TO ATTEMPT THIS QUESTION

Step One --- Establish the relationship between the first two words.

Step Two ---- Find the same relationship among the choices which follows the pattern of the two words.



### KINDS OF RELATIONSHIP

		di ibb di italiitidi bilik	
<i>I</i> .	Purpose relationship Exam	uple Glove: Balls as	
	(A) Hook: Fish	(B) Winter: Weather	
	(C) Games: Sports	(D) Stadium: Seats	
The co	rrect answer is (A)		
		elp in catching the ball and the purpo	ose of hook is to catch fish. Th
correct	answer is (A)		
2.		_Example Race: Fatigue as:	•
	(A) French: Athlete	` '	•
	(C) Art: Bug	(D) Walking: Running	
		suse fatigue is the effect of race; hunger	r is the effect of fast.
<i>3</i> .	Part whole relationshipEx	- <del>-</del>	
	(A) Patch: Thread	(B) Removal: Snow	4.5
	(C) Struggle; Wrestle	(D) Hand; Clock	
4.		action relationship, Examples	
	A. Kick: Football:		
	(A) Kill: Bomb	(B) Break; Pieces	•
	(C) Question: Team	(D) Smoke: Pipe	,
	B. Steak: Broil:		
	(A) Bread: Bake	(B) Food: Sell	
	(C) Wine: Pour	(D) Sugar: Spill	
		all the object of action. This very relat	ionship is represented in (D) i.e
smokir	ng is action and pipe is the objec	t. For B answer is (A).	
<i>5</i> .	Synonym relationship—		e e
Enorm	ous: Huge as		
	(A) Rough: Rock	(B) Muddy: Unclear	
	(C) Purse: Kitchen	(D) Black. White	
	The correct answer is (B) beca	use "muddy" and unclear are synonym	s.
6.	Antonym relationship-Exam	uple	
	Purity: Evil as		
	(A) Suavity: Bluntness	(B)'North: Climate	•
	(C) Angle: Horns	(D) Boldness: Victory	
	The correct answer is (A) beca	use the two words are antonyms.	
7.	Place relationship—Example	- Faisal Mosque: Islamabad as	
	(A) Red Square: Moscow		
	(C) India: Madras	(D) Pakistan: Nepal	
	Faisal Mosque is situated in Is	lamabad so is Albany in New York.	
8.	Degree relationship-Examp		
	(A) Glue: Paste	(B) Climate: Weather	
	(C) Bright: Genius	(D) Frown: Anger	
	Warm is less hot and frown is		
9.	Sequence relationshipSpri		
	(A) Thursday: Wednesday		
	(B) Wednesday: Monday		_
	(C) Monday: Wednesday	•	
	(D) Wednesday: Thursday	•	
	· · · · · · · · · · · · · · · · · · ·	does Thursday after Wednesday.	
<i>10</i> .	Association relationship—Ex	•	
,	(A) Colour: Sidewalk	(B) Slipper: State	
	(C) Ink: Writing	(D) Picture: Bed	
		gs so ink is associated with writing.	
11. Gr	ammatical relationship— Exai		
	(A) Segregation: See	(B) Nymph: In	

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(C) Room: Although

(D) Run: See

Restore and climb are verbs so are run and see.

# EXAMPLES WITH EXPLANATORY ANSWERS

Example 1 BRIM: HAT::

(A) hand: glove

(B) spoke: umbrella

(C) skirt: hem

(D) snood: hood

(E) lace: shoe

Answer: The correct answer is (E)

What is the relationship between BRIM AND HAT? A brim is a part of a hat, so the relationship is that of part to whole. The next step is to examine the answer choices to find another pair of words which bear the same relation to each other. Consider each answer choice in turn.

(A) A hand is not a part of a glove, so eliminate (A).

(B) A spoke is part of an umbrella, so (B) is a likely choice. But don't mark your answer yet. You must always look at all five choices before making your final decision.

(C) A hem is part of a skirt, but BEWARE. The relationship in (C) is whole (the skirt) to part (the hem), which is the reverse of the initial relationship. Your answer must maintain the same relationship in the

same sequence as the original pair. Eliminate (C).

(D) If you know that a snood is a hair net, you can see that snood, hood, and hat are all headgear. However, a snood is not a part of a hood, so (D) is incorrect. If you do not know the meaning of one word among the choices, do not fall into the trap of choosing that answer just because it's unfamiliar. Consider all the choices earefully before you mark an unknown answer as correct.

(E) A lace is a part of a shoe, so (E) appears to be a perfectly good answer.

Having found two likely answers, (B) and (E), you must go back to the original pair and determine its other distinguishing characteristics. A brim is a part of a hat, but it is not a necessary part. Not all hats have brims. A lace is a part of a shoe, but it is not a necessary part. Some shoes have buckles and some are slip-ons. A spoke, however, is a necessary part of an umbrella. Furthermore, a brim is a part of a hat, which is wearing apparel. A lace is part of a shoe, which is also wearing apparel. But an umbrella is not something to wear. Thus there are two counts on which to eliminate (B) and to choose (E) as the best answer.

Usually, the problem with analogies is refining the relationship to find the best answer. Sometimes, however, the difficulty will be in finding even one correct answer. If this happens, you may have to redefine the relationship. Consider an analogy which begins LETTER: WORD. You first thought is probably that a ictter is part of a word, and so you look for an answer choice that shows a part-to-whole relationship.

However, suppose the question looks like this:

Example 2. LETTER: WORD::

(A) Procession: Parde

(B) Dot: Dash

(C) Whisper: Orate

(D) Song: Note

(E) Spell: Recite

Answer: The correct answer is (D).

Not one of these choices offers a part-to-whole relationship. Returning to the original pair, you must then consider other relationship between letter and word. If letter is not "letter of the alphabet," but, rather, "written communication," then a word is part of a letter and the relationship becomes that of the whole to its part. Now the answer is immediately clear. A song is the whole of which a note is a part. Example 3. PILOT: STEER::

(A) Chef: Dine

(B) Boss: Obey

(C) Lawyer: Retain

(D) Guard: Protect

Answer: The correct answer is (D)

At first glance several of these answers may seem to work. "A pilot is someone who steers." "A soldier is someone who is commanded." The relationship looks promising, but it's not correct. Ask yourself who is doing what to whom? In the original pair, the pilot is doing something: the pilot is steering. The choices B and C: a boss is someone who is obeyed: a lawyer is someone who is retained (hired). Again, the original grammatical relationship is reversed.

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By definition, a pilot is a person who steers. In the same way, by definition, a guard is a person who protects. **Example 4.** INTERLOPE: INTRUSION:

(A) Witness: Interrogation(C) Recluse: Interference

(B) Actor: Intermission(D) Mediator: Intercession

Answer: The correct answer is (D).

Again, ask yourself who is doing what to whom. An interloper is a person who butts in or thrusts himself into the business of others. An interloper commits an intrusion; he or she intrudes. A witness, on the other hand, is not the person who conducts the interrogation. A witness is the person who is being interrogated.

You can eliminate choice (A) and any other answer choices in which the original relationship is reversed. The mediator or go-between is the person who acts, trying to reconcile quarrelling parties by means of intercession.

Example 5. CONSTELLATION: STARS::

(A) Prison: Bars

(B) Assembly: Speaker

(C) Troupe: Actors

(D) Mountain: Pcak

Answer: The correct answer is (C)

A constellation is made up of stars. A troupe (not troop but troupe) is made up of actors. Choice C is correct.

Note, by the way, the characteristics of the analogy you have just analyzed, CONSTELLATION: STARS. It is a good analogy. The relationship between the words is built-in; if you look up constellation in a dictionary, you will see that a constellation is a group of stars. The words are related by definition.

Your correct answer choice has got to have the same characteristics as the original pair. The words must have a clear relationship. They must be related by definition. If you substitute them in your test sentence, they must fit it exactly.

Example 6. FISH: TROUT::

(A) Ocean: Wave

(B) Mammal: Whale

(C) Bird: Aviary

(D) Antenna: Insect

Answer: The correct answer is (B)

A trout is a kind of fish. A whale is a kind of mammal. (Class and Members)

Example 7. DIMMED: LIGHT::

(A) Beached: Texture

(B) Muffled: Sound

(C) Measured: Weight

(D) Tragrant: Smell

Answer: The correct answer is (B)

Light that is dimmed is lessened in brightness. Sound that is muffled is lessened in volume.

Example 8. DOCTOR: DISEASE::

(A) Moron: Imbecility(B) Pediatrician: Senility

(C) Psychiatrist: Maladjustment

(D) Broker: Stocks

Answer: The correct answer is (C)

A doctor attempts to treat a disease. A psychiatrist attempts to treat a maladjustment.

Example 9. PATRON: SUPPORT::

(A) Spouse: Divorce

(B) Restaurant: Management

(C) Counselor: Advice

(D) Host: Hostility

answer: The correct answer is (C). A patron by definition provides patronage or support. A counselor by definition provides advice.

Example 10. CLOCK: TIME::

(A) Watch: Wrist

(B) Odometer: Speed

(C) Hourglass: Sand

(D) Yardstick: Distance

Answer: The correct answer is (D)

A clock measures time. A yardstick measures distance (Function).

The candidate should know about the different types of analogies that are more frequently asked in the question paper. Some of the common analogy types are as follows:

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### i. Synonyms:

Some words are linked together in a pair which means the same or has a similar dictionary definition e.g., Large-Big.

### ii. Describing Qualities:

Some pairs have some words in which one word describes the other word, e.g., Hot-Iron.

#### iii. Class and Member:

Some pairs have words which are based on class and member basis, e.g., Vehicle-Car

#### iv. Antonyms:

Some pairs consist of the words that are opposite to each other, e.g., Confess-Deny.

### v. Describing Intensity:

Some pairs eonsist of the words in which one describes the intensity of the other, e.g., Anger-Rage (violent anger).

#### vi. Function:

In some pairs, a word describes the function of the other word, e.g., Football-Pay.

#### vii. Manners:

Some words in a speech describe the manners and behavior e.g., Weep-Bitterly,

### viii. Worker-Workplace

Some pairs in a word describe the profession and its workplace, e.g., Teacher-Class.



### TEST-1

Directions: In the following questions, select the pair of words given against (A), (B), (C) or (D) which has the same relation as between the first two words.

same	e relation as be	etween the first two words.		± (1,7,1,7,1,7,1,1,1,1,1,1,1,1,1,1,1,1,1,1
1.	VERITY:	CASUISTRY::		
	(A)	Egalitarian: Equality	(B)	Sweet: Mellifluous
1.	(C)	Constant: Capricious	(D)	Milk: Cream
2.		NGENUE;;	(2)	TAMES OF CHILIF
	(A)	Ordinary: Genius	(B)	Venerable: Celebrity
	(C)	Urbane: Sophisticate	(D)	Crafty: Artisan
3.		CORRAL::	(-)	o. o. o. o. o. o. o. o. o. o. o. o. o. o
	(A)	Oyster: Reef	(B)	Dog: Muzzle
1.	(C)	Sheep: Flock	(D)	Pig: Sty
4.		LCOHOL::	(-·)	83.9
1	(A)	Cream: Milk	(B)	Canteen: Water
١.	(C)	Tanker: Oil	(D)	Octane: Gasoline
5.		E: RELIGION::	<b>(</b> -)	S. C. C. C. C. C. C. C. C. C. C. C. C. C.
	(A)	Potentate: Kingdom	(B)	Traitor: Country
	(C)	Bureaucrat: Government	(D)	Jailer: Law
6.	ANIMAL.	MONKEY::	(~-)	
	(A)	Zebra: Giraffe	(B)	Stationery : Pencil
	(C)	Book: Cap	(D)	Tree: Wood
7.	MARATHO	ON: STAMINA::	(D)	Hee, wood
	(A)	Relay: Independence	<b>(D)</b>	Hundley December
	(C)	Sprint: Celerity	(B)	Hurdle: Perseverance
8.		DISTANT::	(D)	Jog: Weariness
	(A)	Mourn: Lost	4	
	(C)	Discern: Subtle	(B)	Whisper: Muted
9.	FOX: CUN		(D)	Destroy: Flagrant
	(A)			
		Dog: Playful	<b>(B)</b>	Hyena: Amusing
10.	(C) HOUSE : E	Beaver: Industrious	(D)	Vixen: Cute
	(A)	Home : Live		i
	(A)	DOME : Live	(B)	School: Daily

Inveigh: Inveigle

Ocean: Bay

**(B)** 

**(D)** 

the same relation as between the first two words:

Lunch: Dessert

Affluence: Poverty

Forest: Jungle

Oasis: Desert

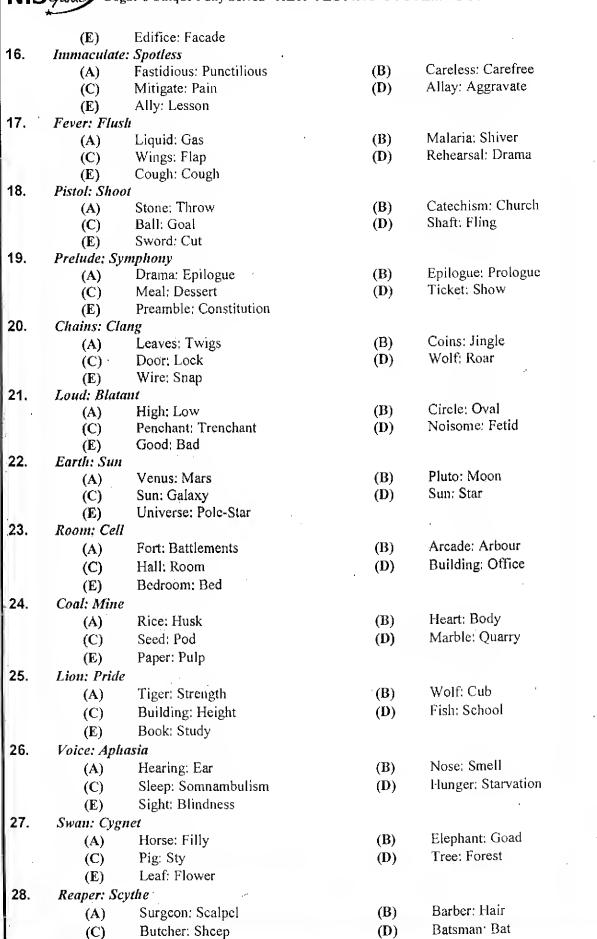
(A)

(C)

**(E)** 

		<u> </u>			
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2.	Sad: Mor	ose	<b>,</b>		
	(A)	Robust: Weak	(B)	Ingress: Egress	16.
	(C)	Grass: Food	(D)	Glad: Happy	
3.	Work: Ti	red	(- )	x	
	(A)	Player: Field	(B)	Swim: Pool	
	(C)	Race: Fatigue	$(\mathbf{D})$	Book: Knowledge	17.
	(E)	Cook: Eat			-5
4.	Thiu: Spa				59 -
	(A)	Tract: Tome	(B)	Prologue: Epilogue	· ·
	(C) (E)	Preface: Book	(D)	Tree: Tall	18.
5.	Sad: Mela	Corpulent: Obese			
٥,	(A)	Over: Under	<b>(T)</b>		2.0
	(A) (C)	Weak: Robust	(B)	Joy: Ecstasy	1 40
	(E)	Floor: Ceiling	(D)	Book: Writer	19.
6.	Flurry: C				11.7
Ĭ	(A)	Water: Thirst	(II)	Mi-La Cl	1 1
	(C)	Colour: Attraction	(B)	Night: Sleep	20.
	(E)	Intimidate: Fear	(D)	Job: Pay	20.
7,	Turbid: M				
	(A)	River: Lake	(B)	Tree: Darkness	k i Y
	· (C)	Bell: Ring	(D)	Huge: Colossal	21.
'	(E)	Deep: Shallow	(D)	Tuge, Colossai	1 1 1 7 1
8.	Fresh: Ne			1	
	(A)	Disease: Malaise	(B)	Supercilious: Meek	
	(C)	Epical: Humorous	(D)	Indigent: Affluent	22.
	<b>(E)</b>	Strident: Polite	<b>V y</b>		
9.	Wheel: H	ub			
	(A)	Sea: Island	(B)	Body: Heart	
	(C)	Ruling Party: Cabinet	(D)	Life: Happiness	23.
40	(E)	Watch: Needle	• •		
10.	Speech: P				
	(A)	Dinner: Dessert	(B)	Country: Boundary	
	(C)	Argument: Conclusion	(D)	Style: Debate	24.
11.	(E)	Money, House			1 1
١١.	Death: La.				1 4
	(A)	Impose: Fine	(B)	Cast: Vote	1 1
	(C) (E)	Make: Furniture Learn: Lesson	(D)	Celebrate: Centenary	25.
12.	Virus: Dis				1 1 - 4.
	(A)	Discussion: Fight	(T)		11.11
	(C)	Suggestion: Acceptance	(B)	Desire: Success	
	(E)	Clothes: Gentleman	(D)	Bombardment: Destruction	26.
13.	Foot: Toe	ciones, Gendeman			20.
	(A)	Body: Legs	(B)	Belly: Intestines	
	(C)	Nail: Fingers	(D)	Hand : Fingers	11.1
	(E)	Leaves: Tree	(D)	Tand : Tingors	1 1 27
14.	Zenith: Na				27.
	(A)	Serious: Sober	(B)	Food: Hungry	HILL
	(C)	Fat: Protein	(D)	Majestic: Sublime	PH
	<b>(E)</b>	Peak: Foot	(2)	g-sur-, o-gorinio	
15.	Giggle: Ch				28.
	(A)	Smile: Grin	(B)	Melancholy: Antipathy	- A
	(C)	Emancipation: Bondage	(D)	Insipid: Charming	

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Society: C	Ostracise		
(A)	Family: Member	(B)	Zoo: Animal
(C)	Judge: Order	(D)	Government: Exile
Wolf: Cut	$oldsymbol{b}$ .		:
(A)	Old Man: Young Man	· (B)	Forest: Trce
(C)	Parliament: Cabinet	(D)	Swan: Cygnet
<b>(E)</b>	Book: Booklet		
Speak: Sl	tout		
(A)	Whimper: Bang	(B)	Silence: Whisper
(C)	Gallop: Stop	(D)	Eat: Digest
<b>(E)</b>	Word: Sentence	,	Ü
Friend: L	ove		
(A)	Enemy: Hate	(B)	Woman: Marry
(C)	Officer: Defied	(D)	Leader: Hear
(E)	Neighbour: Talk	, ,	
Cool: Lik	ed		
(A)	Cold: Disliked	(B)	Hot: Welcomed
(C)	Truth: Hidden	(D)	Weather: Pleasant
(E)	Question: Solved	` /	
	Expensive		
(A)	Expand: Expansive	(B)	Deceive: Deception
(C)	Defend: Intrusive	(D)	Think: Pensive
(E)	Sensitive: Obstrusive	(~)	
Watch: W			
(A)	Clock: Time	(B)	Room: Sitting
(C)	Success: Work	(D)	Ornaments: Decoration
(E)	Grain: Field	(-)	,
Bulb: Śoc			
(A)	Pen: Inkpot	(B)	Necklace: Neck
(C)	Foot: Knee	(D)	Eye: Socket
(E)	Hair: Scalp	(2)	
Aeroplan	-		•
(A)	House: Mason	(B)	School: Principal
(C)	Assembly: Speaker	(D)	Car: Chauffeur
(E)	Machine: Engineer	(5)	The result of the second second second second
(~)		SWERS	
	AN	SYLKS	

		-							
1.	(E)	2	(D)	3.	(C)	4.	(E)	5.	(B)
6.	(E)	7.	(D)	8.	(A)	9.	(C)_	10.	(C)
11.	(D)	12.	(D)	13.	( <b>D</b> )	14.	(E)	15.	(A)
16.	(A)	17.	(B)	18.	(D)	19.	<b>(E)</b>	20.	(B)
21.	(D)_	22.	(C)	23.	(C)	24.	(D)	25.	(D)
26.	(E)	27.	(A)	28.	(A)	29.	<b>(D)</b>	30.	(A)
31,	(B)	32.	(A)	33.	(C)	34.	(A)	35.	(E)
36.	(C)	37.	(C)	38.	(B)	39.	(D)	40.	(E)
41.	(A)	42.	(D)	43.	(D)	44.	(A)	45.	(A)
46.	(A)	47.	(A)	48.	(B)	49.	(D)	50.	(D)

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# SYNONYM/ANTONYM TESTS

**Directions.** In the following questions, each word is followed by four responses a, b, c and d. You should choose the correct synonym of the given word out of the four choices.

You	should choose the correc	t synonym	of the given word out of the four choices.
1.	Abandon:		
	(A) vacate	(B)	foil
1	(C) lose	(D)	gain
2.	Abdicate :		
	(A) give up	(B)	imperious
	(C) rude	<i>(D)</i>	dissent
3.	Abhor:		
	(A) crave	(B)	reconcile
	(C) detest	(D)	rude -
4.	Abnegation:		
	(A) indulgence	(B)	rejection
,	(C) complete	(D)	final
5.	Axiom:		
	(A) absurdity	(B)	shirk
	(C) elude	(D)	maxim
6.	Bloated:		
	(A) privileged	<b>(B)</b>	emaciated
	(C) swollen	(D)	rapture
7.	Blemish:		
	(A) disgrace	<i>(B)</i>	cecentrie
	(C) young	(D)	fair
8.	Bizzare :		
	(A) normal	(B)	strange
	(C) logical	(D)	tense
9.	Bawl:		
	(A) mulberry	<i>(B)</i>	mutter
	(C) vociferate	(D)	daub
10.	Bequeath:		
	(A) alienate	(B)	stab
	(C) obstruct	(D)	dispose of
11.	Cataclysm :		
	(A) reverse	(B)	upheavel
	(C) pungent	(D)	trash
12.	Cupidity:		
	(A) extravagance	(B)	shrewd
	(C) complaisant	(D)	avarice
13.	Cumbersome:		
	(A) awkward	<b>(B)</b>	analyse
14	(C) decay	<i>(D)</i>	grow
14.	Culmination:	490.1	
	(A) nadir	(B)	apex

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	(C) lenient	(D)	blast
<i>15</i> .	Crestfallen:		
	(A) humiliated		hard
	(C) elite	( <b>D</b> )	frustrated
<i>16</i> .	Deluge:		
	(A) flood	<b>(B)</b>	object
_	(C) annihilate	(D)	restore
<i>17</i> .	Dereliction:		
	(A) attention	=	neglect
	(C) divorce	(D)	restore
18.	Derogate :	•	
	(A) exaggerate	<i>(B)</i>	calm
	(C) deflenerate	(D)	ordain
<i>19</i> .	Dorniant:		
	(A) active	(B)	vigilant
	(C) warbling	(D)	inert
20.	Don:		
	(A) doff	<i>(B)</i>	assume
	(C) pine		blithe
21.	Exemplify:		
	(A) reprehensible	(B)	illustrate
	(C) empty	(D)	
22.	Entramel:	` /	
	(A) hamper	(B)	extricate
	(C) apathy	(D)	
23.	Entendation:		
	(A) irritant	(R)	stoicism
	(C) barren	(D)	
24.	Elude:	(2)	TOURING
	(A) evade	(B)	rule
	(C) sway	(D)	fascinate
25.	Exudation:	(1)	rascinate
	(A) aridity	(B)	ecstasy
	(C) percolation		•
26.	Frivolous:	(D)	HOITIG
20.		(D)	4
	(A) scrious	(B)	
27.	(C) peculiar Furtive:	(D)	candid
47.		(D)	
	(A) public	(B)	open
20	(C) secretive	(D)	combine
28.	Fugitive:	, <b>-</b> .	
	(A) escaping	(B)	enduring
30	(C) vain	(D)	weak
29.	Fulminate:		
	(A) clamour	<b>(B)</b>	misfire
	(C) barren	(D)	prodigal

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Bewitch:

*Bauble :* (A) pla

disenchant

plaything

modest

profit

(B)

(D)

(B)

(D)

rapture

valuable

besiege

avail

(A)

(C)

(C)

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	*****		
45.	Busy:		
	(A) bully	(B)	curb
	(C) indolence	(D)	_
46.	Celebrity:		•
5	(A) celebration	(B)	solemnity
र्च : १	(C) obscurity	(D)	-
47.	Cataclysm:		
	(A) peace	(B)	deluge
	(C) quibble	(D).	~
48.	Concord:	1-7	g
4.	(A) consolidate	(B)	bestow
<u> </u>	(C) outline	(D)	
49.	Compliance:		
R	(A) condone	(B)	clamour
\$ 5	(C) resistance	(D)	condense
50.	Circumlocution:		
1	(A) amass	(B)	ambiguity
ξ <u></u>	(C) effusion	<b>(D)</b>	simplicity
5 <i>1</i> .	Despicable :		
÷	(A) worthy	(B)	
len	(C) earn	(D)	purity
<i>52</i> .	Ductile:		
3	(A) indistinct	•	vague
<i>53</i> .	(C) inelastic	<i>(D)</i>	quiescent
33.	Dormant:	ZD.	1 00
7	(A) Inert (C) indulgence	(B)	
54.	Dissipate:	(D)	active
	(A) accumulate	(B)	distil
	(C) percolate	(D)	emanate
55.	Disdain :	(2)	omanate
1	(A) haughtiness	(B)	erroncous
	(C) respect	(D)	contempt
56.	Ephemeral :	(2)	contempt
ľ	(A) transient	<b>(B)</b>	perpetual
Y	(C) disencumber	(D)	demote
<i>57</i> .	Erudition:		
1	(A) ignorance	<b>(B)</b>	evict
	(C) scholarship	(D)	dubious
58.	Exultation:		1
	(A) ecstasy	(B)	frugality
	(C) mourning	(D)	severe
<i>59</i> .	Expunge:		
	(A) erase	(B)	dilate
1	(C) entity	(D)	imprint
60.	Extenuate:		
	(A) palliate	(B)	quality
	(C) enhance	(D)	offhand
	. ,	(2)	Jilliana .

61. Flux:

> (A) stillness

(B) motion

swerve (C)

wince (D)

 $b_2$ 

Fatigue: (A) vitality

(B) weariness

(C) solemn (D) enchant

63. Fume:

> (A) frown

(B) chafe

(C) comply (D) dupe

64. Fugitive:

> (A) evanescent

**(B)** captive

(C) unkempt

smart (D)

65. Fulminate:

> (A) murmur

clamour (B)

efficacious (C)

vain (D)

Gallant: 66.

> (A) bold

fine **(B)** 

(C) frolic **(D)** coward

67. Garrulity:

> (A) reticence

**(B)** gaudy

(C) superb

abettor (D)

68. Generous:

> (A)magnanimous

visual **(B)** 

vivid (C)

(D) stingy

69. Genuine:

> (A) real

voracious (B)

(C) spurious

insincere (D)

70. Germinate:

> shoot (A)

(B) sprout

(C) alien

decay (D)

#### **ANSWERS**

(A)	2	(A)	3	(C)	4	(B)	5	(D)_
(C)	7	(A)	8	(B)	. 9	(C)_	10	(D)
(B)	12	(D)	13	(A)	14	(B)	15	(D)
(A)	17	(B)	18	(C)	19	(D)	20	(B)
(B)	22	(A)	23	(D)	24	(A)	25	(C) _
(B)	27	(C)	28	(A)	29	(A)	30	<i>(D)</i>
(C)	32	(B)	33	(C)	34	(D)	35	(B)
<i>(B)</i>	37	(A)	38	(C)	39	(D)	40	(B)
(A)	42	(D)	43	(A)	44	(B)	45	(C)
(C)	47	(A)	48	(D)	49	(C)	50	(D)
(A)	52	(C)	53	(D)	54	(A)	55	(C)
(B)	57	(A)	58	(C)	59	(D)	60	(C)
(A)	62	(A)	63	(C)	63	(B)	65	(A)
(D)	67	(A)	68	(D)	69	(C)	. 70	(D)
	(C) (B) (A) (B) (C) (B) (A) (C) (A) (C) (A) (B) (A)	(C)     7       (B)     12       (A)     17       (B)     22       (B)     27       (C)     32       (B)     37       (A)     42       (C)     47       (A)     52       (B)     57       (A)     62	(C)         7         (A)           (B)         12         (D)           (A)         17         (B)           (B)         22         (A)           (B)         27         (C)           (C)         32         (B)           (B)         37         (A)           (A)         42         (D)           (C)         47         (A)           (A)         52         (C)           (B)         57         (A)           (A)         62         (A)	(C)         7         (A)         8           (B)         12         (D)         13           (A)         17         (B)         18           (B)         22         (A)         23           (B)         27         (C)         28           (C)         32         (B)         33           (B)         37         (A)         38           (A)         42         (D)         43           (C)         47         (A)         48           (A)         52         (C)         53           (B)         57         (A)         58           (A)         62         (A)         63	(C)         7         (A)         8         (B)           (B)         12         (D)         13         (A)           (A)         17         (B)         18         (C)           (B)         22         (A)         23         (D)           (B)         27         (C)         28         (A)           (C)         32         (B)         33         (C)           (B)         37         (A)         38         (C)           (A)         42         (D)         43         (A)           (C)         47         (A)         48         (D)           (A)         52         (C)         53         (D)           (B)         57         (A)         58         (C)           (A)         62         (A)         63         (C)	(C)         7         (A)         8         (B)         9           (B)         12         (D)         13         (A)         14           (A)         17         (B)         18         (C)         19           (B)         22         (A)         23         (D)         24           (B)         27         (C)         28         (A)         29           (C)         32         (B)         33         (C)         34           (B)         37         (A)         38         (C)         39           (A)         42         (D)         43         (A)         44           (C)         47         (A)         48         (D)         49           (A)         52         (C)         53         (D)         54           (B)         57         (A)         58         (C)         59           (A)         62         (A)         63         (C)         63	(C)         7         (A)         8         (B)         9         (C)           (B)         12         (D)         13         (A)         14         (B)           (A)         17         (B)         18         (C)         19         (D)           (B)         22         (A)         23         (D)         24         (A)           (B)         27         (C)         28         (A)         29         (A)           (C)         32         (B)         33         (C)         34         (D)           (B)         37         (A)         38         (C)         39         (D)           (A)         42         (D)         43         (A)         44         (B)           (C)         47         (A)         48         (D)         49         (C)           (A)         52         (C)         53         (D)         54         (A)           (B)         57         (A)         58         (C)         59         (D)           (A)         62         (A)         63         (C)         63         (B)	(C)         7         (A)         8         (B)         9         (C)         10           (B)         12         (D)         13         (A)         14         (B)         15           (A)         17         (B)         18         (C)         19         (D)         20           (B)         22         (A)         23         (D)         24         (A)         25           (B)         27         (C)         28         (A)         29         (A)         30           (C)         32         (B)         33         (C)         34         (D)         35           (B)         37         (A)         38         (C)         39         (D)         40           (A)         42         (D)         43         (A)         44         (B)         45           (C)         47         (A)         48         (D)         49         (C)         50           (A)         52         (C)         53         (D)         54         (A)         55           (B)         57         (A)         58         (C)         59         (D)         60           (A)

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#### COMPREHENSION

#### Introduction:

Comprehension means the act of comprehending or the capacity of the mind to understand. In the examination papers, questions on comprehension test are included to judge the ability of the students to understand the given passage.

In the English language paper, questions on comprehension test are very important for the students appearing in the competitive examinations. Therefore, they should try to learn how to solve these questions. Practice of solving these questions will greatly help them in the examination.

# LONG PASSAGE COMPREHENSION PASSAGES WITH EXPLANATORY ANSWERS

#### PASSAGE - 1

The Romans – for centuries is the masters of war and politics across Europe, Northern Africa, and Asia Minor – have often been criticized for producing few original thinkers outside the realm of politics. This criticism, while in many ways true, is not without its problems. It was, after all, the conquest of Greece that provided Rome with its greatest influx of educated subjects. Two of the great disasters in intellectual history – the murder of Archimedes and the burning of Alexandria's library – both occurred under Rome's watch. Nevertheless, a city that was able to conquer so much of the known world could not have been devoid of the creativity that characterizes so many other ancient empries.

Engineering is one endeavour in which the Romans showed themselves capable. Their aqueducts carried water hundreds of miles along the tops of vast areades. Roman roads built for the rapid deployment of troops, criss-cross Europe and still form the basis of numerous modern highways that provide quick access between many major European and African cities. Indeed, a large number of these cities owe their prominence to Rome's economic and political influence.

Many of those major cities lie for beyond Rome's original province, and Latin-derived languages are spoken in most Southern European nations. Again a result of military influence, the popularity of Latin and its off spring is difficult to overestimate. During the centuries of ignorance and violence that followed Rome's decline, the Latin language was the glue that held together the identity of an entire continent. While seldom spoken today, it is still studied widely, if only so that such master or rhetoric as Cicero can be read in the original.

It is Cicero and his like who are perhaps the most overlooked legacy of Rome. While far from being a democracy, Rome did leave behind useful political tool that serve the American republic today. "Republic" itself is Latin for "the people's business," a notion cherished in democracies worldwide. Senators owe their name to Rome's class of elders; Representatives owe theirs to the Tributes who seized popular prerogatives from the Senatorial class. The veto was a Roman notion adopted by the historically aware framers of the Constitution, who often assumed pen names from the lexion of Latin life. These accomplishments, as monumental as any highway or coliseum, remain prominent features of the Western landscape.

# Multiple Choice Questions (MCQs)

- 1. The author describes "two of the great disasters in intellectual history" in order to
  - (A) establish a point directly related to the main argument
  - (B) show that certain historical claims are inaccurate
  - (C) demonstrate the importance of certain historical data
  - (D) disprove the claims made by other with a different view
  - (E) concede the partial accuracy of an opposing view
- 2. According to the passage, ancient Roman roads
  - (A) connected many major cities in ancient Europe
  - (B) are engineering marvels unequalled in modern times
  - (C) are similar in some respects to modern highways

- (D) were products of democratic political institutions
- (E) caused the development of modern European cities
- 3. According to the passage, which of the following accurately describes the Latin language?
  - I. It spread in part due to Rome's military power
  - II. It is reflected in modern political concepts
  - III. It is spoken today in some parts of Europe
    - (A) I only

(B) II only

(C) I and II only

(D) I and III only

- (E) II and III only
- 4. It can be inferred from the passage that the framers of the Constitution
  - (A) were familiar with certain aspects of Roman government
  - (B) were similar to the Roman elders
  - (C) embraced the veto as the hallmark of Roman democracy
  - (D) overlooked Cicero's contributions to the theory of democracy
  - (E) formed a government based on world-wide democracy
- 5. The primary purpose of the passage is to
  - (A) reveal the indifferent attitude taken by the ancient Romans toward the fine arts
  - (B) discuss the lasting accomplishments achieved by ancient Romans
  - (C) analyse the use of the Latin language by the framers of the Constitution
  - (D) show that the construction of roads and aqueducts could not have been accomptished in ancient Greece
  - (E) Compare the destruction of the library at Alexandria to the murder of Archimedes
- 6. Which of the following is NOT described in the passage as a part of ancient Roman life that left a lasting legacy?
  - (A) The Latin languages
  - (B) Military accomplishments
  - (C) An extensive system of roads
  - (D) A democratic system of government
  - (E) Wide-ranging economic influence

# Explanatory Answers

- Ans. 1 (E). This specific question has a line number. Remember to read a bit above and below the cited lines. The two disasters citied are mentioned to give an example of Rome's failings, before countering with a number of Rome's successes. The best answer was choice (E).
- Ans. 2 (A). The specific question also has a good lead phrase: "Roman roads." You'll find it in the second paragraph. Choice (C) is wrong because these roads are not just similar to modern highways—they form the basis of these highways. Choice (E) is a bit too extreme. The cities may owe their prominence to these roads, but they were not "eaused" by the roads. The correct answer is choice (A).
- Ans. 3 (C). This is a specific question with a good lead phrase: "Latin language." You'll find it in the third paragraph. The correct answer is choice (C).
- Ans. 4 (A). The specific question also has a good lead phrase: "framers of the Constitution". You'll find it in the last paragraph. You may have been to choices (A) and (C). Choice (C) used extreme language and went a bit too far. Great as the veto is, did the founding fathers consider it the "hallmark" of democracy? The passage doesn't say so. The correct answer was choice (A).
- Ans. 5 (B). The first paragraph puts forth the idea that, despite criticism levelled against it, ancient Rome had many lasting accomplishments. The following three paragraphs give examples of these accomplishments.
- Ans. 6 (D). In the fourth paragraph, it is explicitly stated that despite its political innovations, Rome was "far from being a democracy." All of the other choices are touched upon somewhere in the passage.

#### PASSAGE 2

Anthropologists who study orangutans, distant cousins of the human race, find in the animals behaviour hints of how our earliest ancestors may have lived. It has long been accepted that primates originally dwelt in the treetops and only migrated to the ground as forests began to dwindle. While to a certain extent, all primates except humans spend at least some time dwelling in trees, the orangutans can grow as heavy as 330

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pounds and live for decades, requiring copious amounts of fruit simply to stay alive. Thus, they become very jealous of the territory where they find their food. Compounding this territoriality are the breeding habits of orangutans, since females can only breed every few years and, like humans, give birth not to litters but single off-spring.

Consequently, orangutans are solitary, territorial animals who have difficulty foraging in any part of the forest where they were not raised. Orangutans take from poachers by customs agents undergo incredible hardship on their return to the wild. Incorrectly relocating a male orangutan is especially problematic, often ending in the animal's death at the hands of a rival who sees not only his territory but also the females of his loosely knit community under threat from an outsider. While humans, like chimpanzees, are more gregarious and resourceful than orangutans, the latter provide anthropologists with useful information about the behaviour of prehominid primates and how apelike behaviour influenced out ancestors' search for the food and family beneath the forest's canopy.

Multiple Choice Questions (MCQs)

The primary purpose of this passage is to

- Describe some behavioural and evolutionary characteristics of orangutans (A)
- Analyse the reasons why early primates left their forest dwellings **(B)**
- (C) Illustrate the dangers posed to orangutans by poachers
- Show how orangutan behaviour differs from that of other primates **(D)**
- Criticise anthropologists who misinterpret orangutan behaviour (E) ·
- The author of the passage discusses "orangutans taken from poachers" in order to 2.
  - Stress the importance of preserving orangutans as a species (A) ...
  - Indicate the widespread practice of animal poaching (B)
  - Refute the theory that orangutans can live in a variety of environments (C)
  - Contrast the behaviour of orangutans with that of other apes **(D)**
  - **(E)** Emphasize the consequences of orangutan territoriality
- The passage indicates that it is difficult to return orangutans to the wild for which of the following reasons?
  - The threat posed by new comers to other orangutans' territory
  - B. . The conflict between males over available females
  - The scarcity of available food in the orangutan's environment
    - A only (A)

A and B only **(B)** 

(C) A and C only

B and C only **(D)** 

- **(E)** A, B, and C.
- Which of the following can be inferred about differences between the behaviour of orangutans and that of other ape species?
  - While orangutans spend much of their time on the treetops, other apes live exclusively on the (A)
  - Orangutans and other types of apes are all sociable species, but orangutans are more likely to (B) bond for life
  - Apes such as chimpanzees rely less upon their size than the average orangutans do (C)
  - Orangutans spend less time in the company of their members of their species than do some **(D)** other apes
  - Because of their stringent territoriality, orangutans are less likely to elude capture by poachers **(E)** than are other apes
- According to the author, anthropologists study the behaviour of orangutans in order to 5.
  - Prevent orangutans from becoming the target of poaching (A)
  - **(B)**: Assist customs agents in the relocation of orangutans
  - (C) Analyse the causes and consequences of contemporary human behaviour
  - Prevent larger orangutans from eliminating their weaker rivals (D)
  - (E) Better understand the factors that influenced human evolution
- Which of the following are factors that the author indicates contribute to the orangutan's territoriality? 6.
  - The lack of available food and the antisocial nature of orangutans (A)

- **(B)** The orangutan's need for large quantities of food and the infrequency with which it mates
- **(C)** The threat posed by poachers and the orangutan's inability to protest itself from them
- **(D)** The difficulties that orangutans face when compelled to socialize with other species such as
- (E) The constant dangers that present themselves whenever one orangutan encounters another It can be inferred from the passage that one development responsible for the evolution of distinct ape
  - (A) Early primates inability to survive in the forest
  - The shrinking of the available primitive forest **(B)**
  - (C) The growth of human and chimpanzee communities
  - The orangutan's eventual dominance of the treetops **(D)**
  - The encroachment of other species into the primitive forest **(E)**

Ans. 1 (A). The answer to this general question came from understanding the main idea. The passage did not analyse the reasons primates left trees (B), or devote itself to a discussion of poachers (C), or do a point-bypoint comparison of orangutans with other primates (D), or criticize anthropologists (E). The correct answer is choice (A).

Ans. 2 (E). The specific question has a line number. Remember to read a bit above and below the cited lines, The answer to this question actually came just below the quote. The poacher example is simply a further illustration of orangutans' territorial nature. The correct answer is choice (E).

Ans. 3 (B). Both statements I and II were mentioned, statement III was not. The correct answer is choice (B).

Ans. 4 (D). This is a specific question with no line number, and, really, no lead word. We're looking for differences between orangutans and other types of apes. The only other types of monkey mentioned is the chimpanzee who is said to be more gregarious. The correct answer is choice (D).

Ans. 5 (E). The specific question also has a good lead word: "anthropologists." It is found in two places, at the very beginning and the very end of the passage. You were probably down to choices (C) and (E). Why was (C)

wrong? Because anthropologists only see parallels with early man.

Ans. 6 (B). The specific question also has a good lead word: "Territoriality," you'll find it in the second half of the first paragraph, which discusses two cases: the need for large amounts of food, and breeding habits. You were probably down to (A) or (B). Why was (A) wrong? It didn't discuss both food and breeding habits. Choice (B) was correct.

Ans. 7 (B). The second sentence of the first paragraph ends, ... "only migrated to the ground as forests began to dwindle." That gives us choice (B).

This is a science passage. Paragraph one says the orangutan, studied by scientists for its resemblance to early humans, lives in trees and is very territorial. Paragraph two describes the orangutan's solitary territorial behaviour, which resembled that of early humans.

#### PASSAGE 3

Though the U.S. prides itself on behing a leader in the world community, a recent report shows that it lags far behind other industrialized countries in meeting the needs of its youngest and most vulnerable citizens. The U.S. has a higher infant mortality rate, a higher proportion of low birth weight babies, a smaller proportion of babies immunized against childhood diseases and a much higher rate of adolescent pregnancies. These findings, described as a "quiet crisis" requiring immediate and far-reaching action, appeared in a report prepared by a task force of educators, doctors, politicians and business people. According to the report, a fourth of the nation's I2 million infants and toddlers live in poverty. As many as half confront risk factors that could harm their ability to develop intellectually, physically and socially. Child immunizations are too low, more children are born into poverty, more are in substandard care while their parents work and more are being raised by single parents. When taken together, these and other risk factors can lead to educational and health problems that are much harder and more costly to reverse.

The crisis beings in the womb with unplanned parenthood. Women with unplanned pregnancies are less likely to seek pre-natal care. In the U.S., 80% of teenage pregnancies and 56% of all pregnancies are unplanned. The problems continue after birth where unplanned pregnancies and unstable partnerships often go

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e .) hand in hand. Since 1950, the number of single parent families has nearly tripled. More than 25 percent of all births today are to unmarried mothers. As the number of single parent families grows and more women enter the work force, infants and toddlers are increasingly in the care of people other than their parents.

Most disturbingly, recent statistics show that American parents are increasingly neglecting or abusing their children. In only four years from 1987-1991, the number of children in foster care increased by over 50 percent. Babies under the age of one are the fastest growing category of children entering foster care. The crisis affects children under the age of three most severely, the report says. Yet, it is this period-from infancy through preschool years-that sets the stage for a child's future.

# Matica Chaire Ductions (MCD)

		Tracupae Charce Ques	cuons    "	Udo/
1.	The main foc	us of the passage is on the plight of		
	(A)	Low birth weight babies	(B)	Unwed mothers
	(C)	Orphaned children	<b>(D)</b>	Teenage mothers
:	<b>(E)</b>	None of these		
2.	Children falli	ng in which age group are most sever	ely affected	by the 'quiet crisis'?
	(A)	Between 2 & 3 years	<b>(B)</b>	Between 1 & 3 years
	(C)	Below 1 year	<b>(D)</b>	Below 3 years
	<b>(E)</b>	None of these		
3.		following does not constitute the 'qui	iet crisis' in	the U.S. as per the task force report?
		er rate of babies surviving childhood		
	· · · —	er proportion of babies who are depriv		
		er proportion of new born babies with		
		er incidence of adolescent girls becom		
4		asing cases of teenage couples getting		the nassage?
4.		following statements is not true in the U.S., the number of infants living in		
		20 percent of all the pregnancies in the		
	(B) Only	20 percent of all the pregnancies in the	v je annrov	imately three times that of four decade
	(C) The ago	number of single-parent families toda	y is approx	initiatory three times that or room account
		number of children in the U.S. enterin	o foster car	e has decreased after 1991
	(E) Abou	at 6 million infants in the U.S. are like	ly to develo	on educational and health problems
·5.	The number	of children born to married mothers	in the U.S	is approximately how many times the
J.		ildren born to unwed mothers?		w.F.
	(A)	3 times	(B)	3.5 times
	(C)	1.5 times	(D)	2 times
	Œ	Not mentioned in the passage	` ′	
6.	, ,	n out of unplanned pregnancies are hi	ghly vulner	able because
		are mostly malnourished	•	
	(B) They	are less likely to receive parental car	e	
	(C) They	are raised by single parents		
	(D) Thei	r parents are mostly poor		
	(E) Thei	r parents are emotionally immature		
7.	Decide which	n of the following factors is/are respon	nsible for th	e physical, intellectual and social under
		of infants in the U.S.?		
	(A)	Illiteracy of parents	(B)	Lack of parental care
	(C)	Poverty		
	(A)	Only A	(B)	Only B
	(C)	Only C	(D)	Both A & C
	<b>(E)</b>	Both B & C		
8.		g number of infants in the U.S. are in		
	(A) An i	ncreasing number of employed couple	es who are r	equired to stay apart
1	(B) An i	ncreasing number of women getting d	ivorced and	l abandoning their babies

An increasing number of single parent families with the female member working

					IN	13 Gara	SECTION - III: VERBAL	ARILITY
	ec	conomically indep	endent				atus of unwed motherhood and	becoming
_	(E) A	n increasing numl	ber of pa	rents who	lack av	wareness	about baby-care	
9.	The task for	orce report seems	to be ba	ised on th	e data p	ertaining	g to the period	
	(A)	1987 onwai	rds till da	ate		<b>(B)</b>	1950-91	
	(C)					<b>(D)</b>	1950 onwards till date	
Thiad	(E)	1991 onwar	ds till da	ite				
Direct	ions (Q 10-	12): Choose the	word wh	ich is mo	st nearl	y the sar	ne in meaning as the given wor	d as used
in the p	passage. Confront				4			
10.	(A)	Succumb				/E35		
	(A) (C)	Face				(B)	Eliminate	
	(C) (E)					(D)	Tolerate	
11.	Vulnerable	Oppose						
11.	(A)	e Risky				<b>(D)</b>	<b>T</b>	
	(A) (C)	Insecure				(B)	Promising	
	(E)	Delicate				<b>(D)</b>	Indispensable	
12.	Abusing	Donout		•				
	(A)	. Ill treating				<b>(B)</b>	Accusing	
	(C)	Cursing				(D)	Beating	
	(E)	Oppressing				(12)	Deating	
Directi			word wh	ich is mo	ef anno	eite in m	neaning to the given word as us	ad in the
passage	e. ` `		.,	TORE TO THE	ar oppo	SRC III III	legilling to the given word as de	ea in me
13.	Severely							
	(A)	Minutely				(B)	Normally	
	( <b>C</b> )	Drastically				(D)	Intensely	
	(E)	Slightly				(2)	intensery	
14.	Unstable		100					
	(A)	Stagnant				(B)	Confined	. 1
	(C)	Changing				(D)	Steady	
	<b>(E)</b>	Constant			•			
15.	Substandar							
	(A)	Excellent				(B)	Valuable	
	(C)	Impoverishe	d			(D)	Compassionate	
	<b>(E)</b>	Beneficial				` /		
				ANS	WERS			
	1. (A)	, ,	-3.	$(\mathbf{E})$	4.	(D)		
	5. (A)	6. (B)	7.	<b>(E)</b>	8.	(D) (C)		•
		6. <b>(B)</b> 10. <b>(C)</b>						

# SHORT PASSAGE COMPREHENSION

#### Learn by Example

Read the passage carefully once and detect its theme. Note what the questions are about. Answer the questions.

### PASSAGE WITH EXPLANATORY ANSWERS

It is difficult to reconcile the ideas of different schools of thought on the question of education. Some people maintain that pupils at school should concentrate on a narrow range of subjects which will benefit them directly in their subsequent careers. Others contend that they should study a wide range of subjects so that they have not only the specialized knowledge necessary for their chosen careers but also sound general knowledge about the world they will have to work and live in. Supporters of the first theory state that the greatest contributions to civilization are made by those who are most expert in their trade or profession. Those on the



other side say that, unless they have a broad general education, the experts will be too narrow in their outlook to have sympathy with their follows or a proper sense of responsibility towards humanity as a whole.

# Multiple Choice Questions (MCQs)

- 1. 'Schools of thought' can be explained as:
  - (A) Groups of people who study in a particular school thoughtfully
  - (B) Groups of people having the same ideas but with different perception on a particular subject
  - (C) Groups of people whose job is to think
  - (D) Groups of people who are schooled to think
- 2. Broad general knowledge is necessary because
  - (A) It teaches us about different things
  - (B) It broadens one's outlook
  - (C) Specialisation is incomplete without it
  - (D) Without it no one would get a job
- 3. The idea of the first sehool of thought in the passage is that
  - (A) Students should study all the subjects they want to
  - (B) Students should study a few subjects that will help them in their profession
  - (C) Students should concentrate on studies
  - (D) Students should not undertake any specialized work
- Supporters of the first theory say that
  - (A) Experts have done nothing to help mankind
  - (B) People with general knowledge are more useful than experts
  - (C) Experts have contributed most to progress in the modern world
  - (D) People with general knowledge have contributed to eivilization
- 5. According to the second school of thought, education will not be very effective if pupils
  - (A) Ignore the study of fine arts
  - (B) Have nothing but general knowledge
  - (C) Have inadequate knowledge of their own work
  - (D) Do not have a wide general education

# Explanatory Answers

- (B) 'Schools of thought' means two persons or groups having different ideas or opinions on the same subject or topic.
- (B) The second school of thought supports the idea of having knowledge of a wide range of subjects for wider perception and outlook.
- 3. (B) The idea of the first school of thought is that people should focus on few subjects to benefit their career.
- 4. (C) The statement, 'Supporters of the first theory...expert in their trade or profession' gives the answer.
- 5. (D) The second school of thought opines that pupils should only concentrate on subjects of their interest to have an effective education and career.

### SHORT PASSAGES WITH EXPLANATORY ANSWERS

#### Passage 1

Books are, by far, the most lasting product of human effort. Temples crumble into ruin. Pictures and statues decay, but books survive. Time does not destroy the great thoughts which are as fresh today as when they first passed through their author's mind. These thoughts speak to us through the printed page. The only effect of time has been to throw out of currency the bad products. Nothing in literature which is not good can live for long. Good books have always helped man in various spheres of life. No wonder that the world keeps its books with great care.

Of the produ	ct of human effort, books are the m	ost	
(A)	Permanent	(B)	Important
<b>(C</b> )	Enjoyable	<b>(D)</b>	Useful
Time does no	ot destroy books because they contri	ain	
(A)	Useful material	(B)	Subject-matter for education
(C)	High ideals	(D)	Great ideas
"To throw or	it of currency" means		
· (A)	Destroy	(B)	Put out of use
(C)	Extinguish	(D)	Forget
The world ke	eeps its books with care because		
(A)	They bring great ideas to us		
<b>(B)</b>	They educate us		
(C)	They make us successful		
(D)	They help us in various spheres	of life	
		Answers	
(A)	The phrase 'books survive' destroyed easily.	indicates that	books are permanent and car

- be
- 2. **(D)** 'Time does not destroy the great thoughts', provides the correct answer.
- 3. (B) The author implies that bad products have always been discarded or 'thrown out of currency' with time while good things like books have always withstood the test of time.
- 4. **(D)** The author says that good books have always been handled with care by the world as they have helped man in different phases of life.

#### Passage 2

The low unit of gas is a real temptation to anyone choosing between gas and electrical processes. But gas-fired processes are often less efficient, require more floor space, take longer and produce more variable product quality. The drawbacks negate the savings many businesses believe they make.

By contrast, electricity harnesses a unique range of technologies unavailable with gas. And many electric processes are well over 90 percent efficient, so far less energy is wasted with benefits in terms of products quality and overall cleanliness, it can so often be the better and cheaper choice. Isn't that tempting?

# le Choice Questions

- 1. The passage can be described as
  - An advertisement for electricity and its efficiency (A)
  - An extract from a science journal (B)
  - **(C)** An account of the growth of technology
  - **(D)** An appeal not to use gas
- 2. What does the writer mean by 'variable quality'?
  - (A) The quality of the products cannot be assessed
  - **(B)** Products from gas-fired processes are inefficient

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- - **(C)** The kind of products vary from time to time
  - The quality of the products is not uniform **(D)**
- "Electricity harnesses a unique range of technologies" What does the writer mean? 3. Electricity
  - Has developed new technologies (A)
  - Ensures power for electricity and its efficiency **(B)**
  - Depends on new kinds of technology **(C)**
  - Makes use of several technologies **(D)**

- The passage brings to attention that the 'low unit of gas' should not lead anyone to use **(B)** gas processes as it has many negative factors. It serves to make aware the reader of the scientific reason for using electric processes and hence the passage looks to be an extract from a science journal.
- 'Variable quality' means quality which is not consistent or uniform. **(D)** 2.
- According to the passage, electricity provides a wide range of technologies and such 3. (B) processes are far more efficient and consumes less energy when compared to gas processes.

Passage 3

There was a marked difference of quality between the personages who haunted the near bridge of brick and the personages who haunted the far one of stone. Those of lowest character preferred the former, adjoining the town; they did not mind the glare of the public eye. They had been of no account during their successes; and though they might feel dispirited, they had no sense of shame in their ruin. Instead of sighing at their adversaries they spat, and instead of saying the iron had entered into their luck. The miserables who would pause on the remoter bridge were of a politer stamp - persons who did not know how to get rid of the weary time. The eyes of this species were mostly directed over the parapet upon the running water below. While one on the townward bridge did not mind who saw him so, and kept his back to the parapet to survey the passerby, one on this never faced the road, never turned his head at coming foot-steps, but, sensitive to his own condition, watched the current whenever a stranger approached, as if some strange fish interested him, though every finned thing had been poached out of the river years before.

- The two bridges were known 1.
  - For attaching dejected people to them (A)
  - For being equi-distant from town **(B)**
  - For being haunted places (C)
  - For their similar design (D)
- People belonging to the lower strata, in their moments of distress: 2.
  - Felt ashamed of their failures (A)
  - Dressed shabbily to earn sympathy **(B)**
  - Visited the brick-made bridge **(C)**
  - Remembered their days of glory **(D)**
- The bridge of stone was frequented by 3
  - (A) All the sections of society
  - The sophisticated but luckless (B)
  - Those fond of fishing (C)
  - (D) None of the above
- The attitude of the lowly and genteel towards strangers was
  - Virulently hostile (A)

Completely indifferent **(B)** 

Entirely different **(C)** 

- Virtually the same **(D)**
- In this passage, the author is trying to 5.
  - Explain the variety of ways in which strangers can be treated (A)

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- (B) Describe how people of different classes behaved when unhappy
- (C) Explain the difference between the construction of two bridges
- (D) Describe the way different sections of people like to dress

# Multiple Choice Questions (MCQs)

- 1. (A) The passage talks of dispirited people standing on the bridges. Hence one can say that the two bridges were known for 'the miserables' or the dejected people be coming frequently to those bridges.
- 2. (D) The statement, 'they did not mind the glare of the public cye', gives the correct answer.
- 3. (D) The bridge of stone was frequented by mostly dispirited and miserable people. Hence the answer is (D).
- 4. (C) The altitude of the lonely and genteel towards strangers was entirely different. According to the passage, they pretended to inspect the river under the bridge for some strange fish, whenever a stranger came nearby.
- 5. (B) They author tried to explain the different kinds of behaviour of people of different classes when they were unhappy. Here he used the bridge to explain the behaviour of these different classes of people.

#### Passage 4

It is to progress in the human sciences that we must look to undo the evils which have resulted from a knowledge of the physical world hastily and superficially acquired by populations unconscious of the changes in themselves that the new knowledge has made imperative. The road to a happier world than any known in the past lies open before us if atavistic destructive passions can be kept in leash while the necessary adaptations are made. Fears are inevitable in our time, but hopes are equally rational and far more likely to bear good fruit. We must learn to think rather less of the dangers to be avoided than of the good that will lie within our grasp if we can believe in it and let it dominate our thoughts. Science, whatever unpleasant consequences it may have by the way, is in its very nature a liberator, a liberator of bondage to physical nature and in to come, a liberator from the weight of destructive passions. We are on the threshold of utter disaster or unprecedentedly glorious achievement. No previous age has been fraught with problems so momentous; and it is to science that we must look to for a happy future.

# Multiple Choice Questions (MCQs)

- 1. What does science liberate us from? It liberates us from
  - (A) Idealistic hopes of a glorious future
  - (B) Slavery to physical nature and from passions
  - (C) Bondage to physical nature
  - (D) Fears and destructive passions
- 2. To carve out a bright future a man should
  - (A) Cultivate a positive outlook
  - (B) Analyse dangers that lie ahead
  - (C) Try to avoid dangers
  - **(D)** Overcome fears and dangers
- 3. If man's bestial yearning is controlled
  - (A) The future will be brighter than the present
  - **(B)** The future will be tolerant
  - (C) The present will be brighter than the future
  - (D) The present will become tolcrant
- 4. Fears and hopes, according to the author
  - (A) Are irrational
  - (B) Are closely linked with the life of modern man
  - (C) Can yield good results
  - (D) Can bear fruit

Should human sciences be developed because they will Make us conscious of the changing world (A) Provide more knowledge of the physical world **(B)** Eliminate the destruction caused by a superficial knowledge of the physical world (C) Make us conscious of the changes in ourselves **(D)** The phrase, 'liberator from the weight of destructive passions', provides the correct **(B)** answer. According to the passage, despite problems and dangers, we must adopt an optimistic (A) or a positive outlook and look at science as a means to secure a bright future. The sentence, 'The road to a happier world...adaptations are made,' provides the (A) correct answer. [Bestial means 'beast-like' or brutal] Fears and hopes are bound to occur in one's life, according to the passage, **(B)** The statement, 'Science, whatever unpleasant... passions,' provides the correct **(C)** answer. Passage 5 The Nobel Committee, in fact, a notoriously conservative body which among other things had a marked antipathy to pure science, especially to Mathematical Physics. Restrained by a clause in Alfred Nobel's will that the prize should go to the person whose 'discovery or invention' shall have conferred the greatest benefit to mankind, the committee initially ignored the great theoretical advances in Physics. Wrecked, no doubt, by guilt that he had become a merchant of death through his invention of dynamite and smokeless powder and plagued by sadistic fantasies of destruction, the Swedish chemist, engineer and aspiring poet, Alfred Nobel, who has been described as Europe's richest vagabond, left his colossal fortune to the cause of progress in human knowledge. Five prizes were installed, one each for Literature ('to the person who shall have produced in the field of Literature, the most outstanding work of an idealistic tendency'), Physics, Chemistry, Medicine and Peace ('to the person who shall have done the most or the best work for fraternity among nations for abolition or reduction of armies, and for holding or promotion of Peace'). Aultiple Choice Questions The Nobel Committee has been called a conscrvative body because Its members are old fashioned (A) It awards prizes only to those people who adopt a conservative approach **(B)** It is conservative in choice of subjects (C) Its members believe in a conservative ideology (D) In the beginning, the Nobel Committee ignored the great advances in theoretical physics because 2. The Committee felt that the discovery and invention in the field did not contribute to (A) the benefit of mankind They proved to be merchants of death and hence dangerous to mankind **(B)** They were different from other branches of Physics **(C)** They were concerned with theory and did not suggest its application **(D)** 3. Noble Prize would not be given to A composer who composed a symphony (A) An author who wrote a novel **(B)** A diplomat who negotiated a peace settlement (C) A doctor who discovered a vaccine **(D)** Alfred Nobel left his colossal fortune to the cause of progress in human knowledge because he

Felt guilty for having invented highly destructive things

Felt guilty for having earned so much money

Was a chemist, engineer and an aspiring poet

Was 'Europe's richest vagabond'

(A)

**(B)** 

(C)

(D)

- **(C)** The Nobel Committee is a conservative body because it does not favour subjects like 'Mathematical Physics'. 2. (A)
- The statement, 'will that the prize should go to the person ... in Physics,' provides the 3.
- The five prizes installed for conferring 'Nobel Prize...' do not include music. (A) 4. The phrase, 'wrecked, no doubt, by guilt...,' gives the correct answer. (A)

Passage 6

Mountaineering is now looked upon as the king of sports. But men have lived amongst the mountains since prehistoric times and in some parts of the world, as in the Andes and Himalayas, difficult mountain journeys have inevitably been part of their everyday life. However, some of the peaks were easily accessible from most of the cities of Europe. It is quite interesting that while modern mountaineers prefer difficult routes for the greater enjoyment of sport, the early climbers looked for the easiest ones, for the summit was the prize they all set their eyes on. Popular interest in mountaineering increased considerably after the ascent of the Alpine peak of Matterhorn in 1865 and Edward Whymper's dramatic account of the climb and fatal accident

In the risky sport of mountaineering, the element of competition between either individuals or teams is totally absent. Rather one can say that the competition is between the team and the peaks themselves. The individuals making up a party must climb together as a team, for they depend upon one another for their safety. Mountaineering can be dangerous unless reasonable precautions are taken. However, the majority of fatal accidents happen to parties which are inexperienced or not properly equipped. Since many accidents are caused by bad weather, the safe climber is the man who knows when it is time to turn back, however, tempting it may be to press on and try to reach the summit.

# le Choice Questions

Mountaineering is different from other sports because

- There is no competition between individuals (A)
- **(B)** It is most thrilling and exciting
  - (C) It can be fatal
  - It is risky and dangerous **(D)**
- 2. People living in the Andes and the Himalayas made mountain journeys because
  - It was a kind of sport
  - They had to undertake them in their day-to-day life **(B)**
  - (C) They lived in pre-historic times
  - Of the challenge offered by the difficult journey (D)
- Mountaineers climb as a team because 3.
  - The height is too much for one individual (A)
  - **(B)** They have to rely on each other for safety
  - There is no competition among them (C)
  - **(D)** The competition is between the team and the peak
  - ...the summit was the prize they all set their eyes on". In the context of the passage this means
    - They chose a route from which they could see the summit clearly **(B)**
    - They cared for nothing but the prize of reaching the summit
    - They kept their eyes steadily on reaching the peak (C)
    - Reaching the top was their exclusive concern **(D)**
- "to press on" in the last sentence means 5.
  - To continue in a determined manner (A)
  - **(B)** To work fearlessly
  - (C) To force upon others
  - (D) . To struggle in a forceful manner

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## Explanatory Answers

(D) The phrase 'In the risky sport of mountaineering...', suggests that this kind of sport is different from other sports in being more dangerous and fatal.

(B) The statement, '...difficult mountain journeys have been part of their everyday life,' provides the correct answer.

(B) The statement, '... climb together as a team, for they depend upon one another for their safety' provides the correct answer.

(D) The challenge of the sport lay in reaching the peak. Hence the answer is (D).

(A) 'To press on' means to be persistent in one's struggle to achieve the objective or in other words to continue in a determined manner.

Passage 7

After submitting his resignation, Albert came out and took the long narrow road leading to the railway ation which was one of the busiest roads in the city. Sad and depressed and worried about looking for a new ob, Albert looked around for a cigarette shop. He walked up to the end of the road but found no tobacconist. It as odd that such a busy thoroughfare with thousands of people passing through did not even have a single garette shop. He suddenly felt that it was no longer necessary for him to hunt for a job. He decided to open a obacco shop himself. It was bound to be profitable, he felt.

# Multiple Choice Questions (MCQs)

After submitting his resignation, Albert came out worried about

- (A) A job
- (B) The next available rain
- (C) A shelter
- (D) Cigarettes

Albert was sad and depressed because

- (A) He was not able to buy eigarettes
- (B) He was worried about finding a job
- (C) He had no money for the train journey
- (D) He had to walk on a long road

There was no cigarette shop on that road because

- (A) It was a very narrow road
- (B) Cigarette-shop owners do not make any profit
- (C) Smoking is banned in that area
- (D) Just by chance nobody had opened one on that road

Albert decided not to look for a new job because

- (A) There was no hope of finding a job
- (B) He saw the possibility of self-employment
- (C) The thought of having to look for a job greatly distressed him
- (D) He did not want to work at all

A cigarette shop on a busy road was bound to be profitable because

- (A) Cigarettes are inexpensive items and people buy them willingly
- (B) A cigarette shop on a busy road would attract a large number of customers
- (C) Cigarette shops are known to make a great deal of profit
- (D) Any shop on a busy street would attract a large number of customers

### Explanatory Answers

- (A) According to the author, Albert gave resignation from his job to look for a new job. Hence the answer is (A).
- (D) Albert was worried and depressed about looking for a new job.
- (D) According to the author, it was strange that there was not any single eigarette shop on such a busy road and hence assumed that it must be chance that nobody opened one.

The statement, 'Two world wars...has been paid for the lack of wisdom in man's part

in this generation' gives the correct answer.

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- 4. (B) The statement, 'Even if the end is right...divert us in the wrong direction', gives the correct answer. 'Deflect' means 'to divert' or to turn away from a certain direction.
  - (D) 'Vitiate' means to spoil or impair. Hence it means debase meaning 'to pollute' or to contaminate.

#### Passage 9

In the past thirty years, drugs have been discovered that prevent and cure physical disease and reverse the disturbances that occur in certain mental illness. Excitement over what drugs can do has led people to believe that any ailment, infective or psychic, can be relieved by taking a pill. At the first sign of nervousness, they try pep-up pills. Medical journals now advertise tranquillizers, and other mood-altering drugs; doctors prescribe them; and the public expect miracles from them. In such an atmosphere, it is not surprising that drug abuse has spread.

# - Multiple Choice Questions (MCQs) ==

- According to the author, in recent years there has been
  - (A) Recognition of the ill-effects of medicine
  - (B) A misplaced trust in drugs
  - (C) A distrust of drugs
  - (D) None of the above
- 2. According to the passage, the medicines that have been discovered in recent times
  - (A) Can reduce mental illnesses
  - (B) Cannot cure mental illnesses
  - (C) Can cure mental illnesses
  - (D) Can help treat some symptoms of mental illnesses
- 3. People often believe that
  - (A) Medicines can cure all the diseases
  - (B) Doctors cannot cure all the diseases
  - (C) Medicines cannot cure all the diseases
  - (D) Doctors can cure all the diseases

# Explanatory Answers

- 1. (B) The author talks of the immense trust of people in drugs followed by the statement '...drug abuse has spread'. This indicates a misplaced trust in drugs.
- 2. (D) The statement 'drugs...reverse the disturbances that occur in some mental illness' gives the answer.
  3. (A) The sentence 'Excitoment will always the sentence 'Excitoment will always the sentence of
  - (A) The sentence 'Excitement...pill' gives us the answer.

#### Passage 10

When we are suddenly confronted with any terrible danger, the change of nature we undergo is equally great. In some cases, fear paralyses us. Like animals, we stand still, powerless to move a step in fright or to lift a hand in defence of our lives, and sometimes we are seized with panic, and again, act more like the inferior animals than rational beings. On the other hand, frequently in cases of sudden extreme peril, which cannot be escaped by fright, and must be instantly faced, even the most timid men at once as if by miraele, become possessed of the necessary courage, sharp quick apprehension, and swift decision. This is a miracle very eommon in nature. Man and the inferior animals alike, when confronted with almost certain death 'gather resolution from despair' but there can really be no trace of so debilitating a feeling in the person fighting, or prepared to fight for dear life. At such times, the mind is clearer than it has ever been; the nerves are steel, there is nothing felt but a wonderful strength and daring. Looking back at certain perilous moments in my own

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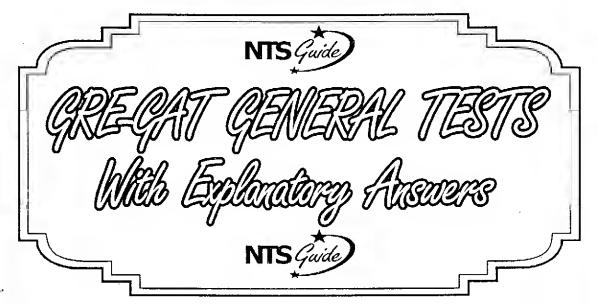
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life, I remember them with a kind of joy, not that there was any joyful excitement then; but because they brought me a new experience, a new nature, as it were and lifted me for a time above myself.

# Multiple Choice Questions (MCQs)

1.	An appropri	ate title for the above passage would be
	(A)	The change of nature
	(B)	Courage and panic
	(C)	The will to Fight
	<b>(D)</b>	The miracle of confronting danger
2.	The author r	names three different ways in which a man may react to sudden danger. What are they?
	(A)	He may be paralysed with fear, or seized with panic, or as if by miracle, become possessed of the necessary courage, and face the danger
	<b>(B)</b>	He may be paralysed with fear, run away or fight
	(C)	He may flee in panic, or fight back or stand still
	<b>(D)</b>	He may be paralysed with fear, seized with panic or act like an inferior animal
3.	The distincti	on between 'inferior animals' and 'rational beings' is that
	(A)	The latter are stronger
	(B)	The latter are capable of reasoning things out whereas the former cannot do so
	(C)	The former are incapable of fighting
	<b>(D)</b>	The latter are clever
4.	Explain the p	phrase 'gather resolution from danger'.
	(A)	Not to lose hope, but fight
	<b>(B)</b>	Find courage to face the danger
	(C)	Find hope and courage
	<b>(D)</b>	A state of utter hopelessness steels one to fight out the danger
5.	The author for	cels happy in the recollection of danger faced and overcome because
	(A)	He survived his ordeal
	<b>(B)</b>	He was lucky to be alive
	(C)	They brought him a new experience
	(D)	They brought him a new experience, and lifted him above himself for a time
		Explanatory Answers
1.	<b>(D)</b>	The passage talks of the different ways in which people react when faced with any kind of danger and hence the title should be 'The miracle of confronting danger'
2.	(A)	In the first few lines, the author talks of fear paralyzing a person or being seized with panic when faced with danger. Then he goes on to explain that some people become amazingly courageous in times of peril and danger.
3.	(B)	The author while stating the different reactions of men when confronted with danger makes a comparison with animals who tend to become powerless or behave irrationally in times of danger.
4.	<b>(D)</b>	The phrase 'gather resolution from danger' means to brace oneself or assemble the strength to face danger.
5.	(D)	The statement, 'Looking backjoyful excitement' gives the answer.





GRE - GAT TEST 1

**Quantitative Section** 

No. of Questions = 20

Q1. If it is now March, what month will be after the 100 months from now?

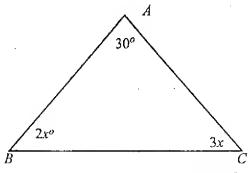
(A) March

(B) April

(C) July

(D) August

Q2. What is the value of x in the following figure?



(A)  $30^{\circ}$ 

**(B)**  $40^{\circ}$ 

(C)  $50^{\circ}$ 

**(D)**  $60^{\circ}$ 

Q3. What is the value of x if  $3^{x+1} = 243$ ?

(A)

**(B)** 5

(C) 7

(D) 4

Q4. If x is a multiple of 5 and y = 5x, then which of the following could be the value of x + y?

I. 60

II. 110

III. 50

(A) I only

(B) II only

(C) I and II only

(D) I and III only

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## Q5. If Riaz can mow $\frac{3}{4}$ of a lawn each hour, how many lawns can be moved in k hours?

(A)  $\frac{4k}{3}$ 

(B)  $\frac{3k}{4}$ 

(C)  $\frac{2k}{3}$ 

**(D)**  $\frac{3k}{2}$ 

Q6. If 
$$2^a = x$$
 and  $2^b = y$ , then  $xy = x^a = y^a + y^a = y^a$ 

(A)  $9^{a_1+b_2}$ 

**(B)** 2<sup>ab</sup>

(C)  $4^{a+b}$ 

(D)  $2^{a+}$ 

## Q7. If the average (arithmetic mean) of three consecutive integers is M, then which of the following must be true?

- I Any one of the three numbers is M
- II The average of two of the three numbers is M.

### III M is also an integer

(A) I only

(B) II only

(C) III only

(D) I, II and X

Q8. If 
$$a^2 = 17$$
, then  $(a + 1)(a - 1) = ?$ 

(A) 15

**(B)** 12

(C)  $\sqrt{18}$ 

**(D)** 16

### Q9. Which of the following cannot be expressed as the sum of three consecutive integers?

(A) 27

(B) 26

(C) 21

**(D)** 42

# Q10. Ali and Omer share an apartment. If each month Ali pays x dollars and Omer pays y dollars, what percent of the total cost does Ali pay?

(A) .(x+y)100

(B)  $\frac{x}{y}$ %

(C)  $\frac{100x}{y}$ %

 $(D) \qquad \frac{100x}{x+y} \%$ 

### Q11. If $(a-b)^2 = a^2 - b^2$ and $a \ne b$ , then which of the following is true?

$$a=0$$

II 
$$b=0$$

III 
$$a = -b$$

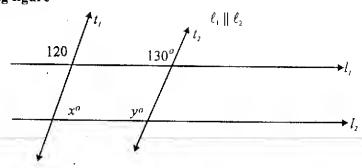
(A) I only

(B) II only

(C) Land II only

(D) I and III only

### Q12. In the following figure



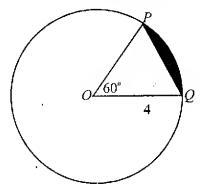
$$x + y =$$

(A) 230

**(B)** 210

**(C)** 110

- **(D)** 190
- Q13. In the following figure the radius of the circle is 4, and m \( POQ = 60. \) What is the perimeter of the shaded region?



(A)  $4 + \frac{2\pi}{3}$ 

**(B)**  $4 + \left(2 + \frac{\pi}{3}\right)$ 

(C)  $4 + \frac{5\pi}{3}$ 

- (D)  $4 + \frac{4\pi}{3}$
- Q14. If  $S_1$  is the sum of integers from 1 to 60 and  $S_2$  is the sum of the integers from 61 to 100, what is the value of
  - $S_2 S_1$ ?
    - (A) 2500

(B) 2100

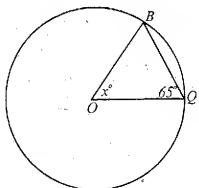
(C) 1800

- (D) 1390
- Q15. If p, q and r are different prime numbers less than 15, what is the greatest possible value of  $\frac{p+q}{r}$ 
  - (Å) 9

(B) 2

(C) 13

- **(D)** 12
- Q16. In the following figure O is the center of the circle. What is the value of x?



(A) 65°

**(B)** 50°

(C)  $45^{\circ}$ 

- **(D)**  $35^{\circ}$
- Q17. If x is increased by 10% and y is decreased by 10%, the resulting numbers will be equal. What is the ratio x to y?
  - **(A)**  $\frac{3}{4}$

**(B)**  $\frac{9}{11}$ 

(C)  $\frac{4}{3}$ 

(D) = \frac{2}{2}

 $Q_3$ 

Q4

Q5

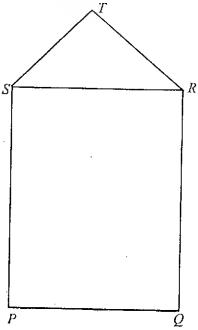
Q6

Q7

Q8

Q9

Q18. In the following figure, the area of the isosceles triangle RST is 8 and the area of the square PQRS is 64. What is the distance from P to T.



- (A) 64
- **(C)** 41

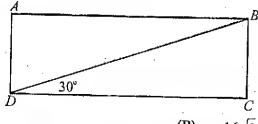
- **(B)** 5
- **(D)**  $2\sqrt{29}$

- Q19. If 5x + 3 = 3x + 5, then x = ?
  - (A)

(B) 2

(C)  $\frac{1}{2}$ 

- (D)  $\frac{1}{2}$
- Q20. What is the area of the following rectangle PQRS?



(A)  $25\sqrt{3}$ 

**(B)**  $16\sqrt{3}$ 

(C)  $12\sqrt{3}$ 

(D) 64

## Explanatory Answers

Q1. (C) In a year there are 12 months, so

100 month 
$$= (12 \times 8) + 4$$

$$= 96 + 4$$

Explanation: 8 years from now, it will again be March, and 4 months later it will be July.

Q2. (A) In any triangle,

The sum of three angles =  $180^{\circ}$ 

$$. \quad 30^{\circ} + 2x + 3x = 180$$

$$\Rightarrow 5x = 180 - 30$$



$$\Rightarrow \qquad x = \frac{150}{5} \Rightarrow x = 30$$

Q3. (D) 
$$3^{x+1} = 243$$
  

$$\Rightarrow 3^{x+1} = 3^{5}$$

$$\Rightarrow x+1 = 5$$

$$\Rightarrow x = 4$$

Q4. (A) As x is a multiple of 5, then for any integer n, x can be written as

$$x = 5n$$

Also 
$$y = 5x$$

$$\Rightarrow x + y = x + 5x \Rightarrow x + y = 6x$$

$$\Rightarrow x + y = 6(5n) \Rightarrow x + y = 30n$$

It means, that x + y is the multiple of 30.

Now, w check I, II and III

(i) Could x + y = 60?

Yes, because 
$$x + y = 30(2) \Rightarrow x + y = 30n$$
  
i.e.,  $(a = 10, b = 50)$ 

(ii) Could x + y = 110?

No, because 110 is not multiple of 30.

(iii) Could x + y = 50?

No, because 50 is not multiple of 50.

Therefore, only option A is true.

Q5. (B) Simply multiply  $\frac{3}{4}$  by k.

$$\frac{3}{4}(k) = \frac{3k}{4}$$

**Q6. (D)** 
$$x=2^a$$
 and  $y=2^b$  (given)

$$xy = 2^a \times 2^b$$

$$\Rightarrow xy = 2^{a+b}$$

Q7. (D) Let the three consecutive numbers be

5, 6 and 7. Its average is

$$M = \frac{5+6+7}{3} = \frac{18}{3} = 6$$

Hence I is true.

Now, 
$$\frac{5+7}{2} = \frac{12}{2} = 6$$

Hence, II is true.

Also, III is true.

Q8. (D) 
$$a^2 = 17$$
  $\Rightarrow a^2 - 1 = 17 - 1$   
 $\Rightarrow a^2 - 1 = 16$ 

$$\Rightarrow (a-1)(a+1) = 16$$

3 = 3(x + 1) which is multiple of 3. Only 26 is not multiple of 26.

Q:

Q1:

Q16

- Q10.(D) The total rent is x + y, so Ali's share is  $\frac{x}{x + y}$ . To convert into percentage we multiply  $\frac{x}{x + y}$  by 100 and place %age sign.
- Q11.(B)  $(a-b)^2 = a^2 b^2$

$$a^2 + b^2 - 2ab = a^2 - b^2$$

Case I: If a = 0, then

$$(0)^{2} + b^{2} - 2(0)(b) = (0)^{2} - b^{2}$$
$$b^{2} = -b^{2}$$

which is not true.

Case 11: If b = 0, then

$$a^2 + b^2 - 2ab = a^2 - 0^2$$

$$a^{2} + (0)^{2} - 2a(0) = a^{2} - (0)^{2}$$

$$\Rightarrow a^2 = a^2$$

which is true,

Case III: If a = -b, then

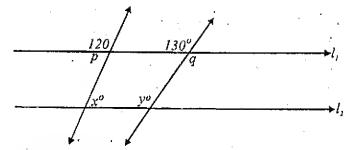
$$(-b)^2 + b^2 - (2)(-b)(b) = (-b)^2 - b^2$$

$$b^2 + b^2 + 2b^2 = b^2 - b^2$$

$$4b^2=0$$

which is not true.

Q12.(D) Here  $120 + p = 180 \Rightarrow p = 60$ 



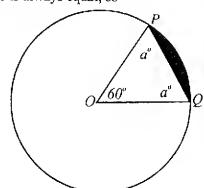
and q = 130 (corresponding angles)

Since  $l_1$  and  $l_2$  are parallel, so

$$p = x^o = 60$$
 and  $q = y^o = 130$ 

Hence 
$$x + y = 60 + 130 = 190$$
.

Q13.(D) Since each radius of a circle is always equal, so



$$OP = OQ = 4$$



Because, two sides of a triangle. POQ are equal, so their opposite angles must be equal. Let one angle be  $a^{\circ}$  then the other will also be  $a^{\circ}$ .

Thus in APOO

$$60^{\circ} + a^{\circ} + a^{\circ} = 180$$
  $\Rightarrow 2a^{\circ} = 180 - 60$   
 $\Rightarrow a^{\circ} = \frac{120}{2} = 60$ 

Thus the length of  $\overline{PQ}$  also 4, and the length of arc PQ is

$$\frac{60}{360} = \frac{1}{6}$$
 of the circumference.

Now, circumference,  $C = 2\pi r \Rightarrow C = 2\pi(4)$ 

$$\Rightarrow C = 8\pi \Rightarrow \frac{1}{6}C = 8\pi \times \frac{1}{6}$$
$$= \frac{4\pi}{3}$$

Hence the perimeter of the region is

$$4 + \frac{4\pi}{3}$$

Q14.(D) To find the sum of  $1+2+3+\ldots+60$ , use the following formula

$$S_1 = \frac{n}{2} \{2a + (n-1)d\}$$

Here, n = 60, a = 1, d = 2 - 1 = 1

$$S_1 = \frac{60}{2} \{2(1) + (60 - 1)1\}$$

$$S_1 = 30(2 + 59) \Rightarrow S_1 = 30(61)$$

$$\Rightarrow$$
 S<sub>1</sub> = 1830

Now, we find the sum of  $\{61 + 62 + 63 + \dots + 100\}$ 

Here, a = 61, n = 40d = 62 - 61 = 1

$$S_n = \frac{n}{2} \left\{ 2a + (n-1)d \right\}$$

$$S_2 = \frac{40}{2} \{ 2(61) + (40-1)I \}$$

$$S_2 = 20\{122 + 39\} \Rightarrow S_2 = 20(161)$$

$$\Rightarrow$$
  $S_2 = 3220$ 

Now, 
$$S_2 - S_1 = 3220 - 1830$$
  
= 1390

Q15.(D) The prime numbers less than 17 are 2, 3, 5, 7, 11, 13

To make a larger fraction, make the numerator as large and denominator as small. So, Let p = 13 and q = 11

and r = 2 (smallest prime number)

$$\therefore \frac{p+q}{2} = \frac{13+11}{2} = \frac{24}{2} = 12$$

Q16.(B) Since all the radii of a circle have the same magnitude, thus OA = OB. Therefore  $m \angle A = m \angle B = 65^{\circ}$ Hence.  $x + m\angle A + m\angle B = 180^{\circ}$ 

$$\Rightarrow x + 65 + 65 = 180$$

$$\Rightarrow$$
  $x + 130 = 180$ 

$$\Rightarrow x = 50$$

Q17.(B) 
$$x + \frac{10}{100}(x) = x + 0.1x = 1.1x$$

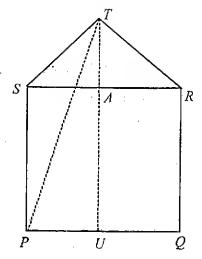
Now 
$$y - \frac{10}{100}(y) = y - 0.1y = 0.9y$$

Setting ratio

$$1.1 x = 0.9 y \Rightarrow \frac{x}{y} = \frac{0.9}{1.1}$$

$$\Rightarrow \frac{x}{y} = \frac{9}{11}$$
.

Q18.(D) Join the point P to T by line segment. From T draw TU perpendicular on PQ, which cut the line RS at A.



Then 
$$AU = 8$$

In 
$$\triangle$$
 RST, base = 8 and Area = 8

As Area = 
$$\frac{1}{2}$$
(base)(Altitude)

$$\Rightarrow 8 = \frac{1}{2}(8)AT \Rightarrow AT = \frac{8 \times 2}{8} = 2$$

$$\Rightarrow TU = TA + AU \Rightarrow TU = 2 + 8 \Rightarrow \boxed{TU = 10}$$

Now, In  $\triangle PTU$ 

Altitude 
$$PU = 4$$
 and Base,  $TU = 10$ 

We know, 
$$(PT)^2 = (PU)^2 + (TU)^2$$

$$\Rightarrow$$
  $(PT)^2 = (4)^2 + (10)^2 \Rightarrow (PT)^2 = 16 + 100$ 

$$\Rightarrow PT = \sqrt{116} \Rightarrow 2\sqrt{29}$$

**Q19.(A)** 
$$5x + 3 = 3x + 5$$

$$\Rightarrow$$
  $5x - 3x = 5 - 3$ 

$$\Rightarrow$$
 2x = 2

$$\Rightarrow$$
  $x = 1$ 

VT:

Q3.

Q4.

For q Four ( differe before Q5,

Q6.

Q7.

**(C)** 

**(E)** 

Dar has his duty on Saturday.

Ali has his duty on Sunday.

Q20.(B) PR is the hypotenuse of a 30-60-90 triangle. Thus, QR, the opposite leg of the  $30^{\circ}$  angle, is 4 (half of PR), and PQ is  $4\sqrt{3}$ . Then the area of the rectangle PQRS.

#### $4 \times 4\sqrt{3} = 16\sqrt{3}$ Analytical Section No. of Questions = 20For questions 1 to 4 Three women — X, Y, and Z are traveling in a van with five children — A, B, C, D and E. The van has a driver's seat and one passenger seat in the front, and two benches behind the front seats, one bench behind the first. Each bench has room for exactly three people. Everyone must sit in a seat or on a bench and seating is subject to the following restrictions: A women must sit on each bench. Either X or Y must sit in the driver's seat. C must sit immediately beside E. Which of the following can sit in the front passenger seat? Q1. (A) C**(B)** D**(C)** X (D) Y **(E)** ZWhich of the following groups of three can sit together on a bench? Q2. (A) A, C and E**(B)** A, C and Z(C) A, Y and Z**(D)** $B_i D$ and Y**(E)** D, E and XQ3, If A sits immediately beside Z, which of the following CANNOT be true? C sits immediately beside Y. (A) (B) D sits immediately beside Z. **(C)** B sits in the front passenger seat. **(D)** A sits on the same bench as B. **(E)** B sits on the same bench as X. Q4. If Y sits on a bench that is behind where C is sitting, which of the following must be true? B sits in a seat or on a bench that is in front of where E is sitting. (Ä) D sits in a seat or on a bench that is in front of where A is sitting. **(B) (C)** A sits on the same bench as B. **(D)** D sits on the same bench as Y. **(E)** E sits on the same bench as Z. For questions 5 to 7 Four computer operators (Ali, Babar, Cheema and Dar) each have to perform duties at the NADRA on four different days, Thursday through Sunday. The following is their duty schedule: Cheema has his duty day before Ali. Dar has his duty day later than Babar. Q5. Which of the following is a possible order of duty days for the four operators? (A) Cheema, Dar, Ali and Babar **(B)** Dar, Cheema, Ali and Babar (C) Babar, Cheema, Dar and Ali **(D)** Ali, Cheema, Dar and Babar **(E)** Ali, Babar, Dar and Cheema Q6, If Cheema has his duty day on Saturday, who must have his duty day on Thursday? Either Ali or Dar (A) **(B)** Dar **(C)** Ali (D) Either Babar or Dar **(E)** Babar Q7. Each of the following possible EXCEPT: (A) Cheema has his duty on Thursday. **(B)** Babar has his duty on Thursday.

Babar has his duty on Sunday.

**(D)** 

### NTS Guide GRE - GAT General Tests With Explanatory Answers

Two statements, labeled X and Y, follow each of the following questions. The statements contain certain information. In the questions you do not actually have to compute an answer, rather you have to decide whether the information given in the statements X and Y is sufficient to find a correct answer by using basic mathematics and everyday facts.

- Q8. How much time will computer need to solve 150 problems?
  - X. The computer needs 50 seconds to solve one problem.
  - Y. Computer never takes more than 60 seconds to solve a problem.
    - (A) Statement X. Alone is sufficient but Y. Alone is not sufficient to answer this question.
    - (B) Statement Y. Alone is sufficient but X. Alone is not sufficient to answer this question.
    - (C) Statements X and Y. TOGETHER are sufficient to answer the question but NEITHER of them is sufficient ALONE.
    - (D) Statements X and Y. COMBINED are NOT sufficient to answer the question and additional information is needed to find the correct answer.
- Q9. A horse ran 80 miles without stopping. What was its average speed in miles per hour?
  - X. The journey started at 6 PM and ended at 2 AM the following day.
  - Y. The horse ran 20 miles per hour for the first 40 miles.
- (A) Statement X. ALONE is sufficient but Y. ALONE is not sufficient to answer this question.
- (B) Statement Y. ALONE is sufficient but X. ALONE is not sufficient to answer this question.
  - (C) Statements X and Y. TOGETHER are sufficient to answer the question but NEITHER of them is sufficient ALONE.
  - (D) Statements X and Y. COMBINED are NOT sufficient to answer the question and additional information is needed to find the correct answer.
- Q10. In a B.Sc. class at G.C. University, 40 boys and 15 girls registered for Calculus and Analytical geometry. How many boys passed the course?
  - X. 7 students could not pass.

question.

- Y. There were 3 girls who obtained A grade.
- (A) Statement X. ALONE is sufficient but Y. ALONE is not sufficient to answer this question.
- (B) Statement Y. ALONE is sufficient but X. ALONE is not sufficient to answer this question.
  - (C) Statements X and Y. TOGETHER are sufficient to answer the question but NEITHER of them is sufficient ALONE.
  - (D) Statements X and Y. COMBINED are NOT sufficient to answer the question and additional information is needed to find the correct answer.
- Q11. A runner has just completed 46 miles running. How long did it take him to finish the journey?
  - X. His record speed is 13.2 miles per hour.
  - Y. His average speed through the journey was 9.2 miles per hour.
    - (A) Statement X. ALONE is sufficient but Y. ALONE is not sufficient to answer this
- (B) Statement Y. ALONE is sufficient but X. ALONE is not sufficient to answer this question.
  - (C) Statements X and Y. TOGETHER are sufficient to answer the question but NEITHER of them is sufficient ALONE.
  - (D) Statements X and Y. COMBINED are NOT sufficient to answer the question and additional information is needed to find the correct answer.

Q12

N

gues

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Q13

Q14

Q15.

Q16.

Solui We s

i) 1

ii)

111)

v) ′

v)

Q12.		of national hockey tea f Pakistan's national h	m should be the most p ockey team?	opular member of the team. Who is the
ŀ		n is the best player on		
		is the scnior-most me		
quest	(A)	Statement X. ALON	IE is sufficient but Y. ALC	ONE is not sufficient to answer this
quest	ion.	Statement Y. ALON	E is sufficient but X. ALC	ONE is not sufficient to answer this
	(C)	Statements X and Y. them is sufficient AI	TOGETHER are sufficien LONE.	t to answer the question, but NEITHER of
	<b>(D)</b>	Statements X and Y. additional information	COMBINED are NOT su on is needed to find the co	afficient to answer the question and
Q13.	chozen II.	ipal of a college is for om Mr. A, Mr. B, Mr. o	ning a committee. There	e are to be five members: three teachers,
	Mr. A wil	l serve only if <i>O</i> is also	on the committee. Mr.	C will not serve unless Mr. R and L also
	serve. Her	ither lyft. D nor lyft, F	will serve without the	other. If M serves, either N nor O can
	serve. Her	ich of the following is:	s will serve without the an acceptable committee	other. If <i>M</i> serves, either <i>N</i> nor <i>O</i> can e?
	serve. Wh	ich of the following is: $A, C, D, E, L$	s will serve without the an acceptable committee (B)	other. If <i>M</i> serves, either <i>N</i> nor <i>O</i> can e? <i>B</i> , <i>C</i> , <i>E</i> , <i>L</i> , <i>M</i>
	serve. Wh	ich of the following is : $A, C, D, E, L$	s will serve without the an acceptable committee (B)	other. If <i>M</i> serves, either <i>N</i> nor <i>O</i> can e?
Q14.	serve. Wh  (A)  (C)  (E)	ich of the following is:  A, C, D, E, L  B, D, E, L, O  D, E, L, M, N	will serve without the an acceptable committee (B) (D)	other. If <i>M</i> serves, either <i>N</i> nor <i>O</i> can e? <i>B</i> , <i>C</i> , <i>E</i> , <i>L</i> , <i>M C</i> , <i>D</i> , <i>E</i> , <i>L</i> , <i>M</i>
Q14.	serve. Wh  (A)  (C)  (E)	ich of the following is:  A, C, D, E, L  B, D, E, L, O  D, E, L, M, N	will serve without the an acceptable committee (B) (D) could include Mr. A and	other. If M serves, either N nor O can e? B, C, E, L, M C, D, E, L, M
Q14.	serve. Wh  (A)  (C)  (E)  How many	ich of the following is:  A, C, D, E, L  B, D, E, L, O  D, E, L, M, N  y different committees	will serve without the an acceptable committee (B) (D) could include Mr. A and (B)	other. If <i>M</i> serves, either <i>N</i> nor <i>O</i> can e?  B, C, E, L, M  C, D, E, L, M  i N?
Q14.	serve. Wh  (A)  (C)  (E)  How many  (A)	ich of the following is:  A, C, D, E, L  B, D, E, L, O  D, E, L, M, N  y different committees	will serve without the an acceptable committee (B) (D) could include Mr. A and	other. If M serves, either N nor O can e? B, C, E, L, M C, D, E, L, M
Q14. Q15.	serve. Wh  (A)  (C)  (E)  How many  (A)  (C)  (E)	ich of the following is:  A, C, D, E, L  B, D, E, L, O  D, E, L, M, N  y different committees  1  3  5	will serve without the an acceptable committee (B) (D)  could include Mr. A and (B) (D)	other. If M serves, either N nor O can e? B, C, E, L, M C, D, E, L, M I N? 2 4
	serve. Wh  (A)  (C)  (E)  How many  (A)  (C)  (E)	ich of the following is:  A, C, D, E, L  B, D, E, L, O  D, E, L, M, N  y different committees  1  3  5	will serve without the an acceptable committee (B) (D)  could include Mr. A and (B) (D)	other. If M serves, either N nor O can e?  B, C, E, L, M  C, D, E, L, M  i N?  2  4  on the committee?
	serve. Wh  (A)  (C)  (E)  How many  (A)  (C)  (E)  If N and O  (A)	ich of the following is:  A, C, D, E, L  B, D, E, L, O  D, E, L, M, N  y different committees  1  3  5  are both on the comm	will serve without the an acceptable committee (B) (D) could include Mr. A and (B) (D)	other. If M serves, either N nor O can e?  B, C, E, L, M  C, D, E, L, M  i N?  2  4  on the committee?  B
	serve. We serve. Wh (A) (C) (E) How many (A) (C) (E) If N and O	ich of the following is:  A, C, D, E, L  B, D, E, L, O  D, E, L, M, N  y different committees  1  3  5  Fare both on the comm	will serve without the an acceptable committee (B) (D)  could include Mr. A and (B) (D)	other. If M serves, either N nor O can e?  B, C, E, L, M  C, D, E, L, M  i N?  2  4  on the committee?
Q15.	serve. Wh  (A)  (C)  (E)  How many  (A)  (C)  (E)  If N and O  (A)  (C)  (E)	ich of the following is:  A, C, D, E, L  B, D, E, L, O  D, E, L, M, N  y different committees  1  3  5  are both on the comm  A  C  L	will serve without the an acceptable committee (B) (D)  could include Mr. A and (B) (D)  nittee, who clse must be could (B) (D)	other. If M serves, either N nor O can e?  B, C, E, L, M  C, D, E, L, M  i N?  2  4  on the committee?  B  D
Q15.	serve. We serve. Wh (A) (C) (E) How many (A) (C) (E) If N and O (A) (C) (E) In how ma	ich of the following is:  A, C, D, E, L  B, D, E, L, O  D, E, L, M, N  y different committees  1  3  5  are both on the comm  A  C  L	will serve without the an acceptable committee (B) (D)  could include Mr. A and (B) (D)  nittee, who clse must be o (B) (D)  the principal select an acceptable and acceptable committee.	other. If M serves, either N nor O can e?  B, C, E, L, M  C, D, E, L, M  i N?  2  4  on the committee?  B  D  cceptable committee?
	serve. Wh  (A)  (C)  (E)  How many  (A)  (C)  (E)  If N and O  (A)  (C)  (E)	ich of the following is:  A, C, D, E, L  B, D, E, L, O  D, E, L, M, N  y different committees  1  3  5  are both on the comm  A  C  L  ny different ways can	will serve without the an acceptable committee (B) (D)  could include Mr. A and (B) (D)  nittee, who clse must be could (B) (D)	other. If M serves, either N nor O can e?  B, C, E, L, M  C, D, E, L, M  i N?  2  4  on the committee?  B  D

### Solution 1-4

We summarize the given paragraph as:

- Everyone must sit in a seat or on a bench but
  - A women must sit on each bench.
  - Either X or Y must sit in the driver's seat.
  - C must sit immediately beside E.
- There are three women and 5 children in the van.
- iii) There are two benches behind the front seats.
- iv) Each bench has room for exactly three people.
- The van has a driver's seat and one passenger scat in the front.

Ç

- Q1. (B) There are five options given and asked which of the following sit on the front passenger seat. C cannot sit in the front passenger's seat, because by given restrictions C must sit immediately beside E, and there are only one passenger seat in front, so C cannot sit in the front passenger seat. X, Y and Z also could not sit in front seat, because by the given restriction, either X or Y must sit in the driver's seat and a woman must sit on each bench. So, if Y sits on driver's seat, then X and Z must be on benches, similarly, if X sits on driver's seat then Y and Z must be on the benches. Hence, X, Y and Z cannot sit on front passenger's seat. The possible children who can sit on front passenger's seat are A, B and D. But D is the only name from these three (A, B and D) names in the given choices. Hence the correct answer is choice (B).
- Q2. (D) Take first choice A, C and E. Here we see that C and E must sit together, it is also restricted that a woman must sit on a bench, but A is not a women. Hence, choice A is not a correct answer. Take second choice, A, C and Z. Because C must sit beside E, so this choice is not acceptable. Take third choice, A, Y and Z. In this choice Y and Z are women, and according to given restriction, a woman must sit on each bench. Now if Y and Z sit on a same bench, then X will be on driving seat. In this case a bench will be without a woman. Hence, choice C is also not acceptable combination. Now take choice D, i.e., B, D and Y. In this choice, there is only one woman Y since C and E not occurring separately. So this choice is acceptable. In last choice, since E is sitting without C, so this choice is also not acceptable. Hence the best answer is choice D.
- Q3. (E) In this question, we should choose a wrong combination in case of, if A sits immediately beside Z. Take choice A, C sits immediately beside Y. This is correct choice, because there is only one woman Y and one child C. The third child may be E. According to second choice, "D sets immediately beside Z". It may also be possible that D may sit beside Z. Here Z is only one woman on the bench, the third child may be A, according to this question. According to third choice, B sits in the front passenger seat. This is also possible. Because, women X, Y, Z and children A, C and E cannot sit on front passenger's seat. So B may sit in front passenger's seat. The fourth choice, D may also be true, because if A sits immediately beside Z, then there is one seat of a child is empty on that bench. Since, C sits beside E, so C and E may not be sit on this bench. Only B or D can sit on that empty seat. Hence, choice D may be possible. According to choice E, B sits on the same bench as X." Since, X is a woman and she cannot sit on that bench with other woman Z. So, B cannot sit as X. This choice may not be possible. Hence the correct answer is choice E.
- Q4. (E) In this question, it is understood that C and Y are not on the same bench. Thus E is also not on the same bench where Y is. Take choice A, "B sits in a seat or on a bench that is in front of where E is sitting. From above discussion we concluded that woman Y is on the last bench since C and E must sit together, therefore B, A and D can sit only in front passenger's seat. Now, take second choice, according to this, D sits in a seat or on a bench that is in front of where A is sitting." This is also incorrect choice, because C and E sit between front and a last bench, so D can sit with A or behind C and E. According to third choice, "A sits on the same bench as B." A can sit both B and D not only B. Choice C, may also be true, but choice D may not be possible, because C and E must sit together. Thus if E sits as Z then the third may be X.

#### Solution 5-7

Here, we decompose the given paragraph:

- i) There are four computer operators, Ali, Babar, Cheema and Dar.
- ii) Each have to perform their duties on four different days.
- iii) Days of duty are: Thursday, Friday, Saturday and Sunday.
- iv) Checma has his duty day before Ali.
- v) Dar has his duty day later than Babar.
- **Q5.** (C). In choice A, Cheema will perform his duty a day before Ali, this is according to the given restriction, but by the given restriction, Dar's duty should be a day later than Babar. Here, the Dar's duty is before Babar. Thus, this combination is not acceptable. In second choice, there is not a day's gap between Cheema and Ali, so this is also not acceptable. Choice C, is a right combination because,

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Cheema will perform his duty a day before Ali, and Dar will perform his duty a day later than Babar. Hence, the correct answer is choice C.

Q6. (E) If Cheema has his duty on Saturday, then the possible schedule is:

Thursday	Friday	Saturday	Sunday
Babar	Dar	Cheema	Ali

Hence, the correct answer is choice E.

Q7. (D) If Cheema has his duty on Thursday, the possible schedule is:

TI I		7, 1	bollodale (5,
Thursday	Friday	Saturday	Sunday
Cheema	Babar	Ali	Dar

which is acceptable according to the given restrictions.

If Babar has his duty on Thursday, then the possible schedule is:

Thursday	Friday	Saturday	Sunday
Babar	Cheema	Dar	Ali

which is also acceptable according to the given restrictions.

If Dar has his duty on Saturday, then the above schedule is formed, which is acceptable. If Babar has his duty on Sunday, then it is not possible to follow the given restrictions. Because, Dar has his duty later than Babar. So, it is not possible to perform Dar duty if Babar perform his duty on Sunday. Because Sunday is the last day in the given schedule. Hence the correct answer is choice D.

Q8. (A) We set a proportion, to solve this problem

	,		- with brookers				
T	ime in seconds		Problems		Time in second		Problems
	50	:	1	::	x	;	150
<u>50</u>	$=\frac{x}{150}$						

$$\Rightarrow x = 150 \times 50 \implies X = 7500 \text{ seconds} = 2 \text{ hours and 5 minutes}$$

So, statement X, ALONE is sufficient to solve this problem. Hence, the correct answer is choice A.

- Q9. (A) Since, the journey started at 6 PM and ended at 2 AM, so this journey is 8 hours. The average speed of the horse is  $=\frac{80}{8}=10$  miles per hour. So, statement X, ALONE is sufficient to solve this problem. Hence, the correct answer is choice A.
- Q10 (D) Statements X and Y are not sufficient to answer.
- Q11.(B) Average speed of the runner = 9.2 m/hour

Average speed 
$$= \frac{\text{Distance travelled}}{\text{time}}$$

$$9.2 = \frac{46}{t}$$

$$\Rightarrow t = \frac{46}{9.2} = 5 \text{ hours}$$

So, statement Y, ALONE is sufficient but X alone is not sufficient to answer this question. Hence, the correct answer is choice B.

Q12.(D) COMBINED statements X and Y are not sufficient to answer the question and some additional information is needed to find the correct answer.

#### Solution 13-16

is

Here, we decompose the given paragraph:

i) The principal of college is forming a committee of five members.

- ii) Three teachers chosen from five teachers, Mr. A, Mr. B, Mr. C, Mr. D and Mr. E.
- iii) Two students chosen from four students, L, M, N and O.
- iv) Mr. A will serve only if O is also in the committee.
- v) Mr. C will not serve unless Mr. B and L also serve.
- vi) Neither Mr. D nor Mr. E will serve without the other.
- vii) If M serves, neither N nor O can serve.
- Q13.(C) Take choice A i.e., A, C, D, E and L, this choice will not be acceptable because according to the given condition, Mr. A will serve only if O is also in the committee. Take choice B i.e., B, C, E, L, M. This choice is also not acceptable, because according to the given restriction, neither Mr. D not Mr. E will serve without the other. Herc, E is without D. Take choice C i.e., B, D, E, L, O. Since, this choice satisfies all the given restrictions. So this combination is acceptable for committee.
- Q14.(A) There is only possible committee can be formed including Mr. A and N. The combination of this committee is A, D, E, N, O. Hence the correct answer is choice A.
- Q15.(C) If N and O are both on the committee, then the other three members should all be teachers. Since, Mr. C will not serve unless Mr. B and L also serve. So Mr. C would not be on the committee, If he is on the committee, the third student L must include the other two students N and O. Thus the correct answer is choice C.
- Q16.(C) The principal can select acceptable committee in the following ways:
  - 1. B, D, E, L, O
  - 2. A, D, E, N, O
  - 3. A, C, B, L, O
  - 4. D, E, M, B, L
  - 5. C, B, L, N, A
  - 6. A, B, O, L, C
  - 7. D, E, B, L, N

Hence, the correct answer is choice C.

### III. Verbal Section

No. of Questions = 25

Select the correct answer for each question and blacken the corresponding circle in the answer sheet.

Instructions (1-10): In this part of test, you have 10 MCQs about English. Each sentence below has one or two blanks, each blank shows that something has been omitted. Choose the correct answer from the four answer choices given with each question, numbered (A), (B), (C), (D).

1.	She turned	this place_	look	ing for h	er keys.
	7.83	771			

(A) Thoroughly

(B) Inside out

(C) Up and down

- (D) In and out
- 2. It is widely believed that a nuclear war could \_\_\_\_\_ enough smoke and dust to black out the sun and freeze the earth.
  - (A) Billow

(B) Extinguish

(C) Generate

- (D) Duplicate
- 3. Many kinds of harmful viruses are unhindered when passing through different parts of the host organism; indeed, there are few organic substances which such viruses cannot \_\_\_\_\_\_
  - (A) Undermine

**B**) Disseminate

(C) Aerate

- (D) Exterminate
- 4. The light kept flashing \_\_\_\_\_ all night long.
  - (A) One and of

(B) On and off

(C) Up and down

(D) In and out

NT:

5.

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lettere relation

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**(D)** 

Friend: Foe

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(A) Mature: Juvenile

(B) Withdrawn: Reserved

(C) Evasive: Elusive

(D) Derivative: Traditional

Q2.

Q3.

O4.

Q5.

Q6.

Q7.

**O8.** 

09.

Q10

### 20. SALVAGE: TREASURE

(A) Settle: Argument

- (B) Incorporate: Company
- (C) Send: Correspondence
- (D) Rescue: Victim

### Read the following passage carefully and answer the question given at its end:

Something is radically wrong with the entire structure of human relationship that makes man delight in killing man, whether it be in the name of civilization or religion or anything else. Two wrongs do not make a right, hatred must beget hatred. It is this fundamental truth that women have got to bring home to the people in their respective countries, no peace treaties can avail that have revenge as their basis and self righteous arrogance and hypocrisy in the so called victors. But women are the natural preservers of life.

- 21. Which of the following expresses most accurately the idea contained in the opening sentence of the passage?
  - (A) Man destroying another man is a painful practice.
  - (B) A social structure that permits people to kill each other for religion is inherently rotten.
  - (C) It is strange that one religion encourages its followers to kill the followers of another religion.
  - (D) It is wrong on man's part to derive pleasure out of killing others for any motive whatsoever.
- 22. The expression "Two wrongs do not make a right' means that:
  - (A) A wrong action in retaliation does not mend matters.
  - (B) Hatred destroys the person who perpetrates it.
  - (C) A tit for tat policy aggravates hatred.
  - (D) Even repeated assertions of a wrong statement do not make it right.
- 23. Which of the following statements is not implied in the passage?
  - (A) It is human tendency to kill others professing different religion.
  - (B) It is the duty of women to foster peace and harmony amongst their countrymen.
  - (C) Peace treaties among nations tend to establish peace in the world.
  - (D) If you hate someone, he is bound to respond with the same feeling.
- 24. Which word is opposite in meaning to 'preserver' as used in the passage?
  - (A) Enemy

(B) Destroyer

(C) Rival

- (D) Belligerent
- 25. Which of the following would sum up most suitably the central idea of the passage?
  - (A) The role of women in the world of hatred and violence
  - (B) Man's instinct of destroying others
  - (C) Hatred leads to further hatred
  - (D) The significance of peace treaties

#### **ANSWERS**

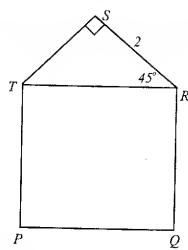
1.	(B)	2.	(C)	3.	(D)	7.	(B)	5.	(B)
6.	(D)	7.	(B)	8.	(B)	9.	(B)	10.	<b>(B)</b>
11.	(C)	12.	(C)	13.	(A)	14.	(D)	15.	(A)
16.	<b>(D)</b>	17.	(B)	18.	(D)	19.	(A)	20.	(D)
21.	<b>(D)</b>	22.	(A)	23.	(C)	24.	(B)	25.	(A)

\*\*\*\*\*\*\*



### GRE - GAT TEST 2

	Qua	antitative Section	I	No. of Questions = 20			
Q1.	If p and q must be tr		1  if  69(p+q) =	(69 + p)q, then which of the following			
	(A)	p = 69		p+q=pq			
	(C)	<i>p</i> < 1	(D)	q = 69			
Q2.		Town is divided into p division c players. How many players are		n has c cricket team, and each cricke atire town?			
	(A)	pcx	<b>(B)</b>	p+c+x			
	( <b>C</b> )	$\frac{pc}{x}$	(D)	$\frac{px}{c}$			
Q3.,	What is th	e value of x if $2^{10} \times 8^2 = 4^2 \times 2^x$ ?					
	(A)		(B)	8			
	(C)		(D)	12			
Q4.	chooses a What is th	card randomly. He wins if the r e probability that Hamza to win	number on the 1?	egers from 1 to 35 are written, Hamzard he chooses is a multiple of 3 or 7			
	(A) (C)	5	(B)				
	(C)	$\frac{1}{7}$	(D)	$\frac{3}{7}$			
Q5.	Which of integers?	the following cannot be expres	ssed as the sur	n of two or more eonsecutive positive			
	(A)	24	(B)	26			
	(C)	32	( <b>D</b> )	19			
Q6,				from y countries. If each country is delegates does each country has?			
	(A)	$\frac{x}{v}$	(B)	$\frac{y}{x}$			
	(C)	$xv^2$	(D)	$yx^2$			
<b>Q7</b> .		nany positive numbers x is it true	* '	· ·			
	101 11011 11		x = x + x + x				
	(A)	1	(B)	2			
	(C)	0	(D)	3			
<b>Q8.</b>	The length		presented by p	+3,2p-3 and $3p-5$ . If the perimeter			
	' (A)	7.	(B)	12			
i	(C)	5	(D)	3			
Q9.		now 5 times as old as Maryium, l then. How old is Maryium now	but after 6 ycai	rs from now she will be 3 times as old a			
•	(A)	25	(B)	18			
, .	(C)	12.	(D)	30			
Q10.	• •	e perimeter of pentagon PQRST	` '				



a square and RST is a right triangle?

**(A)** 
$$2 + 2\sqrt{2}$$

(B) 
$$8 + 12\sqrt{2}$$

(C) 
$$4 + 6\sqrt{2}$$

(D) 
$$4 + \sqrt{2}$$

Q11. If 
$$4 - (4 - m) = 4$$
, then  $m =$ 

Q12. Munir purchased some shares of stock at \$20 per share. Three months later the stock was worth \$40 per share. What was the percentage increase in the value of Munir's shares?

 $\mathbf{Q}1$ 

Q2

Q1

Q2.

Q13. If 
$$a^4 = 10$$
, then  $a^6 = ?$ 

(C) 
$$10\sqrt{10}$$

(D) 
$$100\sqrt{10}$$

Q14. If 
$$5x = 15$$
, then  $3x =$ 

Q15. If 
$$4x = 144$$
, then  $\frac{x}{4} =$ 

Q16. The following chart shows the value of an investment in January of each year from 2000 to 2005. In which year the percent increase in the value of the investment is the greatest?

Year	Values of Investment
2000	\$175
2001	\$275
2002	\$475
2003	\$775
2004	\$1225
2005	\$1825



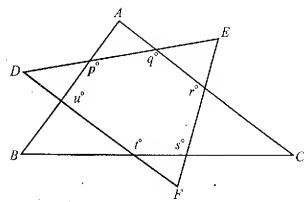
- Q17. The average (Arithmetic Mean) of two numbers is m. If one of the number is 12, what is the other?
  - **(A)** m-6

**(B)** 2m - 6

(C) m - 12

**(D)** 2(m-6)

Q18.



In the figure above, what is the value of p + q + r + s + t + u?

380 (A)

180 (B)

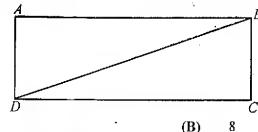
(C) 720 **(D)** 1260

Q19. If 
$$x\left(\frac{3}{7}\right) = \left(\frac{3}{7}\right)y$$
, then  $\frac{x}{y} =$ 

**(B)** 

(D)

Q20. If the perimeter of the rectangle ABCD is 16, what is the perimeter of  $\triangle BCD$ ?



(A) 7

**(B)** 

- (C)  $8\sqrt{2}$
- **(D)** It is not possible to determine from the given information.

Q2. (A) Since, Ravi Town is divided into p divisions and each division has C team. So, there are pc teams in

$$69(p+q) = 69p + 69q$$
 (By distributive law)  
 $(69+p)q = 69q + pq$  ( // )

Then 
$$69p + 69q = 69q + pq$$

$$\Rightarrow$$
 69 $p = pq$ 

$$\Rightarrow$$
 q = 69 (Dividing both sides by p)

- Ravi Town. Now, because there are x players in each team, thus, there are  $pc \times x = pcx$  players in Ravi Town.
- $2^{10} \times 8^2$
- $=4^2\times 2^x$

$$\Rightarrow 2^{10} \times (2^3)^2 = (2^2)^2 \times 2^x$$

$$\Rightarrow 2^{10} \times 2^6 = 2^4 \times 2^x$$

$$\Rightarrow 2^{10} \times 2^6 = 2^4 \times 2^x$$
$$\Rightarrow 2^{10+6} = 2^4 \times 2^x$$

$$\Rightarrow \frac{2^{16}}{2^4} = 2^x$$

$$\Rightarrow 2^{16} \times 2^{-4} = 2^x$$

$$\Rightarrow 2^{16-4} = 2^x$$

$$\Rightarrow 2^{12} = 2^x$$

$$\Rightarrow x = 12$$

Q4. (D) Let  $E_1$  be the event that the outcome is multiple of 3, then

$$E_1 = \{3, 6, 9, 12, 15, 18, 21, 24, 27, 30, 33\}$$

$$\Rightarrow n(E_1) = 11$$

Let  $E_2$  be the event that outcome is multiple of 7, then

$$E_2 = \{7, 14, 21, 28, 35\}$$

$$n(E_2) = 5$$

Now 
$$E_1 \cup E_2 = \{3,6,7,9,12,14,15,18,21,24,27,28,30,33,35\}$$

$$\Rightarrow n(E_1 \cup E_2) = 15$$

$$P(E_1 \cup E_2) = \frac{15}{35}$$

$$=\frac{3}{7}$$

Q5. (C) Any odd number can be expressed as the sum of two consecutive integers:

$$19 = 9 + 10, 23 = 11 + 12, 24 = 7 + 8 + 9$$

$$26 = 5 + 6 + 7 + 8$$

So eliminate A, B, D and E

Thus the answer is 32.

Q6. (A) Dividing the number of delegates by the number of countries, we have

$$\frac{x}{y}$$

Q7. (A) The given equation can be written as  $x^3 = 3x$ . Since x is positive, dividing each side of the equation by x, we have

$$x^2 = 3 \Rightarrow x = \pm \sqrt{3}$$

But x is positive, so there is only 1 positive integer that satisfies this equation.

Q8. Since the perimeter of the triangle is 19,

$$p+3+2p-3+3p-5=19$$

$$6p - 5 = 19$$

$$\Rightarrow$$
 6 $p = 19 + 5$ 

$$\Rightarrow$$
 6 $p = 24$ 

$$\Rightarrow \qquad p = 4$$

Now, substitute the value of p in the given sides, we get

$$4+3=7$$
,  $2(4)-3=5$ ,  $3(4)-5=7$ 

Hence the shortest side is 5.

Q9. (D) Let x be the age of Maryium, then

TS = 2

 $2\sqrt{2}$ 

 $2\sqrt{2}$ 

Now the age of Fatima is 5x.

Six years before "now" age of Maryium was x + 6 and age of Fatima was 5x + 6. Then

$$5x+6 = 3(x+6)$$

$$\Rightarrow$$
 5x + 6 = 3x + 18

$$\Rightarrow$$
  $5x - 3x = 18 - 6$ 

$$\Rightarrow$$
  $2x = 12$ 

$$\Rightarrow x = 6$$

Thus, age of Maryium is 5(6) = 30 years.

Q10.(C) In the given figure RST is a 45 - 45 - 90 triangle, thus if one side is 2, then and  $RT = 2\sqrt{2}$ .

Since all sides of a square have equal length and PQRT is a square, so its all sides are also equals to  $2\sqrt{2}$ .

Now perimeter of the pentagon PQRST is given by

$$2\sqrt{2} + 2\sqrt{2} + 2 + 2 + 2\sqrt{2} = 4 + 6\sqrt{2}$$
$$= 2(2 + 3\sqrt{2})^{2}$$

Q11.(A) 
$$4 - (4 - m) = 4$$
  
 $\Rightarrow 4 - 4 + m = 4$ 

Q12.(B) Increment in the share's = 
$$40 - 20 = 20$$
\$

m = 4

Percentage increment 
$$=\frac{20}{20} \times 100$$

Q13.(C) 
$$a^{4} = 10$$

$$\Rightarrow (a^{2})^{2} = 10 \Rightarrow \sqrt{(a^{2})^{2}} = \sqrt{10}$$

$$\Rightarrow a^{2} = \sqrt{10}$$
Now  $a^{6} = a^{4} \times a^{2} = 10 \times \sqrt{10}$ 

$$\Rightarrow a^{6} = 10\sqrt{10}$$

Q14.(D) Given that 
$$5x = 15$$

$$\Rightarrow \frac{5x}{5} = \frac{15}{5} \Rightarrow x = 3$$
$$\Rightarrow 3x = 3 \times 3$$

$$\Rightarrow 3x = 9$$

Q15.(B) 
$$4x = 144$$
  

$$\Rightarrow x = \frac{144}{4} \Rightarrow x = 36$$

$$Now \frac{x}{4} = \frac{36}{4} \Rightarrow \frac{x}{4} = 9$$

Q16.(B) %age increase in a quantity

$$= \frac{\text{increment}}{\text{original}} \times 100$$

Now, we check the %age increment given in the table

In 2001, %age increase = 
$$\frac{275-175}{175} \times 100$$

$$= \frac{100}{175} \times 100 = 57.12$$

In 2002, %age increase = 
$$\frac{475 - 275}{275} \times 100 = 72.73$$
  
=  $\frac{200}{275} \times 100 = 72.73$ 

In 2003, %age increase = 
$$\frac{775 - 475}{475} \times 100$$
  
=  $\frac{300}{475} \times 100 = 63.15$ 

In 2004, %age increase = 
$$\frac{1225-775}{775} \times 100$$
  
=  $\frac{450}{775} \times 100 = 58.06$ 

In 2005, %age increase = 
$$\frac{1825 - 1225}{1225} \times 100$$
  
=  $\frac{600}{1225} \times 100 = 48.98$ 

Q17.(D) Let the other number be y, then by given condition

$$m = \frac{12 + y}{2} \Rightarrow 2m = 12 + y$$
$$\Rightarrow 2m - 12 = y$$
$$\Rightarrow y = 2(m - 6)$$

Q18.(C) The interior side of the shape (star) is a six-sided figure (hexagon).

Now the sum of the angles of six-sided figure is (n-2)180

$$\Rightarrow (6-2)180$$
$$\Rightarrow 4(180) = 720$$

Q19.(A) 
$$x\left(\frac{3}{7}\right) = \left(\frac{3}{7}\right)y$$

$$\Rightarrow x = y$$
 (Dividing both sides by  $\frac{3}{7}$ )

$$\Rightarrow \frac{x}{y} = 1$$

Q20. Since, we cannot find the value of BD from the given information. Therefore, we cannot find the area of  $\triangle BCD$ .

### II. Analytical Section

### No. of Questions = 20

### For questions 1 to 4

A builder will build five houses in New Housing Scheme on a street that currently has no houses. The builder will select from seven different models of houses — L, M, N, O, P, Q and R. The Development Authority has placed the following restrictions on the builder: No model can be selected for more than one house. Either model O must be select or model R must be selected, but both cannot be selected. If model Q is selected, then model N cannot be selected. If model M is selected, then model O cannot be selected.

Į1.	also be selec	eted?	,	
	(A)	L	<b>(B)</b>	0
	(C)	P	<b>(D)</b>	Q
	( <b>E</b> )	R		
Q2.	If <i>L</i> , <i>M</i> and the other tw	P are three of the models selected for two models selected?	he stre	et, then which of the following must be
	(A)	N and O	(B)	N and Q
	(C)	N and R	<b>(D)</b>	O and Q
	(E)	Q and R		
Q3.	Which of t	he following is an acceptable combin		f models that ean be selected for the
		L, M, N, P, Q	<b>(B)</b>	L, M, P, Q, R
	` ,	L, N, P, Q, R	<b>(D)</b>	M, N, O, P, Q
	<b>(E)</b>	N, O, P, Q, R		
Q4.	The model		et, then	the other model NOT selected must be
	(A)	•	(B)	M
	(C)		<b>(D)</b>	0
	<b>(E)</b>	P		
For q	uestions 5 to	7		leven seats around it. Five girls (Fatima,
Q5.	A CONTRACTOR OF THE CONTRACTOR	n Javed does not sit next to Osama.  he following is a possible seating order  Empty seat, Bilal, Fatima, Najam,  Maryam, Iram, Hamza, Osama, Amna,  Javed and Sana	around (B)	the table? Empty seat, Bilal, Fatima, Najam, Maryam, Javed, Amna, Sana, Osama, Iram, Hamza
	(C)		<b>(D)</b>	Empty seat, Sana, Bilal, Fatima, Najam, Maryam, Javed, Osama, Amna, Hamza, Iram
	(E)	Empty seat, Iram, Bilal, Fatima, Najam, Maryam, Javed, Amna, Osama, Sana, Hamza		
Q6.	If Javed le	aves bis seat and occupies the empty se	at, his r	new scating position would be between:
	(A)	Bilal and Fatima	(B)	Iram and Najam
	(C)	Fatima and Najam	<b>(D)</b>	Osama and Maryam
	<b>(E)</b>	Amna and Maryam		
Q7.	If Maryan	n, Hamza, Iram, Javed and Najam are mpletion of the seating order after Naja	seated i am?	in that order, which of the following is a
•	(A)	Fatima, Bilal, Sana, Osama, Amna, empty seats	(B)	Fatima, Bilal, Osama, Sana, empty seat, Amna
	(C)	Bilal, Amna, Fatima, Osama, Sana, empty seats	<b>(D)</b>	Fatima, Bilal, Amna, Osama, empty seats, Sana
		• •		
	<b>(E)</b>	Fatima, Bilal, Sana, empty seats, Amna, Osama		·

### For questions 8 to 12

The accounts staff of the Mark corporation presently consists of three book-keepers (X, Y and Z) and five Data Entry Operators (M, N, O, P and Q). Management is planning to open a new office in another city sending three Data Entry Operators and two book-keepers from the present staff. To do so they plan to separate certain individuals who do not function well together. The following guidelines were established to set up the new office:

- Book-keepers X and Z are constantly finding faults with one another therefore should not be sent together. (i) to the new office.
- (ii) Z and N function well alone but not as a team. They should be separated.
- (iii) M and P have not been on speaking terms for many months. They should not go together.
- (iv) Since M and O have been competing for a promotion, they should not be in one team. Based on the above information, find the correct answers to the following questions:
- If Y insists on staying back then how many combinations are possible? Q8.
  - (A)

**(B)** 2

(C) 1

- **(D)** None
- If X is to be moved as one of the book-keepers, which of the following CANNOT be a possible O9. working unit?
  - (A) XYMNO

**(B)** XYNOQ

(C) XYMPQ

- **(D) XYNPQ**
- If Z is sent to the new office then which member of the staff CANNOT be sent? Q10.
  - (A)

(B)

(C) 0

- P (D)
- If M is sent to the new office then which of the following is a possible team? 011.
  - (A) XYMNP

**(B)** YZMOO

(C) YZMNO

- (D) **XYMNQ**
- If both Z and O are moved to the new office, how many combinations are possible? O12.

(A)

**(B)** 4

**(C)** 3

(D) 2

Direction: For questions 13 to 16

Each of the following problems has a question and two statements which are labeled 1 and 2. Use the data given in 1 and 2 together with other information given in the statement, and find a correct answer by using basic mathematics and everyday facts.

- How many bulbs does Munir have?
  - 1. He bought two boxes each containing 12 bulbs.
  - 2. He lent three bulbs to Khalid.
    - Statement 1. ALONE is sufficient but 2. ALONE is not sufficient to answer this question.

NEITHER of them is sufficient

sufficient to answer the question but

- **(B)**
- Statements 1 and 2. TOGETHER are
  - Statements 1 and 2. COMBINED are (D) not sufficient to answer the question
- If M > N and O > P, then, M + O > N + P. Is S > T? Q14.

ALONE.

1. S + A > T + B

**(C)** 

2. A > B Statement 2. ALONE is sufficient but 1. ALONE is not sufficient to answer this question.

2

3

4

5

6

7

and additional information is needed to find the correct answer.

**(B)** 

**(B)** 

**(D)** 

**(D)** 



- Statement 1. ALONE is sufficient but (A) 2. ALONE is not sufficient to answer this question.
- **(C)** Statements 1 and 2. COMBINED are sufficient to answer the question but NEITHER of them is sufficient ALONE.
- Statement 2. ALONE is sufficient but 1. ALONE is not sufficient to answer this question.
- Statements 1 and 2. COMBINED are **(D)** not sufficient to answer the question and additional information is needed to find the correct answer.
- In Lahore Zoo, there are 37 deer. How many small black deer are there? 015.
  - 1. 12 of deer are small.
  - 2. There are 20 black deer in the Zoo.
    - Statement 1. ALONE is sufficient but 2. ALONE is not sufficient to answer this question.
    - **(C)** Statements 1 and 2, TOGETHER are sufficient to answer the question but NEITHER of them is sufficient ALONE.
- Statement 2. ALONE is sufficient but 1. ALONE is not sufficient to answer this question.
- Statements 1 and 2. COMBINED are not sufficient to answer the question and additional information is needed to find the correct answer.
- Can there be more than 150 pictures in a 30-page book? Q16.
  - There is at least two pictures in each page.
  - There are no more than 4 pictures in any page. 2.
    - Statement 1. ALONE is sufficient but (A) **(B)** 2. ALONE is not sufficient to answer this question.
    - Statements 1 and 2. TOGETHER are (C) sufficient to answer the question but NEITHER of them is sufficient ALONE.
- Statement 2. ALONE is sufficient but 1. ALONE is not sufficient to answer this question.
- Statements 1 and 2. COMBINED are not sufficient to answer the question and additional information is needed to find the correct answer.



### Solution 1 to 4

From the given paragraph, we write the following main points:

- A builder will build five houses on a street that currently has no house on it. 1.
- There are 7 different models of houses L, M, N, O, P, Q and R. 2.
- The builder will select five different models from L, M, N, O, P, Q and R. 3.
- No model can be selected for more than one house. 4.
- Either model O must be selected or model R must be selected, but both cannot be selected. 5,
- If model Q is selected, then model N must also be selected. 6.
- If M is selected, then model O cannot be selected.
- Q1. (E) If model M is selected, then builder should ignore O. We see from above point 5 that, either O must be selected or model R must be selected, but both cannot be selected. So, if builder cannot select O, he would select R. Hence the correct answer is choice E.
- Q2. (C) If models L, M, and P have already been selected, then model O cannot be selected because O will not be selected if M has already selected. Since, O will not be selected, therefore R will be surely selected. Hence, the fourth model is R. Now, fifth model will be selected from N and Q. Here, we suggest N as a fifth model, because if the builder choose Q as a model, then model N must also be chosen, and there will be only five models must be selected. Hence the correct answer is choice C.
- Q3. (C) Take choice "A", L, M, N, P, Q. This choice is not acceptable, because, either model O must be selected or model R must be selected. In this choice, any of them (O or R) is not present. Take choice

"B", L, M, P, Q, R. According to the given condition, if model Q is selected, then model N must also be selected. In this choice, Q is without N. Hence, this choice is also not acceptable. Take choice "C", L, N, P, Q, R. Since, this choice satisfies all the conditions.

Hence, the correct answer is choice C.

Q4. (B) If, the model R is one model not selected, then model O must be selected, because by the given condition, either model O must be selected or model R must be selected. Now in this case O must be selected, but M cannot be selected, because, according to the given restriction, if M is selected, then model O cannot be selected. Hence, the correct answer is choice B.

#### Solution 5 to 7

We simplify the given problem in the following points:

- 1. There are eleven seats around a circular table.
- 2. There are five girls (Fatima, Maryam, Iram, Sana and Amna) who will be seated. For convenience, we denote them by F, M, I, S and A.
- 3. There are five boys (Bilal, Najam, Hamza, Osama and Javed) who will be seated. For convenience, we denote them by B, N, H, O and J.
- 4. None of the girls are seated in a seat adjacent to another girl.
- 5. Fatima sits between Bilal and Najam, and next to each of them Javed does not sit next to Osama.
- Q5. (E) Take choice, "A". The choice is not acceptable because in this choice, Maryam sits adjacent to another girl Iram. But by the given restriction none of the girls are seated in a seat adjacent to another girl. In choice "B", since Amna sits adjacent to Sana, so this choice is also not acceptable. Clearly, the choice "E" is the only choice that satisfies all the condition. Hence, the correct answer is choice E.
- Q6. (E) The correct order of seating is

Empty, Iram, Bilal, Fatima, Najam, Maryam, Javed, Amna, Osama, Sana, Hamza.

If Javed leaves his seat empty then the above setting becomes Iram, Bilal, Fatima, Najam, Maryam, Empty, Amna, Osama, Sana, Hainza.

Clearly more setting is required between Maryam and Amna, because none of the girls are scated in a scat adjacent to another girl. Hence the correct answer is choice E.

Q7. (A) If Maryam, Hamza, Iram, Javed and Najam are seated in that order, the correct completion of the seating order is

Fatima, Bilal, Sana, Osama, Amna, empty seat.

Hence, the correct answer is choice A.

#### Solution 8 to 12

Brief points from the given paragraph are given below:

- 1. Accounts staff of Mark Corporation consists of three book-keepers (X, Y and Z) and five data entry operators (M, N, O, P and Q).
- 2. Management sending three Data entry operators and two book-keepers from the present staff to new office located to another city.
- 3. Book-keepers X and Z should not be sent together to the new office.
- 4. Z and N should be separated.
- 5. M and P should not go together.
- 6. M and O should not be in one team.
- Q8. (D) Since, book-keepers X and Z are constantly finding faults with one another, therefore they should not be sent together to the new office. But the management has decided to sent two book-keepers, now, if Y insists on staying back, then there would not be another combination of two book-keepers except X and Z. Hence the correct answer is choice D.

Q9 Q1

Q1

Q1

Q1

O1

Q1

Q1



- Q9. (C) Since M and P have not been on speaking terms for many months, so they should not go together. Hence, choice "C" cannot be a possible working unit.
- Q10 (A) If Z is sent to the new office, then X should not be sent and Y should be sent to the new office. Now, if Z is sent to new office, then N should not sent. Hence the correct answer is choice A.
- Q11.(D) If M is sent to the office, then we analyze the given options as:

Choice "A", XYMNP, this choice is not acceptable because M and P cannot be sent together.

Choice "B", YZMOQ, this choice is also not acceptable, because M and O should not be in one team.

Choice "C", YZMNQ, because Z and N should be separated, therefore, this choice is also not acceptable.

Choice "D", XYMNQ, since this combination satisfies all the conditions, so this choice is acceptable. Hence, the correct answer is choice "D".

- Q12.(A) If Z and O both are moved to the new office, then M should not be included in the team because M and O should not be in one team, also N should not be included in the team because Z and N should be separated. Therefore, only one combination YZOPQ, is possible, if Z and O both are moved to the new office. Hence, the correct answer is choice A.
- Q13.(C) Take 1 statement, Munir bought two boxes each containing 12 bulbs, so

Munir initially has  $12 \times 2 = 24$  bulbs

Now, take 2 statement, he lent three bulbs to Khalid, combining the two statements we find that Munir has 21 (24 - 3 = 21) bulbs. So, statements 1 and 2 TOGETHER are sufficient to answer the question but neither of them alone is sufficient. Hence, the correct choice is choice C.

Q14.(C) If M > N and O > P, then M + O > N + P

$$S > T = ?$$

Statement (1), S + A > T + B

Statement (2), A > B

We analyze the given problem, by supposing values of the variables involved in this problem

Let 
$$S = 7$$
 and  $T = 6$ , then

and Let A = 4 and B = 3, then

clearly, S > T and A > B, but

$$S + A > T + B$$

$$7 + 4 > 6 + 3$$

Hence, statements 1 and 2. TOGETHER are sufficient to answer the question but NEITHER of them alone is sufficient. Hence, the correct answer is choice C.

Q15.(D) Total deer in the  $Z_{00} = 37$ 

ot

Small dcer = 12

Black deer = 20

Small black deer =?

Since, a small deer may be black or not black, and a black deer may be small or not small, so we cannot find the exact answer from the given two statements, 1 and 2. Hence, the correct answer is choice D.

Q16.(B) Since, there are no more than 4 pictures in any page, so there are maximum  $30 \times 4 = 120$  pictures in the 30 pages book. Thus, statement (2) ALONE is sufficient but (1) ALONE is not sufficient to answer the question.

III. Verbal Section	No. of Questions = 25			
Select the correct answer for each question and blacken the corresponding circle in the answer sheet.				
Instructions (1-10): In this part of test, you have 10 ks, each blank shows that something has been omitted with each question numbered (4) (B) (C) (D)	MCQs about English. Each sentence below has one of ed. Choose the correct answer from the four answer ch			

		estion, numbered $(A)$ , $(B)$ , $(C)$ , $(D)$ .		
. He c	ouldn	't decide whether to read or study, h	ie was	
	(A)	Betwixt and between	(B)	For and against
	(C)	Pulled down	<b>(D)</b>	Over and out
Why	are yo	ou still sleeping? You'll be late	of bed now.	
	(A)	Out	(B)	Get out
	(C)	Get up	<b>(D)</b>	Up and out
You	have t	o wait Thursday.		
	(A)	Since	(B)	From .
	(C)	Ву	<b>(D)</b>	Until
All ti	he chil	dren went down measles.		
	(A)	With	(B)	From
,	( <b>C</b> )	Due to	<b>(D)</b>	Without
Auts with	live tu others	colonies based on; each n in performing necessary tasks.	nember coutribi	utes to the good of all by actively work
(	(A)	Heredity	(B)	Individualism
(	(C)	Cooperation	(D)	Reasoning
(	ettolds [A) [B)	some form of major crime in Incredible, Witnesses Astronomical, Experiences	in any year.	tes remains and that one in th
•	C)	rish cheffical, Experiences		
,		•		
(	•	Simultaneous, Perpetrates		
	D)	Simultaneous, Perpetrates Defeated, Prosecutes		
We go	D)	Simultaneous, Perpetrates	(B)	Into: At
We go	D) ot A)	Simultaneous, Perpetrates  Defeated, Prosecutes  the train Rawalpindi.	(B)	Into; At
We go	D)  ot A) C)	Simultaneous, Perpetrates  Defeated, Prosecutes	<b>(D)</b>	ln; At
We go (. () On the	D)  ot A) C)	Simultaneous, Perpetrates  Defeated, Prosecutes	(D) hing; I	In; At rather felt a great to God.
We go () () On the	D)  ot A) C) e top o	Simultaneous, Perpetrates  Defeated, Prosecutes  the train Rawalpindi.  On; In Into; In  f Mount Everest, I did not feel anyth	(D) hing; I a	In; At  rather felt a great to God.  Superstitious; Similarity
We go () () On th	D)  A) C) e top o A) C)	Simultaneous, Perpetrates  Defeated, Prosecutes	(D) hing; I	In; At rather felt a great to God.
We go () () On the () ()	D)  A) C) e top o A) C)	Simultaneous, Perpetrates Defeated, Prosecutesthe train Rawalpindi. On; In Into; In f Mount Everest, I did not feel anyth Sinful; Love Superhuman; Closeness	(D)  hing; I (B)  (D)	In; At  rather felt a great to God.  Superstitious; Similarity  Strange; Nearness
We go ( ( ( ( ( ( ( (	D) ot A) C) e top o A) C)is	Simultaneous, Perpetrates  Defeated, Prosecutes	(D) hing; I (B) (D) (B)	In; At  rather felt a great to God.  Superstitious; Similarity  Strange; Nearness  Criterion, Mistake
We go (	D)  ot A) C) e top o A) C)is A) C)	Simultaneous, Perpetrates Defeated, Prosecutesthe train Rawalpindi. On; In Into; In f Mount Everest, I did not feel anyte Sinful; Love Superhuman; Closeness a Norm, Standard Discipline, School	(D) hing; I. (B) (D) (B) (D)	In; At  rather felt a great to God.  Superstitious; Similarity  Strange; Nearness  Criterion, Mistake  Doctrine, Follower
We go	D)  ot A) C) e top o A) C)is A) C)	Simultaneous, Perpetrates  Defeated, Prosecutes  the train Rawalpindi.  On; In Into; In  f Mount Everest, I did not feel anyth Sinful; Love Superhuman; Closeness  a  Norm, Standard	(D) hing; I. (B) (D) (B) (D)	In; At  rather felt a great to God.  Superstitious; Similarity  Strange; Nearness  Criterion, Mistake  Doctrine, Follower

letter relati

12.

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# Dogar's Unique Fully Solved "NEW TESTING SYSTEM" GUIDE

NTS Guide

Instructions (11-20): Each question below consists of a related pair of words or phrases, followed by four lettered pairs of words or phrases numbered (A), (B), (C), (D). Choose the lettered pair that best expresses a relationship similar to that expressed in the pair given in the question.

1.	SILO: CO	PRN	·	
	(A)	Mill: Grain	(B)	Reservoir: Water
	(C)	Acre: Wheat	(D)	Paddy: Rice
2.	GAGGLE	: GEESE		
	(A)	Coop: Chickens	(B)	Muzzle: Dogs
	<b>(C)</b>	Gill: Fish	(D)	Swarm: Bees
3.	OBSTRUC	CTION: BUOY::		
	(A)	Construction: Building	(B)	Boy: Girl
,	(C)	Danger: Red Light	(D)	Iceberg: Titanic
4.	MARATH	ON: STAMINA::		
	(A)	Hurdle: Perseverance	(B)	Sprint: Celerity
	(C)	Relay: Independence	(D)	Ramble: Directness
5.	INTERES	T: FASCINATE		
	<b>(A)</b>	Vex: Enrage	<b>(B)</b>	Vindicate: Condemn
	(C)	Regret: Rue	(D)	Appall: Bother
6.	HORNS: H	BULL::		
	(A)	Hoofs: Horse	<b>(B)</b>	Wings: Eagle
	(C)	Mane: Lion	<b>(D)</b>	Antlers: Stge
7.	TOSS: HU	'RL::	•	
	(A)	Speak: Shout	<b>(B)</b>	Sense: Flourish
	<b>(C)</b>	Prepare: Emit	( <b>D</b> )	Consider: Formulate
8.	SHALE: G	EOLOGIST::		
	(A)	Catacombs: Estomologist	<b>(B)</b>	Reef: Astrologer
	(C)	Obelisk: Fireman	(D)	Aster: Botanist
9.	PERMEAT	E: REFUEL	•	
	(A)	Truculent: Merciful	<b>(B)</b>	Sadden: Pitiful
	(C)	Evaporate: Mournful	(D)	Penetrate: Sorrowful
0.	MUMBLE:	SPEAK::		
2	(A)	Adorn: Denude	<b>(B)</b>	Convert: Preach
	(C)	Plagiarize: Write	( <b>D</b> )	Delimit: Expand
D	1 47 6 11	•		

Read the following passages carefully and answer the questions given at its end:

Passage: Each nation has its own peculiar character which distinguishes it from others. But the people of the old have more points in which they are all like each other than points in which they are different. One type of son that is common in every country is the one who always tries to do as little as he possibly can and to get as in return as he can. His opposite, the man who is in the habit of doing more than is strictly necessary and is dy to accept what is offered in return, is rare everywhere. Both these types are usually unconscious of their facter. The man who avoids effort is always talking about his rights, he appears to think that society owes him a sant easy life. The man who is always doing more than his sheer talks of duties feels that the individual is in

debt to society, and not society to the individual. As a result of their view, neither of these men thinks that he behaves at all strangely.

# 21. What type of person is common in every nation?

- (A) A person who want to do little and get more
- (B) A person who want to do more and get little
- (C) Each person is different
- (D) There is no such type of person that is common in every country

# 22. A man who talks about his rights:

- (A) Avoids meeting other people
- (B) Avoids hard work
- (C) Knows his duties well
- (D) Believes in hard work

# 23. Which one of the following thinks that the individual is in debt to society?

- (A) A person who talks of his rights only
- (B) A person who is always doing more than his sheer talks of duties
- (C) Every citizen of the country
- (D) A person who talks of his duties only

Passage: A man who has no sense of history, Hitler declared is like a man who has no ears or eyes. He himself claimed to have had a passionate interest in history since his school days and he displayed considerable familiarity with the course of European history. His conversation was studied with historical reference and historical parallels. More than that Hitler's whole cast of thought was historical and his sense of mission was derived from his sense of history. Like his contemporary Spengler, Hitler was fascinated by the rise and fall of civilizations. He was himself born at a critical moment in European history when the liberal bourgeois world of nineteenth century was disintegrating. What would take its place? The future lay with the 'Jew-Rolshevik' ideology of the masses unless Europe could be saved by the Nazi racist ideology of the clite.

# 24. Who has no ears or eyes?

- (A) A man having sense of history
- (B) A man who has no sense of history
- (C) A man who has extra knowledge
- (D) A man having passionate interest in history

# 25. Hitler displayed familiarity with:

(A) Scientific facts

(B) American history

(C) European history

(D) None of these

### **ANSWERS**

1.	(A)	2.	(D)	3.	(D)	4.	(A)	5.	(C)
6.	(D)	7.	(B)	8.	(D)	9.	(A)	10.	(A)
11.	(B)	12.	(D)	13.	(C)	14.	(B)	15.	(A)
16.	<b>(D)</b>	17.	(A)	18.	(D)	19.	<b>(D)</b>	20.	(C)
21.	(A)	22.	(B)	23.	(C)	24.	(B)	25.	(C)

\*\*\*\*\*\*\*



(A) x > -3

# **GRE - GAT TEST 3**

#### I. Quantitative Section No. of Questions = 20Q1. If n is a multiple of 5 and m = 5n, which of the following will be the value of n + m? II. 100 III. 150 (A) I only (B) II only **(C)** I and II only I and III only **(D)** Q2. If the sum of the edges of a cuhe is 48 inches, the volume of the cuhe in inches is: 4096 cubic inches (B) 512 cubic inches (C)· 64 cubic inches (D) 1728 cubic inches The two numbers, whose sum is -3 and product is -40, are: Q3. (A) 15, -2(B) (C) -8.5**(D)** -8, -5Q4. If $n+3=n\times 3$ , then n=(A) **(B)** (C) **(D)** None of these The integral part of logarithm is called: Q5. (A) Characteristic **(B)** Mantissa (C) (D) Imaginary Q6. Which of the following expression has the greatest value? $3 \times 3 \div 3 + 3$ (A) **(B)** $3 \div 3 + 3 + 3$ $3 \times 3 - 3 \times 3$ (C) **(D)** $3 + 3 + 3 \times 3$ Q7. On the x-axis, the y-coordinate is: (A) 1 (B) (C) (D) Q8. If scales are bought at 35 rupees per dozen and sold at 3 scales for 10 rupees, the total profits on $5\frac{1}{2}$ dozen is: (A) 35 rupees (B) 23.5 rupees (C) 26.5 rupces **(D)** 27.5 rupees If x hooks cost \$3 each and y hooks cost \$7 each, then the average (arithmetic mean) cost, in dollars per book, is equal to: (A) **(B) (D)** If y < 2 and 2x - 3y = 0, which of the following must be true?

**(B)** 

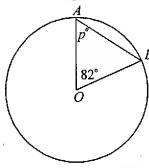
**(C)** x = 3

- **(D)** x < 3
- Q11. The angles of a pentagon are in the ratio 1:2:3:5:9. The smallest angle is:
  - (A) 72°

(B)  $45^{\circ}$ 

(C) 54°

- **(D)** 27°
- Q12. In the following figure, what is the value of p?



(A) 49

**(B)** 42

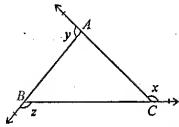
(C) 52

- (D) 78
- Q13. The number of cubic inches in one cubic foot is:
  - (A) 144 cubic inches

(B) 1728 cubic inches

(C) 1000 cubic inches

- (D) 27 cubic inches
- Q14. In the following figure, the sides of a triangle are produced. The sum of the exterior angles i.e.,  $\angle x + \angle y + \angle z =$



(A) 180°

(B) 360°

(C) 90°

- (D)  $270^{\circ}$
- Q15. In a right triangle, one of the angle is 60°. The side opposite to the angle is:
  - (A)  $\frac{1}{2}$  × hypotenuse

(B)  $\frac{1}{\sqrt{2}} \times \text{hypotenuse}$ 

(C)  $\frac{2}{3}$  × hypotenuse

- (D)  $\frac{\sqrt{3}}{2}$  × hypotenuse
- Q16. The number of degrees through which the hour hand of a clock moves in 2 hours and 12 minutes is:
  - (A) 72°

 $(\mathbf{B})$   $66^{\circ}$ 

(C) 60°

- (D)  $13^{\circ}$
- Q17. The height of a cylinder is 4 times its circumference, what is the volume of the cylinder in terms of its circumference, C?
  - (A)  $\frac{C^3}{2\pi}$

(B)  $\frac{2\pi}{C}$ 

(C)  $\frac{2C^3}{\pi}$ 

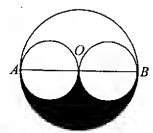
- (D)  $\frac{\pi}{2C}$
- 1218. What is the area of the circle which is inscribed in an equilateral triangle of side 24 cm<sup>2</sup>?

(A)  $24 \text{ m cm}^2$ 

**(B)**  $36 \text{ m cm}^2$ 

(C)  $48 \pi \text{ cm}^2$ 

- (D)  $18 \, \pi \, \text{cm}^2$
- Q19. In the following figure, the larger circle with radius 4 cms is touched internally by two smaller circles that also touch each other externally at the centre O of the larger circle. The area of the shaded region is:



(A)  $4\pi$ 

(B) 7π

(C)  $12\pi$ 

- (**D**) 16π
- Q20. The number of common tangents that can be drawn to two given circles at the most:
  - (A) one

(B) two

(C) three

- (D) four
- Explanatory Answers
- Q1. (D) Since n is the multiple 5, i.e.,

$$n = 5, 10, 15, 20, 25...$$

Now m = 5

$$m = 5n \Rightarrow m = 25, 50, 75, 100, \dots$$

Now m+n=(5+25), (10+50), (15+75), (20+100), (25+125),...

= 30, 60, 80, 120, 150

Hence the correct answer is choice D.

Q2. (C) As we know, a cube is a rectangular solid in which length, width and height are equal. Note that, length, width and height are the edges of the cube. Let e be the edge of the cube, then according to given condition:

Since a cube has 12 edges, 12e = 48  $\Rightarrow e = \frac{48}{12}$ .

$$\Rightarrow e = 4$$
 inches

Now, the volume of a cube  $= e^3 = (4)^3 = 64$ .

Q3. (C) The product of two numbers could be negative only if one of them is negative and the other is positive

Now,  $40 = 2 \times 2 \times 2 \times 5$ 

$$= 8 \times 5$$

utes

erms

1f we take 8, –ive and 5 as positive then,  $-8 \times 5 = 40$  and -8 + 5 = -3

Hence the required numbers are -8 and 5, and the correct answer is choice C.

Q4. (A) Civen that  $n + 3 = n \times 3$ , we substitute the numbers in the options

When,  $n = 1 \Rightarrow 1 + 3 \neq 1 \times 4$ ,  $\Rightarrow 4 \neq 3$ 

When, 
$$n = \frac{1}{2} \Rightarrow \frac{1}{2} + 3 \neq \frac{1}{2} \times 3$$
,  $\Rightarrow 3.5 \neq 1.5$ 

When,  $n = 1.5 \Rightarrow 1.5 + 3 = 1.5 \times 3 \Rightarrow 4.5 = 4.5$ 

Hence the correct answer is choice A.

- Q5. (A) The common logarithms consists of two parts, the integral part is known as characteristic and the decimal part is known as Mantissa. Hence the correct answer is choice A.
- Q6. (D) We solve expressions given in the options

$$3 \times 3 \div 3 + 3 = 9 \div 6 = 1.5$$

$$3 \div 3 + 3 + 3 = 1 + 6 = 7$$

$$3 \times 3 - 3 \times 3 = 9 - 9 = 0$$

$$3 \div 3 + 3 \times 3 = 1 + 9 = 10$$

Hence the correct answer is choice D.

- Q7. (B) On the x-axis the y-coordinate are always zero. Hence the correct answer is choice B.
- Q8. (D) We solve it by unitary method

1 scale cost = 
$$\frac{35}{12}$$

1 scale will sold 
$$=\frac{10}{3}$$

Profit in one scale 
$$=\frac{10}{3} - \frac{35}{12}$$

$$=\frac{5}{12}$$

Profit of 66 scales 
$$(5\frac{1}{2} \text{ dozen}) = \frac{5}{12} \times 66$$

$$=\frac{55}{2}=27\frac{1}{2}$$

Hence the correct answer is choice D.

Q9. (C) The total number of books is x + y, and their total cost is 3x + 7y dollars. Therefore, the average cost per book is

$$\frac{3x+7y}{x+y}$$
 dollars.

Thus, the best answer is choice C.

Q10.(D) It follows from 2x - 3y = 0 that  $y = \frac{2}{3}x$ 

So 
$$y < 2$$
  $\Rightarrow \frac{2}{3}x < 2 \Rightarrow 2x < 6$ 

$$\Rightarrow x < 3$$

Hence the best answer is choice D.

\* Note that choices A and B may be true.

But the exact and best choice is D.

Q11.(D) Sum of all angles of a pentagon =  $[(2 \times 5 - 4) \times 90]$ 

$$=(6 \times 90) = 540$$

Let the angle be x, 2x, 3x, 5x and 9x. Then

$$x + 2x + 3x + 5x + 9x = 540$$

$$\Rightarrow$$
 20x = 540  $\Rightarrow$  x = 27°

Q12.(A) In triangle AOB, since two of the sides are radii of the circles, and all the radius of a circle are equal, so the triangle is isosceles. Hence the unmarked angle is also p.



$$180 = 82 + x + x \implies 2x + 82 = 180$$
$$\Rightarrow 2x = 180 - 82 = 98$$
$$\Rightarrow x = \frac{98}{2} = 49$$

Hence the correct answer is choice A.

Q13.(B) Volume of a cube =  $e^3$ 

If e = 1 foot, then volume  $= (1)^3$ 

As (e = 1 feet = 12 inches), volume =  $(12 \text{ inches})^3$ 

= 1728 cubic inches

Hence the correct answer is choice B.

Q14.(B) Since every exterior angle is equal to the sum of opposite interior angles, so

$$\angle x = \angle A + \angle B$$
,  $\angle y = \angle B + \angle C$ 

and  $\angle z = \angle A + \angle C$ 

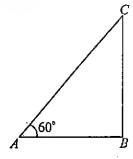
$$\angle x + \angle y + \angle z = 2(\angle A + \angle B + \angle C)$$

$$= 2(180)$$

$$= 360^{\circ}$$

Hence the correct answer is choice B.

Q15.(D) Let ABC be a triangle in which  $\angle A$  is 60°.



In 
$$\triangle ABC$$
,  $\frac{BC}{AC} = \sin 60^{\circ}$ 

$$\Rightarrow$$
 BC = (AC)  $\times \sin 60^{\circ}$ 

$$\Rightarrow$$
 BC = (hypotenuse)  $\times \frac{\sqrt{3}}{2}$ 

Hence the correct answer is choice D.

Q16.(B) The complete revolution of an hour hand subtends an angle of 360°. Since 360° is divided into 12 equal parts as an hour, thus each hour hand is  $\frac{360}{12} = 30^{\circ}$  with minute hand. If we divide 30° into 5 parts we get 12 minute rotation hour hand, i.e.,  $\frac{30}{5} = 6$ . Hence the angle of the hour hand at 2 hour and 12 minute is

$$30 \times 2 + 6 = (60 + 6)^{\circ}$$
  
=  $66^{\circ}$ 

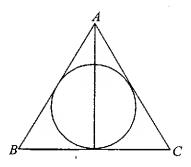
Q17.(C) Volume of a cylinder =  $V = \pi r^2 h$ According to given condition, h = 4C,

$$C = 2\pi r$$
  $\Rightarrow$   $r = \frac{C}{2\pi}$ 

Now V = 
$$\pi \left(\frac{C}{2\pi}\right)^2 (4C)$$
  
 $\Rightarrow V = \frac{2C^3}{\pi}$ 

Hence the correct answer is choice C.

Q18.(C) Here, we draw a figure



$$\frac{1}{2} \times 24 \times h = \frac{\sqrt{3}}{4} \times 24 \times 24$$

$$\Rightarrow \frac{h}{2} = \frac{\sqrt{3}}{4} \times 24$$

$$\Rightarrow h = 12\sqrt{3}$$

$$\Rightarrow h = 12\sqrt{3}$$

$$\therefore 3r = 12\sqrt{3} \text{ or } r = 4\sqrt{3}$$

$$\therefore$$
 Area of the circle =  $\pi r^2$ 

$$= \pi (4\sqrt{3})^2 = \pi (16(3))$$
$$= 48\pi$$

Hence the correct answer is choice C.

Q19.(B) Since the two smaller circles touch internally at the centre of the larger circle, they have equal radius; the diameter of each being 2 cm and radius of each is 1 cm.

Required Area = (Area of semi-circle with radius 4 cm) - (Area of semi-circle with radius 1 cm)

$$= \frac{1}{2} \times \pi \times (4)^2 - 2 \times \frac{1}{2} \times \pi \times (1)^2$$
$$= 8\pi - \pi$$

$$= 8\pi - \pi$$

$$=7\pi$$

Q20.(B) At the most two common tangents can be drawn to two circles.

# II. Analytical Section

No. of Questions = 20

#### For questions 1 to 2

A city map representing roads M, N, O, P, Q and R. Link roads cannot have the same colour in the map. The roads link to each other are as under:

Each M, N, P and Q has link to Q.

P has a link to Q.

Each of M and N has a link to R.

- 01. Which of the following roads can be the same colour as O on the map?
  - (A)

(C) Q

- R **(D)**
- Q2. Which of the following is a pair of roads that can be the same colour?

NIS	Guide Do	gar's Unique Fully Solved "	NEW TESTING SYS	TEM" GUIDE 33	1
	(A)	M and N	<b>(B)</b>	N and O	
	(C)	O and P	( <b>D</b> )	P and Q	
Questi	ons 3 to 8 de	epend on the following pas	ssage		
		lege sports president wishe leet the requirements of col		rs of a sports-wing committee as specia	al
		sists of eight members four are students.	of which (K, L, M and	N) are sports teachers whereas the other	<b>:</b> r
The pro	esident can s	elect any four of the eight c	ommittee members as l	ong as the following rules are observed	:
The for	ur representa	tives must consist of exactl	y two sports teachers as	nd two students.	
		be one of the representate the must also be a representate.		cannot be the representatives. If $P$ is	a
If R is a	a representati	ive then $L$ cannot be a repre	esentative.		
Q3.	If R is a re		a representative then	the whole group can be determined	if
	(A)	K is a representative	(B)	N is a representative	
	(C)	P is a representative	(D)	S is not a representative	
Q4.	If P is a rep	presentative then which o	f the following CANN	OT be a representative?	
	(A)	M	(B)	N	
	(C)	Q .	(D)	R	
Q5.	If $L$ is a rep	presentative then which o	f the following can be	the other three representatives?	
	(A)	K, Q and S	(B)	M, N and P	
	(C)	M, P and Q	(D)	N, P and S	
Q6.	If neither representa		tative then which of	the following is a pair of teacher	*5
	(A)	$oldsymbol{\mathit{K}}$ and $oldsymbol{\mathit{L}}$	(B)	K and M	
	(C)	K and N	<b>(D)</b>	$oldsymbol{\mathit{L}}$ and $oldsymbol{\mathit{M}}$	
Q7.	If <i>L</i> , <i>N</i> and	Q are representatives the	en which of the follow	ing must also be a representative?	
	(A)	M	(B)	P	

(C) R

S **(D)** 

Q8. If K and N are representatives then which of the following is not a representative?

> (A) Q

**(B)** R

(C) P (D) None

Two statements, labeled (1) and (2), follow each of the following given questions. The statements contain certain information. In the question you do not actually have to compute an answer, rather than you have to decide whether the information given in the statements (1) and (2) is sufficient to find a correct answer by using basic mathematics and everyday fact?

- **Q9**. What day of the week is today?
  - 1. Today is December 25.
  - 2. Amjad left Pakistan on Monday.
    - Statement 1. ALONE is sufficient but 2. ALONE is not sufficient to answer this question.
- Statement 2. ALONE is sufficient but **(B)** 1. ALONE is not sufficient to answer this question.

**(D)** 

**(B)** 

**(D)** 

- (C) Statements 1 and 2. TOGETHER are sufficient to answer the question but NEITHER of them is sufficient
- Statements 1 and 2. COMBINED are not sufficient to answer the question and additional information is needed to find the correct answer.
- Q10. Can any of the four rivers be more than 200 meters wide?

ALONE.

- The narrowest of the four rivers is 140 meters wide.
- Average width of the four rivers is 200 meters.
  - (A) Statement 1. ALONE is sufficient but 2. ALONE is not sufficient to answer this question.
- Statement 2. ALONE is sufficient but 1. ALONE is not sufficient to answer this question.

  Statements 1 and 2. COMBINED are
- (C) Statements 1 and 2. TOGETHER are sufficient to answer the question but NEITHER of them is sufficient ALONE.
- Statements 1 and 2. COMBINED are not sufficient to answer the question and additional information is needed to find the correct answer.
- Q11. If it is raining then there must be clouds. Are there clouds?
  - Today is Saturday. It is not raining.
  - 2. It rained Friday.
    - (A) Statement 1. ALONE is sufficient but2. ALONE is not sufficient to answer this question.
- (B) Statement 2. ALONE is sufficient but 1. ALONE is not sufficient to answer this question.
   (D) Statements 1 and 2. COMBINED are
- (C) Statements 1 and 2. TOGETHER are sufficient to answer the question but NEITHER of them is sufficient ALONE.
- D) Statements 1 and 2. COMBINED are not sufficient to answer the question and additional information is needed to find the correct answer.

# For questions 12 to 13

There are seven cages next to each other in a zoo. The following is known about the cages. Each cage has only one animal, which is either a lion or a monkey. There is a lion in each of the first and last cages. The cage in the middle has a monkey. No two adjacent cages have monkeys in them. The monkey's cage in the middle has two lion cages on either side. Each of the other monkey cages are between and next to two lion cages.

- Q12. How many cages have lions in them?
  - (A) 3

(B)

**(C)** 4

**(D)** 6

(E) 5

Q13.

- The monkey cage in the middle must have:
  - (A) . No other monkey cage to its left.
- (B) No lion cage on its right.
- (C) A lion cage to its left and to its right.
- (D) Other monkey cages next to it.
- (E) No lion cage to its left.

## For questions 14 to 16

Seven children — M, N, O, P, Q, X and Y are eligible to enter a drawing contest. From these seven, two teams must be formed, a blue team and a yellow team, each team consisting of exactly three of the children. No child can be selected for more than one team. Team selection is subject to the following restrictions: If P is on the blue team, O must be selected for the yellow team. If M is on the blue team, Q, if selected must be on the yellow team. Q cannot be on the same team as Q.

- Q14. Which of the following can be the three members of the blue team?
  - (A) M, N and O

(B) M, Q and Y

(C) N, O and Y

(**D**) O, P and Q

**(E)** P, Q and Y



- Q15. If P and M are both on the blue team, the yellow team can consist of which of the following?
  - (A) N, O and Q

(B) N, X and Y

(C) O, Q and X

(D) O, Q and Y

- $(\mathbf{E})$  Q, X and Y.
- Q16. If P is on the blue team, which of the following if selected, must also be on the blue team?
  - (A) M

(B) N

(C) Q

(D) X

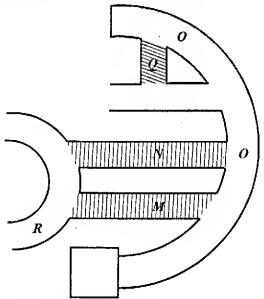
(E) Y



## Solution 1 to 2

Here, first of all we decompose the given problem in the shape of important points.

- 1. A city map representing roads, M, N, O, P, Q and R.
- 2. Link roads cannot have the same colour on the map.
- 3. Each M, N, P and Q has link to Q.
- 4. P has a link to Q.
- 5. Each of M and N has a link to R.
- Q1. (D) Since, link roads cannot have the same colour on the map. Now, according to the given condition, each, M, N, P and Q has link to O. As R has no link to O, so its colour should be same as O. Hence, the correct answer is choice D.
- Q2. (A) We draw the following estimated sketch of the roads on the map:



From above diagram, clearly roads M and N have no link each other. Hence, M and N should have the same colour. So, the correct answer is choice A.

#### Solution 3 to 8:

The important conclusions from the given problem are given below:

- 1. Sports committee consists of eight members.
- 2. There are four (K, L, M and N) sports teachers and four (P, Q, R and S) students in the committee.
- 3. President can select any four of the eight committee members.
- 4. The four representatives must consist of exactly two sports teachers and two students.
- 5. Either K or L must be one of the representatives but K and L both cannot be representatives.

- 6. If P is representative, then M must also be a representative.
- 7. If R is a representative then L cannot be a representative.
- Q3. (D) Take choice "A", which says, K is a representative. We analyze the given statement, according to this statement, if R is representative, but M is not representative. If K is representative, then R combine K. Since M is not representative, so according to above point 6; P will also not representative. This situation is given in the following table " $\checkmark$ " indicates the representation and " $\times$ " represents "not representation".

<b>✓</b>	×	×	
K	L	M	N
×		<b>✓</b>	
P	Q	R	S

From above table, we find two groups, *i.e.*, KNRQ, KNRS. Thus we cannot find a single group. So, choice "A" is not correct choice. Now, if we accept choice "B", then the possible outcomes are given in the following table.

	×	×	✓
K	L	M	N
×		<b>4</b>	
P	-Q	R	S

It is elear from above table, that if we accept choice "B" then whole group cannot be determined. Now, take choice, "C", according to this choice, the following table formed.

	х	х	
K	L	M	N
✓		✓	
P	Q·	R	S

It cannot be acceptable, because if P is accepted then M will also be accepted. But in the given statement M is not representative.

Lastly, we prepare the table according to the choice "D"

	Ψ		
	×	×	
K	L	М	N
×		<b>✓</b>	×
P	Q	R	S

Thus a whole group KNQR can be determined. Hence, the correct answer is choice D.

- Q4. (B) If P is representative then M must also be representative. Thus, choice "A" is not acceptable. The correct choice is choice "B".
- Q5. (C) If "L" is a representative, then choice "A" is not acceptable, because K and L both cannot be representative. Choice B is also not acceptable, because there will three teachers (L, M, N) be joined in one group. The choice C is acceptable.
- Q6. (B) If neither Q nor S is a representative, then choice "A" cannot be accepted, because K and L both cannot be representative. The choice "B" is acceptable. Hence the correct answer is choice B.
- Q7. (D) If K, N and Q are representative, then choice "A" is not true choice, because if M join with K, N and Q, then the teacher representatives become three, but the four representative must consist of two teachers. Now, take choice, B, if we accept this choice then the group of representative is K, N, P, Q. But, according to the given condition, if P is representative then M must also be a representative. Here, P is without M, so this choice is also rejected. Now, if we accept choice "C" then the group of representative is K, N, Q, R, which is also not acceptable. If we accept choice "D", then the group of

NTS Guide

representative becomes K, N, Q, S, which is a acceptable representative group. Hence, the correct answer is choice D.

- Q8. (C) If K and N are representative, then, clearly, choice "A", which is "Q" is not acceptable. The second choice R is also not acceptable, because if R is a representative, then L cannot be a representative. Here R is with K not with L. So R may be form a representative group. Hence this choice is also not acceptable. The choice "C" is acceptable, because if P is representative then M must also be a representative. Then the group becomes KNMP. This group is not a representative because in this group there are three teachers (K, N and M) which is not according to the given condition. Hence, the correct answer is choice C.
- Q9. (D) Since, there is not any link between two statements and statements (1) and (2) COMBINED are not sufficient to answer the question and additional information is needed to find the correct answer. The correct answer is choice D.
- Q10.(C) Since, according to statement (1), the narrowest of the four rivers is 140 meters and according to the statement (2), average width of the four rivers is 200 meters. We are asked, can any of four rivers be more than 200 meters. Let we suppose the width of the rivers;  $R_1 = 200$ ,  $R_2 = 200$ ,  $R_3 = 200$ ,  $R_4 = 140$  meter.

Average = 
$$\frac{200 + 200 + 200 + 140}{4}$$
 = 185

But according to second statement, the average of four rivers is 200. It is only possible if any one or more rivers have their width more than 200. Hence, statements, (1) and (2) TOGETHER are sufficient to answer the question but NEITHER of them is sufficient ALONE.

Q11.(D) Since, Statements 1 and 2. COMBINED are not sufficient to answer the question and additional information is needed to find the correct answer.

#### Solution 12-13

We write the important points from the given problem briefly:

- 1. There are seven eages next to each other in the zoo.
- 2. Each cage has only one animal.
- 3. The animal is either a lion or a monkey.
- 4. There is a lion in the first and last cage.
- No two adjacent cages have monkeys in them.
- 6. The monkey's cage in the middle has two lion cages on either side.
- 7. Each of the other monkey eages are between and next to two lion cages. From above points we sketch the following diagram.

Lion	Monkey	Lion	Monkey	Lion	Monkey	Lion
1st cage					-	Last cage

- Q12.(C) From above diagram, clearly there are four lion cages.
- Q13.(C) From above fig., we find two cages of lion to left and right of Monkey's cage.

#### Solution 14 to 16

Important points deduction from the given problem are given below:

- 1. Seven children M, N, O, P, Q, X and Y are eligible to enter a drawing context.
- From these seven children, two teams must be formed
   A blue team, a yellow team and each team consisting of exactly three of the children.
- 3. No child can be selected for more than one team.
- 4. If Pris on the blue team, O must be selected for the yellow team.
- 5. If M is on the blue team, Q, if selected must be on the yellow team.



- 6. Q cannot be on the same team as X
- 7. N cannot be on the same team as O.
- Q14.(E) Take choice "A" that is M, N and O. This choice is not acceptable because N cannot be on the same team as O. Take choice "B", that is, M, Q and Y. This choice is also not acceptable, because M and Q could not be in the same team. Take choice "C", that is N, O and Y. Since N and O cannot be in the same team, so choice "C" also not acceptable. Take choice "D", that is, O, P and Y. Since P and O cannot be on the same team, so choice, D, also not acceptable. The correct choice is E, since it meets all the requirements given in the problem.
- Q15.(D) Here, we draw the following table, according to the given condition.

Blue team	Yellow team
P	0 <
M	Q
X	Y
N	

If P, M, X and N are in blue team, then O and Q must be in yellow team, Y can be either on blue and yellow team, so the yellow team may be O, Q and Y. Hence, the correct answer is choice D.

Q16.(B) By the given restrictions, if P is on the blue team, O must be selected for the yellow team. Similarly, if M is on the blue team, Q must be on the yellow team. The most important point to solve this problem is that, Q eannot be on the same team as X and N cannot be on the same team as O. Now, if P is on blue team O must be on yellow team, so N cannot be on the yellow team. Hence, the correct answer is choice B.

# III. Verbal Section

(C)

Enervation: Retaliated By

No. of Questions = 25

Select the correct answer for each question and blacken the corresponding circle in the answer shect.

Instructions (1-10): In this part of test, you have 10 MCQs about English. Each sentence below has one or two blanks, each blank shows that something has been omitted. Choose the correct answer from the four answer choices given with each question, numbered (A), (B), (C), (D).

grven	i wini cacii que	short, numbered $(M)$ , $(D)$ , $(C)$ , $(D)$	<i>?</i> ·		
1.	Normally a	ın individual thunderstorm	about 45 minutes	5.	
	(A)	Lasts	<b>(B)</b>	Ends	
	(C)	Remains	(D)	Continues	
2.	The	arguments put forth for not d	isclosing the facts dia	l not impress anybody.	
	(A)	Specious	(B)	Intemperate	
	(C)	Spurious	<b>(D)</b>	Convincing	
3.	Modern ar	chitecture has discarded the	trimming on bu	ildings and emphasises simplicity of	life.
	(A)	Flamboyant	(B)	Flabbergasting	
	(C)	Gaudy	(D)	Gaunt	
4.	I decided to	o sell a piece of land when I was	offered a more	price.	
	(A)	True	(B)	Realistic	
	(C)	Exact	(D)	Correct	
5.	Because of	f moon's, it has little or n	io substance.		
	(A)	Weak	(B)	Dull	
	(C)	Frail	(D)	Unsubstantial	
6.		of spending more than he earned ore affluent day.	l left him in a state of	f perpetual but he hop	oing
	(A)	Indigence: Persevered in			
	(B)	Confusion: Compromised By			

	<b>(D)</b>	Motion: Responded		
7.	Come and	d stond me my un	nbrello or vou will g	vet avite wet.
	(A)	With: Under	(B)	By: Beneath
	(C)	Beside: Under	( <b>D</b> )	Near: Below
8.	Hydrogen	balloons, which were much		
	(A)	Smaller; Cheap		Lighter; Popular
	( <b>C</b> )	Cheaper; Fashionable		Brighter; Common
9.	Surprising	zly enough, it is more difficult to		thon obout the ond strange.
	( <b>A</b> )	Specific, Foreign	(B)	
	( <b>C</b> )	Commonplace, Exotic	(D)	
10.		_		e philonthropist deserved for his
	·			
	(A)	Recognition: Folly	<b>(B)</b>	Blame: Hypocrisy
	(C)	Reward: Modesty	(D)	Credit: Altruism
letter	Instructions (	11-20): Each question below co	nsists of a related p	pair of words or phrases, followed by four
terrere	eu pairs or w	vords of phrases numbered (A)	(R) $(C)$ $(D)$ Char	ose the lettered pair that best expresses a
11.	VESSEL:	to that expressed in the pair gives	n in the question.	
	(A)	Wolf: Pack	(D)	5 . 6
	(A) (C)	Vehicle: Truck	(B)	Forest: Clearning
12,	BUSTLE:		(D)	Carriage: Horse
1 441				_
	(A)	Hum: Sing	(B)	Lope: Run
13.	(C)	Glide: Dance	<b>(D)</b>	Chatter: Talk
10.		ENT: JUSTIFICATION::		
	(A)	Kindness: Obedience	(B)	Authority: Sanction
14.	(C)	Usage: Submission	(D)	Tradition: Novelty
l 44,	NOTE: SC			
	(A)	Conductor: Orchestra	(B)	Singer: Music
46	(C)	Musician: Instrument	<b>(D)</b>	Letter: Alphabet
15.		G: LEARNING::		
	(A)	Running: Jumping	(B)	Investigating: Discovery
40	(C)	Reading: Writing	<b>(D)</b>	Dancing: Swimming
16.	HELMET:			
	. (A)	Pendant: Neck	(B)	Breastplate: Chest
47	(C)	Pedal: Foot	<b>(D)</b>	Knapsack: Back
17.		REGIMENT		
	(A)	Colonel: Martinet	(B)	Dancer: Balletomane
4.6	(C)	Singer: Chorus	<b>(D)</b>	Trooper: Rifle
18.		I: PHOTOGRAPH::		·
	( <b>A</b> )	Finger: Fabric	<b>(B)</b>	Hang: Painting
	(C)	Compose: Melody	<b>(D)</b>	Refine: Style
19.	YAWN: BO			
	(A)	Dream: Sleep	(B)	Anger: Madness
	(C)	Smile: Amusement	<b>(D</b> )	Face: Expression
ነጠ	BALLAD: S	SONG:		
20.				
20.	(A)	Melody: Rhythm	(B)	Novel: Chapter

# Read the following passages carefully and answer the questions given at its end-

Suppression of people's feelings in any form not only provokes mental reaction but also amounts to asking for trouble. It is always hazardous to deny self-expression either to the born rebel or to the cool and satirical critic, for the former will go the whole hog in denouncing the policy of repression while the latter may reserve his right to support the government and may even turn ironical in his approach.

A tolerant government will see to it that it enlists the backing of all sections including the extremists and humorists. England has won a number of friends following the policy of tolerance by granting asylum to staunch opponents of their respective governments. Even from practical point of view, it is safe to allow people to voinit their venom against the government rather than deny their self-expression and incite them to go for pernicious activities.

Even if a government happens to be despotic, it will do well to provide and facilitate opportunities at self-expression. It will be well advised to avoid wasting money on security arrangements and go in for utilizing stipulated sum for facilitating the openings for expression. Hence no government, despotic or otherwise, should persecute people for holding political views contrary to their own.

# 21. It can be inferred that the author favours:

(A) Suppression

(B) Despotism

(C) Criticism

(D) Self-expression

01

Q5

Q6.

Q7.

Q8.

09.

011

# 22. According to the passage:

- (A) Supporting government is good
- (B) Denouncing government is good
- (C) Even despotic governments should allow self-expression
- (D) Denying self-expression is good

#### 23. The passage indicates that:

- (A) The government should allow people to go against it
- (B) England has developed tolerance towards the opponents of the government
- (C) Self-expression incites people towards destructive works
- (D) All governments should restrict free expression

#### 24. Security arrangements to suppress self-expression are:

(A) Preferable

(B) Advisable

(C) Not advisable

(D) None of the above

### 25. Which of the following is incorrect?

- (A) It is dangerous to deny self-expression
- (B) A tolerant government wins over extremists and humorists
- (C) It is safe to allow self-expression
- (D) Government should persecute people for holding political view against it

#### **ANSWERS**

1.	(A)	2.	(A)	3.	(C)	4.	(B)	5.	(A)
6.	(A)	7.	(C)	8.	(B)	9.	(C)	10.	(D)
11.	(A)	12.	(D)	13.	(B)	14.	(D)	15.	(B)
16.	(B)	17.	(C)	19.	(D)	19.	(C)	20.	(C)
21.	(D)	22.	(C)	23.	(B)	24.	(C)	25.	(D)

\*\*\*\*\*



# GRE - GAT TEST 4

	Qu	antitative Section		No. of Questions = 20
Q1.	The sum reciprocal	of a number and its reciprocal. The number is:		the difference of the number and its
		$\pm\sqrt{2}$	<b>(B)</b>	$\pm \frac{1}{\sqrt{2}}$
	(C)	$\pm \frac{1}{\sqrt{3}}$	(D)	$\pm \frac{1}{\sqrt{2}}$ $\pm \sqrt{3}$
Q2.	When the hy 23, the	integer $k$ is divided by 17, the quiquotient is $q$ and the remainder is	otient is p ar	nd the remainder is 5. When $k$ is divided of the following is true?
	(A)	23p + 17q = 19	(B)	
		17p - 23q = 9	, ,	5p - 14q = 6
Q3.		ne area of a circle whose radius is		
	(A)	8π	(B)	18π
	( <b>C</b> )	$3\pi$	(D)	9π
Q4.	The circum			of the circle is $y\pi$ square units. If $x = y$ ,
	(A)	1	<b>(B</b> )	2
	(C)	3π	(D)	$2\pi$
Q5.	A cylindric inches. Sin (A)	cal sillo (container for storing gr ice one gallon equals 231 cubic inc 4 gallons	thes, the capa	liameter of 14 inches and a height of 6 acity of the sillo is approximately: $1\frac{1}{2} \text{ gallons}$
	, ,	$2\frac{2}{7}$ gallons	(D)	$1\frac{1}{7}$ gallons $2\frac{1}{2}$ gallons
Q6.	What is the	e volume of a cube whose surface		_
	(A)	125	(B)	216
	(C)	294	(D)	343
Q7.	The ratio o		room was 2 :	: 3. If hoys represented five more than
	(A)	15	(B)	23
	(C)	21	(D)	27
Q8.		e average of $5^{30}$ , $5^{60}$ , $5^{17}$ , $5^{13}$ and $5^{90}$	?	
i.	(A)	5 <sup>210</sup>	(B)	5 <sup>209</sup>
	` ,	$5^{29} + 5^{59} + 5^{16} + 5^{12} + 5^{89}$	(D)	5 <sup>205</sup>
Q9.	If $p+1 < 3p$	9 + 5, then:		
		p < -2	<b>(B)</b>	p > −2.
å.		p=0	<b>(D)</b>	p > 2
Q10	Which of th	ne following numbers cannot be re	epresented b	
1	(A)	23 7	(B)	13 3
		•		•

(A) 3:4°

**(B)** 4:3

(C) 1:2

**(D)** 1:3

Q12. If  $\frac{1}{x} + \frac{1}{x} + \frac{1}{x} = 12$ , then x =

(A)  $\frac{3}{4}$ 

(B)  $\frac{1}{4}$ 

(C)  $\frac{1}{3}$ 

**(D)**  $\frac{1}{12}$ 

Q13. If a + 2b = x and a - 2b = y, which of the following expression is equal to ab?

 $(A) \quad \frac{x+y}{2}$ 

(B)  $\frac{x-y}{2}$ 

(C)  $\frac{x^2 + y^2}{4}$ 

(D)  $\frac{x^2 - y^2}{8}$ 

Q14. If the sum of the two integers is 42 and their difference is 22. Then the greater of the two integers is:

(A) 25

(B) 32

(C) 8

**(D)** 10

Q15. Each of Nazir's buckets has a capacity of 11 gallons, while each of Osama's buckets can hold 8 gallons. How much more water in gallons can 7 of Nazir's buckets held compared to 7 of Osama's buckets?

(A) 7 gallons

(B) 9 gallons

(C) 21 gallons

(D) 24 gallons

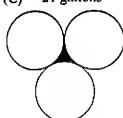
C

C

C

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Q16.



In the above figure, three equal circles of radius 3 cm each touch each other, then the area of the shaded portion is:

(A)  $\frac{3}{2}(\sqrt{3} - \pi) \text{ cm}^2$ 

(B)  $\frac{9}{2}(2\sqrt{3} + \pi) \text{ cm}^2$ 

(C)  $\frac{9}{2}(2\sqrt{3}-\pi) \text{ cm}^2$ 

(D)  $\frac{\sqrt{3}}{2}(2-\pi) \text{ cm}^2$ 

Q17. If two circles touch each other externally at C and AB is a common tangent to the eireles. Then  $\angle$ ACB is:

(A) greater than 120°

(B) greater than 90°

(C) less than 90°

(D) equal to 90°

Q18. A train running between two towns arrives at its destination 10 minutes late when it goes 40 miles per hour and 16 minutes late when it goes 30 miles per hour. The distance between two towns is:

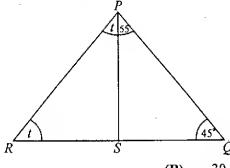
(A) 12

**(B)** 720

(C)  $8\frac{1}{2}$ 

**(D)**  $12\frac{1}{7}$ 

Q19. What is the value of t in the following figure?



- (A) 45
- **(C)** 40

- **(B)** 30
- **(D)** 55
- Q20. Two trains 132 meters and 108 meters in length are running towards each other on parallel lines, one at the rate of 32 km per hour and another at 40 km per hour. In what time will they be clear off each other from the moment they meet?
  - (A) 20 sec

(B) 15 scc

(C) 12 sec

(D) 29 sec

# Explanatory Answers

Q1. (A) Let the number be x. Then, its reciprocal is  $\frac{1}{x}$ . According to the given condition,

$$x + \frac{1}{x} = 3\left(x - \frac{1}{x}\right)$$

$$\Rightarrow \frac{x^2 + 1}{x} = 3\left(\frac{x^2 - 1}{x}\right)$$

$$\Rightarrow x^2 + 1 = 3x^2 - 3 \Rightarrow 3x^2 - x^2 = 1 + 3$$

$$\Rightarrow 2x^2 = 4$$

$$\Rightarrow x^2 = 2$$

$$\Rightarrow x = \pm \sqrt{2}$$

Hence the correct answer is choice A.

Q2. (C) According to the first condition, k = 17p + 5

According to the second condition k = 23q + 14

$$\Rightarrow$$
 17p + 5 = 23q + 14

$$\Rightarrow$$
  $17p - 23q = 9$ 

Hence the correct answer is choice C.

Q3. (B) Since the area of the square is 9, therefore, each side is 3. Thus the length of the diagonal is  $3\sqrt{2}$ . Now the area of the circle whose radius is  $3\sqrt{2}$  is

Area = 
$$\pi r^2$$
  $\Rightarrow$  Area =  $\pi (3\sqrt{2})^2$   
 $\Rightarrow$  Area =  $\pi [9(2)]$   
 $\Rightarrow$  Area =  $18\pi$ 

Thus, the best answer is choice B.

Q4. (B) It is given:

en

Circumference:  $C = \kappa \pi$  and

$$A = y\pi$$

$$\therefore x = y \Rightarrow C = A \Rightarrow 2\pi r = \pi r^2$$

Hence, the correct answer is choice B.

Q5. (A) Volume of the cylinder =  $\pi r^2 h$ 

Here, 
$$r = \frac{1}{2}$$
 diameter  $= \frac{1}{2}(14) = 7$  inches

$$h = 6 \text{ inches}$$

$$V = \pi(7)^2(6)$$

$$=\pi(49)(6)$$

$$= 294 \times \frac{22}{7} = 924 \text{ cubic inches}$$

231 cubic inches = 1 gallon

1 cubic inch 
$$=\frac{1}{231}$$
 gallon

924 cubic inches 
$$=\frac{1}{231} \times 924$$
 gallons

Hence the correct answer is choice A.

Q6. (D) Let e be the each face of the cube, then

$$e^2 + e^2 + e^2 + e^2 + e^2 + e^2 = 6e^2 = 294$$

$$\Rightarrow e^2 = \frac{294}{6} = 49$$

$$\Rightarrow e = 7$$

So each edges are all 7.

Hence the volume is  $e^3 = 7^3 = 343$ 

The correct answer is choice D.

Q7. (A) Let x be the total number of boys in the class and b, be the total boys in the class, then by the given condition

$$\frac{2}{5} \times x = b \dots (i)$$

$$\frac{1}{3}x = b - 5$$

$$\Rightarrow \frac{1}{3}x + 5 = b \dots (ii)$$

Substituting the value of b from (ii) in (i), we have

$$\frac{2}{3}x = \frac{1}{3}x + 5$$

$$\Rightarrow \frac{2}{3}x = \frac{x+15}{3} \Rightarrow 2x = x+15$$

$$\Rightarrow$$
  $x = 15$ 

$$x = 15$$
The correct answer is choice A.

Q8. (C) 
$$\frac{5^{30} + 5^{60} + 5^{17} + 5^{13} + 5^{90}}{5}$$

$$=\frac{5^{30}}{5}+\frac{5^{60}}{5}+\frac{5^{17}}{5}+\frac{5^{13}}{5}+\frac{5^{90}}{5}$$

$$=5^{29}+5^{59}+5^{16}+5^{12}+5^{89}$$

Q9.

Q10

QII

Q12

Q1.

Hence the correct answer is choice C.

Q9. (B) 
$$p+1$$
  $<3p+5$   
 $\Rightarrow p+1-p$   $<3p+5-p$   
 $\Rightarrow 1$   $<2p+5$   
 $\Rightarrow 1-5$   $<2p+5-5$   
 $\Rightarrow -4$   $<2p$   
 $\Rightarrow \frac{-4}{2}$   $<\frac{2p}{2}$   
 $\Rightarrow -2$   $< p$   
 $\Rightarrow p > -2$ 

Hence, the correct answer is choice B.

- Q10.(D) The square root of any prime number cannot be represented by a repeating decimal. Hence the correct answer is choice D.
- Q11.(B) Let s be the side of equilateral triangle and t be the side of the square, then

Perimeter of triangle = s + s + s = 3s

Perimeter of square = t + t + t + t = 4t

Since the perimeter of the square and the triangle is equal, in other words 3s = 4t

the two sides must be equal only if s = 4 and t = 3, hence the ratio between the sides of the equilateral triangle and a square is 4:3

Hence the correct answer is choice B.

Q12.(B) 
$$\frac{1}{x} + \frac{1}{x} + \frac{1}{x} = 12$$

$$\frac{1+1+1}{x} = \frac{12}{1}$$

$$\Rightarrow \frac{3}{x} = \frac{12}{1} \Rightarrow 12x = 3$$

$$\Rightarrow x = \frac{3}{12}$$

$$\Rightarrow x = \frac{1}{4}$$

Hence, the best answer is choice B.

Q13.(D) 
$$a+2b = x$$
 ...(i)  
 $a-2b = y$  ...(ii)  
 $2a = x+y$  (Adding (i) and (ii))  
 $\Rightarrow a = \frac{x+y}{2}$  ...(iii)

Now, subtracting (ii), from (i), we get

$$4b = x - y$$

$$\Rightarrow b = \frac{x - y}{4} \dots (iv)$$

Now, multiplying (iii) and (iv), we get

$$ab = \left(\frac{x+x}{2}\right)\left(\frac{x-y}{4}\right)$$

$$\Rightarrow ab = \frac{x^2 - y^2}{8}$$

Hence the correct answer is choice D.

Q14.(B) Let the two integers be x and y, then

$$x + y = 42$$
 ...(i)

$$x - y = 22$$
 ...(ii)

Adding (i) and (ii), we get

$$2x = 64$$

$$\Rightarrow$$
  $x = 32$ 

Subtracting (ii) from (i), we get

$$2y = 20$$

$$\Rightarrow v = 10$$

Clearly, the greater integer is x having value 32. Hence, the correct answer is choice B.

Q15.(C) Capacity of Nazir's bucket = 11 gallons

7 bucket of Nazir will contain water  $= 11 \times 7 = 77$  gallons

Capacity of Osama = 8 gallons

7 buckets of Osama will contain water =  $8 \times 7 = 56$  gallons

The difference = 77 - 56 = 21 gallons

Hence the correct answer is choice C.

Q16.(C) Let A, B and C be the centres of the three circles, respectively. The ABC is an equilateral triangle with each side equal to 6 cm

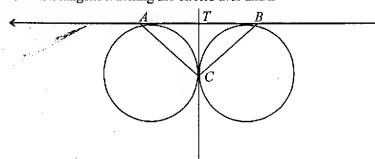
Required area = Area of  $\triangle ABC - 3 \times$  area of sector of a circle with r = 3 and  $\theta = 60^{\circ}$ 

$$= \left[ \frac{\sqrt{3}}{4} \times 36 - 3 \times \pi \times 3^2 \times \frac{60}{360} \right]$$

$$= \left[ 9\sqrt{3} - \frac{9\pi}{2} \right] = \frac{9}{2}(2\sqrt{3} - \pi) \text{cm}^2$$

The correct answer is choice C.

Q17.(D) Let AB be a common tangent touching the circles at A and B



Let CT be the common tangent at C, meeting AB at T

Then, tangents to a circle from a point outside it being equal, we have

$$TA = TC \& TB = TC$$

$$\therefore$$
 ZTAC = ZTCA and ZTBC = ZTCF

So, 
$$\angle ACB = \angle TCA + \angle TCB$$

$$= \angle TAC + \angle TBC$$

$$\Rightarrow$$
 2 $\angle$ ACB =  $\angle$ TAC +  $\angle$ TBC +  $\angle$ ACB = 180°

$$\Rightarrow \angle ACB = 90^{\circ}$$

NTS Guide

Hence the correct answer is choice D.

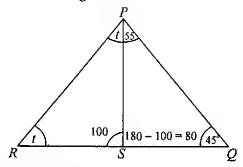
Q18.(A) Let the required distance be x km with two speeds, the difference of time taken is (16 - 10) 6 minutes

Using the formula

Distance = 
$$\frac{\text{Product of two speeds}}{\text{Difference of two speeds}} \times \text{Difference between time arrival}$$
  
=  $\frac{30 \times 40}{40 - 30} \times \frac{6}{60} = 12 \text{ km}$ 

Hence the correct answer is choice A.

Q19.(C) We simplify the figure in the following manner:



: The sum of the angles of a triangle = 180

$$\therefore t + t + 100 = 180 \qquad \Rightarrow 2t + 100 = 180$$
$$\Rightarrow 2t = 80 \qquad \Rightarrow \qquad \boxed{t = 40}$$

Q20. Relative speed of the trains = (32 + 40)km/hour

= 72 km/h  
= 
$$\left(72 \times \frac{5}{18}\right)$$
 m/sec  
= 20 m/sec

Time taken by the trains in passing each other

$$= \left[ \frac{\text{Sum of lengths}}{\text{Relative speed}} \right]$$
$$= \left( \frac{240}{20} \right) \sec = 12 \sec$$

Hence the correct answer is choice C.

# II. Analytical Section

No. of Questions = 20

#### For questions 1 to 4

A carrier must deliver mail by making a stop at each of six buildings: S, T, U, V, W and X. Mail to be delivered are of two types, ordinary mail and priority mail. The delivery of both types of mail is subject to the following conditions: Regardless of the type of mail to be delivered, mail to W and mail to W must be delivered before mail to W and mail to W must be delivered before mail to W is delivered. Mail to buildings receiving some priority mail must be delivered, as far as the above conditions permit, before mail to buildings receiving only ordinary mail.

Q1. If S is the only huilding receiving priority mail, which of the following lists the buildings in an order, from first through sixth, in which they can receive their mail?

(A) 
$$T_i$$
 S, W, X, V, U

(B) 
$$T, S, X, W, U, V$$

**(E)** 

June

346		NTS Guide GRE	- GAT Genera	al Tests With Explanatory Answers
		S, T, W, U, X, V	<b>(D)</b>	S, W, T, X, V, U
	` ,	V, S, T, W, X, U		
Q2.	order, from	m first through sixth, in which tl	mail, which of hey can receive	f the following lists the buildings in an email?
		S, T, W, X, V, U	(B)	T, S, V, W, X, U
	, ,	T, S, X, W, U, V	(D)	U, T, X, W, S, V
	` '	X, T, U, W, S, V		
Q3,	priority ma	uence of buildings to which mail ail, which of the following is a co priority mail?	l is delivered is implete and acc	s V, W, T, S, X, U and if X is receiving curate list of buildings that must also be
		V, T	(B)	v, w
	, ,	W, T	• •	W, U
	` ,	V, W, T, S	. ,	
Q4.	If only one the order of day?	building is to receive priority not buildings, which of the follow	nail, and as a re ving must be th	esult, V can be no earlier than fourth in he building receiving priority mail that
	(A)	S	(B)	T
	(C)	U .	<b>(D</b> )	W
	<b>(E)</b>	X		
Oues	tions 5–9			
of Co Hami	ollege has aske d and Noman	ed each of the college six profes	ssors in the department of the	Department will be on Sabbath. The Dean partment — Akhter, Bilal, Chohan, Fraz, esc months. The physicists can decide the established by the dean.
		erve as chairman in February.		
		rve as chairman before Hamid does	es.	
		will serve as chairman in consecut		
Q5.		he following professors could se		n in January?
	(A)	Bilal	(B)	Chohan
	(C)	Fraz	(D)	Hamid
	(E)	Noman	$(\mathbf{D}_f)$	нани
O6 <sup>.</sup>			* ** Namon	Chairman'in Many
				has to serve as Chairman in May?
	(A)	1	(B)	3
	(C)	6	<b>(D)</b>	4
	(E)	2		
Q7.		serves in April, all of the followin	ng could be true	e except:
	(A)	Akhter serves in January	( <b>B</b> )	Hamid serves in March
	(C)	Bilal serves in May	(D)	Bilal serves in June
	<b>(E)</b>	Hamid serves in June		
Q8.		ves in May, what is the latest mo	onth in which A	khter could serve?
	(A) `	March	(B)	April
	(C)	January	(D)	February

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Q9.	Which of the following CANNOT be true?

- (A) Akhter and Noman serve in consecutive months
- (B) Noman and Hamid serve in consecutive months
- (C) Hamid and Fraz serve in consecutive months
- (D) Akhter and Chohan scree in consecutive months
- (E) Bilal and Chohan serve in consecutive months

### Questions 10-14

をあるとうできます。 かんしゅうしゃ かんしゅうしゃ かんかん かんしゅうしゃ かんしゅうしゅうしゅう

During practice matches, before a major tournament, in a football ground, one team can practice at a time. There are seven teams — the Argentine, the Brazil, the Senegal, the Dubai, the England, the France and the Germany. The football ground is open seven evenings a week from Monday to Sunday (Sunday being considered the last day of the week), and the allocation of the practice times is governed by the following rules:

- (i) On any evening, only one team can play.
- (ii) The Argentine must practice on Monday.
- (iii) The Dubai practice exactly one day before the France practice.
- (iv) The France practice exactly one day before the Germany practice.
- (v) The Senegal and the Brazil must practice earlier in the week than the England.
- Q10. The latest day in the week that the Brazil can practice is:
  - (A) Tuesday

(B) Wednesday

(C) Thursday

(D) Friday

**(B)** 

- (E) Saturday
- Q11. If a person went to the football ground on three consecutive evenings, her or she could see which of the following teams in the order listed?
  - (A) the France, the Germany, the Senegal
- the France, the Germany, the Dubai
- (C) the Argentine, the Dubai, the Senegal
- (D) the Brazil, the Senegal, the France
- (E) the Dubai, the England, the France
- Q12. On week, the Senegal practiced on Wednesday and the Dubai practiced the next day. That week, the Brazil must have practiced on:
  - (A) Monday

(B) Tuesday

(C) Friday

(D) Saturday

- (E) Sunday
- If the Germany practice on Thursday, the England and the Dubai must practice on which days, respectively?
  - (A) Sunday and Tuesday

- (B) Saturday and Tuesday
- (C) Friday and Wednesday
- (D) Wednesday and Thursday
- (E) Tuesday and Monday
- Q14. If the France practice on Saturday, the England must practice on what day?
  - (A) Tuesday

(B) Wednesday

(C) Thursday

(D) Friday

(E) Sunday

#### Questions 15 to 17

O13.

At a meeting of the Ruling Party, the seven top party leaders, who are all cabinet ministers, are seated on a platform in order of rank the Prime Minister being in the center. The closer a person is to the Prime Minister; the higher is his/her rank. Moreover, a person sitting on the right of the Prime Minister outranks the one sitting equidistant on the left of the Prime Minister. The seven leaders are L, M, N, O, P, Q and R.

Q is four places left to the Minister of Agriculture, who is two places to the right of N.

M's neighbours are L and the Minister of Agriculture R is two places to the left of O.

The Minister of Education, Mining and Culture are seated together, in order, from left to right.

The remaining Ministers are these of Social Welfare and Defence.

- Q15. The fifth ranking person in the party hierarchy is:
  - (A) R, the Minister of Mining
- (B) Q, the Minister of Culture

(C) O, the Prime Minister

(D) P, the Minister of Defence

Ųτ

O

Q

- Q16. How many of the seven party leaders outrank the Minister of Education?
  - (A) 2

**(B)** 3

(C) 4

**(D)** 5

- **(E)** 6
- Q17. The lowest ranking Minister is:
  - (A) Minister of Education
- (B) Minister of Social Welfare

(C) Minister of Mining

(D) Minister of Defense

(E) Minister of Culture



#### Solution 1-4

Here, we illustrate the given problem into important points:

- 1. A courier must deliver mail by making a stop at each of the six buildings: S, T, U, V, W and X.
- 2. There are two types of mail: Ordinary mail and priority mail.
- 3. Mail to W and mail to X must be delivered before mail to U be delivered.
- 4. Mail to T and mail to S must be delivered before mail to X is delivered.
- Q1. (D) If S is the only building receiving priority, mail. Then building S will be the first on priority. Since, mail to W and mail to X must be delivered before mail to U is delivered. Then the first four mails in the list are SWXU. Now, according to the point 4 mail T and mail S must be delivered before mail X, so the above list becomes after this condition SWTXVU, which is the correct list.
- Q2. (C) Since mail to T and mail to S must be delivered before mail to X, but in this problem T has a priority, so the same elements of the list are T, S, X according to point (3) and given priority the list becomes, T, S, X, W, U, V. Hence the correct answer is choice C.
- Q3. (B) Clearly V and W is the receiving priority mail. Hence, the correct answer is choice "B".
- Q4. (E) If V can be no earlier than fourth in the order, then the receiving priority must be X. Because in the list T, S, X, W, U, and V, V replaces with X. Hence, the correct answer is choice E.

#### Solution 5-9

Let A, B, C, F, H and N represents professors Akhter, Bilal, Chohan, Fraz, Hamid and Noman, respectively. Then, from the given problem, we find the following important points:

- 1 Chohan will serve as chairman in February.
- 2. Akhter will serve as chairman before Hamid does. That is A < H.
- 3. Bilal and Fraz will serve as chairman in consecutive months. That is

B << F and F << B

Q5. (E) Since, Chohan will serve as chairman in February, so Bilal and Fraz could not serve because Bilal and Fraz will serve as chairman in consecutive months. Because, Akhter will serve as chairman before Hamid, now. Hamid could not serve as chairman in February. So Akhter will not serve in January. So, only person Noman is there, which does not violate any of the conditions. Hence, the correct answer is the choice E.

# Dogar's Unique Fully Solved "NEW TESTING SYSTEM" GUIDE

NTS Guide

Q6. (E) If Chohan serve as chairman in February, and Noman serves in May, then the possible schedule is given by:

January	February	March	April	May	June
Akhter	Chohan	Bílal	Fraz	Noman	Hamid
Akhter	Chohan	Fraz	Bilal	Noman	Hamid

Hence the correct answer is choice E.

Q7. (E) If Noman serves in April, then the possible schedule is given as:

January	February	March	April	May	June
Akhter	Chohan	Hamid	Noman	Bilal	Fraz
Akhter	Chohan	Hamid	Noman	Fraz	Bilal

From above schedule, it is possible that Akhter can serve as chairman in January, so choice A is not correct choice. It is also clear from above table that Hamid can serve in March, so choice B is also not correct choice. Choice, C and D not correct choices, because Bilal can serve as chiarman both in May and June as shown in the above table. Hence, C and D are also not correct choices. Only, choice "E" is not possible. Hence the correct answer is choice E.

Q8. (A) If Bilal serve in May, then the possible schedule for Akhter is given as:

January	February	March	April	May	June
January	Chohan	Hamid	Fraz	Bilal	Fraz
Noman	Chohan	Akhter	Hamid	Bilal	Fraz

From above table it is clear that Akhter can serve in January and March. In which, March is the latest month. Hence, the correct choice is choice A.

Q9. (A) The only professors that can serve in January are Akhter and Noman, so one of them must serve in January, and neither in February. So, Akhter and Noman cannot serve as chairman in consecutive months. Hence, the choice A cannot be true. Hence, the correct answer is choice A.

Q10.(B) From the given rules, one of the schedules is given as under:

•	tom the Street area, one of the sentences to Street								
	Monday	Tuesday	Wednesday	Thursday	Friday	Saturday	Sunday		
	Argentine	Senegal	Brazil	Dubai	France	Germany	England		

Hence, the correct answer is choice B.

Q11.(A) From the following schedule given in the table, we find that the correct answer is choice A.

Monday	Tuesday	Wednesday	Thursday	Friday	Saturday	Sunday
Argentine	Brazil	Dubai	France	Germany	Senegal	England

Q12.(B) If Senegal practiced on Wednesday and the Dubai practiced the next day, the new schedule is given below:

Monday	Tuesday	Wednesday	Thursday	Friday	Saturday	Sunday
Argentine	Brazil	Senegal	Dubai	France	Germany	England

So the Brazil will practice on Tuesday. Hence the correct answer is choice B.

O13.(A) If the Germany practice on Tuesday, then the new schedulc may be as:

ı		<b>*</b> 1					- •
ļ	Monday	Tuesday	Wednesday	Thursday	Friday	Saturday	Sunday
	Argentine	Dubai	France	Germany	Brazil	Senegal	England

From above table, we find that England and Dubai will practice on Sunday and Tuesday respectively. Hence, the correct answer is choice A.

Q14.(C) If the France practice on Saturday, then the new schedule is given by:

-		process or			Ł			
	Monday	Tuesday	Wednesday	Thursday	Friday	Saturday	Sunday	
-	Argentine	Brazil	Senegal	England	Dubai	France	Germany	



From above schedule, under the given rules, if France practice on Saturday, then England must practice on Thursday. Hence the correct answer is choice C.

#### Solution 15 to 17

From the given problem, we sorted out the following points:

- 1. The seven party leaders are, L, M, N, O, P, Q and R.
- 2. Prime Minister is in the center.
- 3. The closer a person to the Prime Minister; the higher is his/her rank.
- 4. A person sitting on the right of the Prime Minister outranks the one sitting equidistant on the left of the Prime Minister.
- 5. Q is four places to the left of the Minister of Agriculture, who is two places to the right of N.
- 6. M's neighbours are L and the Minister of Agriculture.
- 7. R is two places to the left of O.
- 8. The minister of Education, Mining and Culture are seated together, in order from left to right.
- 9. The remaining Ministers are those of Social Welfare and Defense.

From above points we draw a following sketch:

Culture	Mining	Education	P.M	Minister of Agriculture	Social Welfare	Defense
Q	R	N	0	P	М	L
4	5	. 6		1	2	3

- Q15.(A) From above table, clearly, the fifth rank of the party person is R, who is the Minister of Mining. Hence, correct answer is choice A.
- Q16 (E) Including P.M. there are six party leaders outrank the Minister of Education. It is clear from the table.
- Q17.(A) From table, it is clear that Minister of Education has the lowest rank. Hence, the correct answer is choice A.

\*\*\*\*\*\*

III. Verbal Section No. of Questions = 25

Select the correct answer for each question and blacken the corresponding

circle in the answer sheet.

Instructions (1-10): In this part of test, you have 10 MCQs about English. Each sentence below has one or two blanks, each blank shows that something has been omitted. Choose the correct answer from the four answer choices given with each question, numbered (A), (B), (C), (D).

			microscope;	but we	know that they are there because we can
5		they cause.			
		Cheap; Damage		(B)	Elementary; Harm
	(C)	Simple; Danger		(D)	Ordinary; Havoc
7		s coming after me as high a	s a great hili an	d	as a enemy.
	(A)		<del>-</del>	(B)	Dreadful; Advancing
	(C)			<b>(D)</b>	Angry; Attacking
A			_, the film itse	f is inte	elligent, well-acted, handsomely produced
	and altogeti				
	(A)	Tasteless; Respectable		(B)	Extensive; Moderate
	(C)	Sophisticated; Moderate		(D)	Risqué; Crude
1		character to th	e extremities of	the arcti	ic region.
		An unflappable; Sustain		<b>(B)</b>	A dictatorial; Brook
	(C)	A Spartan; Negotiate		(D)	An inimitable; Resist
	As a jaurna		erroneous convi	ctions, (	Griffin Nicholson was opposed to the court
	*** ** ** *** *** ***				

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A duty is an obligation. It is something we owe to others as social beings when we live together. We must let others live with us. May right of living implies my duty to my fellowmen to allow them the same conditions of life. Infact, rights and duties are co-related. What is a right in regard to one is a duty in regard to others. Rights and duties are two sides of the same coin. We should always observe from the stand point of others. Thus they are duties. Moral duty is more effective than the legal. A moral duty is that which is upon the people on moral grounds.

It is my moral duty to help the poor because of being a member of the society.

I must try to create these conditions which contribute to the welfare of humanity. Similarly, I owe a duty to my parents—to be obedient and respectful to them. This duty originates from the sense of responsibility which is directly related with our conscience. So this maxim is concerned with a moral duty which a man should owe without the legal bondage.

Sense of duty is paramount for the proper development of civilization in the 20th century. Hypocrisy and diplomacy are quite reverse to the sense of duty. Hypocrisy involves wickedness duty involves sincerity and faithfulness.

- 21. Rights and duties according to the passage are:
  - (A) Co-related
  - (B) Two sides of the same coin
  - (C) Neither of the above
  - (D) Both (A) and (B)
- 22. According to the author, the moral duty is:
  - (A) Enjoined upon animals
  - (B) Helping the rich
  - (C) More effective than the legal duty
  - (D) Secondary to the legal duty
- 23. Where does the duty originate from?
  - (A) From responsibility but not from conscience
  - (B) From responsibility which is related with conscience
  - (C) From legal bondage
  - (D) From hypocrisy and diplomacy
- 24. Point out the incorrect statement.
  - (A) Hypocrisy and diplomacy do not support the sense of duty
  - (B) Hypocrisy involves wickedness
  - (C) Duty involves sincerity
  - (D) Sense of duty is not important for the development of civilization
- 25. The author:
  - (A). Has sense of responsibility
  - (B) Doesn't have sense of duty
  - (C) Both (A) and (B)
  - (D) Neither (A) nor (B)

# **ANSWERS**

1.	<b>(D)</b>	2.	(A)	3.	(A)	4	(C)	5.	(C)
6.	(C)	7.	(A)	8.	(A)	<b>S.</b>	(B)	19.	(A)
11.	(B)	12.	(A)	14.	(C)	14.	<b>(D)</b>	15.	(A)
16.	(B)	17.	(B)	18.	<b>(D)</b>	19.	(D)	20.	(B)
21.	(D)	22.	(C)	23.	(B)	24.	(D)	25.	(A)

Q(

Q7

Q8

\*\*\*\*\*\*



Q1.

Q2.

Q3.

Q4.

Q5.

Q6.

Q7.

Q8.

one pound approx): (A)

**(C)** 

1.125 pounds

1.3 pounds

_			*	NTS	TES'	TNO.	1			
<b>•</b>	Selec		correct ng circle	answer in the ans	for wer sl	each neet.	question	and	blacken	the
he	e area (	of the cir	cle that is	inscribed i	n a squ	are of a	rea 4, is:			i
	(A)	$\frac{\pi}{2}$				(B	. ,			
		_				(L)	θ π			
	(C)	$\frac{\pi}{3}$				<b>(D</b>	) 4π .			
f tl	he ang	les of a fi	ve-sided p	olygon are	in the	ratio of	2:3:4:4	l : 5, wh	at is the m	easure (
me	inest a.	ngie:								
•	(A)	30°				(B	•			
	(C)	45°	11			(D				
st	at this	rate give	ganons of en that the	gasoline ar re are z ca:	e need rs in th	cd per n ie town?	nonth for e	ach car.	How long v	will y ga
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	()	zr				(B)	$\frac{1}{x}$		•	
	(C)	$\frac{z}{x\nu}$				(D)	$\frac{y}{z}$	-		
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	(C)	_1_					1			
		20160				· (D)	200			
et '	T = tot	ial area o	of five circ	lcs of radi	us r an	d let S =	= total arca	of thre	e circles of	radius
<b>.</b>	S, then	$\frac{r}{u}$ =								
		T5								
	(A)	$\sqrt{\frac{3}{3}}$				(B)	$\frac{3}{5}$	•		
		$\sqrt{3}$					-			
	(C)	$\sqrt{\frac{1}{5}}$				(D)	3π			
su	m of R	s. 7000 i	s divided :	amon <i>g A. I</i>	3 and 6	Cin sucl	h a wav the	ıt shara	$\mathbf{s}$ of $A$ and $A$	R ana in
tio	2:3 a	nd those	of $B$ and	Care in the	ratio	4 : 5. Th	n a way ina ne amount i	reeeived	by C is:	o are in
٠	(A)	Rs. 390	)			(B)			•	
	<b>(C)</b>	Rs. 280				(D)				
r :	y=2:	5, then (	3x+4y):	(4x + 5y) =						
	(A)	6:20	•			(B)	9:21			
	(C)	26:33				(D)	16:20			

additional ounce, what is the weight of a package for which the charges are \$1.66? (16 ounces =

**(B)** 

**(D)** 

1.1 pounds

0.8 pounds

I. 
$$(36-81)=(6-9)(6+9)$$

II. 
$$5(16+7) = 5(16) + 5(7)$$

III. 
$$5 \div (10-1) = (5 \div 10) - (5 \div 1)$$

(A) I only

(B) II only

(C) I and II only

(D) II and III only

Q1

Q1

Q1'

Q18

Q19

Q20.

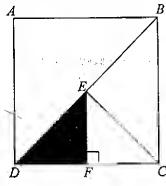
Q1. (

- Q10. Two candidates contested an election. One got 65% of the votes and won by 300 votes. The total number of votes polled is:
  - (A) 1200

**(B)** 1000

(C) 800

- **(D)** 600
- Q11. In square ABCD below, if DE = EB and DF = FC, then, what is the fraction of the area of the shaded region to the area of square region ABCD?



(A)  $\frac{1}{3}$ 

(B)  $\frac{1}{8}$ 

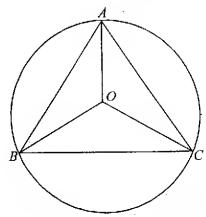
(C)  $\frac{1}{16}$ 

- **(D)**  $\frac{1}{6}$
- Q12. In a certain pizza, two straight cuts of different radii succeed in removing  $\frac{4}{15}$  of the total pizza. What is the central angle in degrees of the piece cut?
  - (A) 85

**(B)** 92

(C) 96

- **(D)** 60
- Q13. In the figure below, O is the centre of the circle. If  $\angle OBC = 25^{\circ}$ , then  $\angle BAC$  is equal to:



(A)  $150^{\circ}$ 

(**B**) 65°

(C)  $30^{\circ}$ 

**(D)**  $25^{\circ}$ 

If  $x : y \text{ is } 7 : 6 \text{ and } 3y : 2z \text{ is } 2 : 3, \text{ what is } \frac{z}{x}$ ?

**(B)** 

(C)

**(D)** 

Fatima is having a party, at 7:00 P.M., guests begin arriving at a uniform rate of 8 people every 15 minutes. If this pattern continues, how many guests will have arrived at 9:00 P.M.?

(A)

(B) 64

**(C)** 40

**(D)** 20

For positive integers x and y, if  $x^2 + 2y^2 = 41$ , and  $2x^2 + y^2 = 34$ , then  $x^2 =$ Q16.

(A)

**(B)** 

(C)

(D) 20

The value of  $\left[ \frac{(0.05)^2 + (0.41)^2 + (0.073)^2}{(0.005)^2 + (0.041)^2 + (0.0073)^2} \right]$  is: Q17.

(A)

**(B)** 10

**(C)** 100

**(D)** 1000

Aslam sells a chair at a gain of  $7\frac{1}{2}\%$ . If he had bought it at a  $12\frac{1}{2}$ Q18. % less and sold it for Rs. 5 more, he would have gained 30%. The cost price of the chair is:

(A) Rs. 72

**(B)** Rs. 80

Rs. 88 (C)

**(D)** Rs. 96

For developing pictures, Modern Photo Lab., charges a service fee of \$6 for every order it 019. receives in addition to a printing fee. If the order consists of 12 pictures or less, the printing fee per picture is \$0.24. If the order consists of more than 12 pictures, the printing fee per picture is \$0.16. What is the total cost per picture for an order consisting of 30 pictures.

(A) \$0.44

\$0.16 **(B)** 

(C) \$4.8

(D) \$0.36

Q20. If the interior angle of a regular polygon is 11 times its exterior angle, the number of sides of the

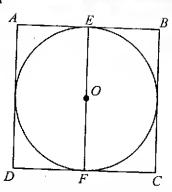
> (A) 11

**(B)** 18

**(C)** 24

(D) 22

Q1. (B) First of all, we draw a diagram



01

**Q**11

Q12

Since the arca of square ABCD is 4

$$\therefore$$
 AD = 2. Also, diameter EF = 2 and

radius OE = OF = 
$$\frac{2}{2}$$
 = 1

Area of the circle = 
$$\pi r^2 = \pi (1)^2 = \pi$$

Hence the correct answer is choice B.

Q2. (B) The sum of the angles of a five-sided polygon is 
$$(5-2) \times 180 = 3 \times 180 = 540$$
.

Now, 
$$540 = 2x + 3x + 4x + 4x + 5x \implies 18x = 540$$

$$\Rightarrow x = 30$$

The measure of the smallest angle is 
$$= 2 \times 30 = 60^{\circ}$$

Hence the correct answer is choice B.

Q3. (D) Each car needed gasoline = 
$$x$$
 gallons z cars needed gasoline =  $zx$  gallons

y gallons required at this rate = 
$$\frac{y}{zx}$$

Hence the correct answer is choice D.

Q4. (D) There are 24 hours in a day, and 
$$24 \times 14$$

= 336 hours in two weeks, also 
$$336 \times 60$$

= 20,160 minutes in two weeks. Thus the fraction with 36 minutes is 
$$\frac{36}{20,160} = \frac{1}{560}$$
.

Hence the correct answer is choice D.

# Q5. (C) Since T is the total area of the 5 circles,

therefore, 
$$T = 5(\pi t^2)$$

Now, S is the total area of the 3 circles of radius u, therefore  $S = 3(\pi u^2)$ 

$$T = S \text{ (given)}$$

$$5\pi r^2 = 3\pi u^2$$

$$\Rightarrow \frac{r^2}{u^2} \qquad = \frac{3\pi}{5\pi} \Rightarrow \frac{r^2}{u^2} = \frac{3}{5}$$

$$\Rightarrow \frac{r}{u} = \sqrt{\frac{3}{5}} = \frac{\sqrt{3}}{\sqrt{5}}$$

Hence the correct answer is choice C.

**Q6.** (B) 
$$A : B = 2 : 3$$
 and  $B : C = 4 : 5$ 

$$= \frac{3}{4} \times 4 : \frac{3}{4} \times 5 = 3 : \frac{15}{4}$$

$$\therefore$$
 A: B: C = 2:3:  $\frac{15}{4}$  = 8:12:15

:. C's share = Rs. 
$$\left[ 7000 \times \frac{15}{35} \right]$$
 = Rs. 3000

Hence the correct answer is choice B.

Q7. (C) Given that 
$$\frac{x}{y} = \frac{2}{5}$$

Now, 
$$\frac{3x + 4y}{4x + 5y} = \frac{3\left(\frac{x}{y}\right) + 4}{4\left(\frac{x}{y}\right) + 5}$$
$$= \frac{3 \times \frac{2}{5} + 4}{4 \times \frac{2}{5} + 5} = \frac{\frac{6}{5} + 4}{\frac{8}{5} + 5}$$
$$= \frac{\frac{6 + 20}{5}}{\frac{8 + 25}{5}} = \frac{26}{33}$$

Hence, (3x + 4y) : (4x + 5y) = 26 : 33

Thus, correct answer is choice C.

Q8. (A) Since charges on first five ounces = 62 cents. Now, 1.66 dollars = 100 + 66 = 166 cents. Thus, first 62 cents are charged for five ounces, then by remaining cents will be 166 - 62 = 104. Since 8 cents are received for additional ounce. Therefore, 104 is received for  $\frac{104}{8} = 13$  ounces. The total package is

$$13 + 5 = 18$$
 ounces.

1 ounces 
$$=\frac{1}{16}$$
 pound

18 ounces = 
$$\frac{1}{16} \times 18$$
 pounds

= 1.125 pounds

Hence the correct answer is choice "A".

Q9. (C) Take I, (36-81) = (6-9)(6+9) is true because  $[(6)^2 - (9)^2] = (6-9)(6+9)$ , as  $a^2 - b^2 = (a+b)(a-b)$ 

Take II, 5(16 + 7) = 5(16) + 5(7) is also true, because according to distributive property of multiplication over addition

$$x(a+b) = xa + xb$$

Now, take III,  $5 \div (10 - 1) = (5 \div 10) - (1 \div 5)$  is not a true statement. Hence the correct answer is choice C.

Q10.(B) Let the total number of votes polled be x.

Then 65% of x - 35% of x = 300

$$\Rightarrow$$
 30% of  $x = 300$ 

$$\therefore \frac{30}{100} \times x = 300 \text{ or } x = \frac{300 \times 100}{30} = 1000$$

Helice the correct answer is choice B.

Q11.(B)  $\therefore$  DE = EB and DF = FC, the area of the shaded region is one-fourth the area of triangular region BCD, since BD divides square ABCD into two equal triangular regions, the shaded region is  $(\frac{1}{2})(\frac{1}{4})$ ,

or  $\frac{1}{8}$ , of the area of square region ABCD. Hence, the best answer is B.

Q12.(C) Let x be the total prize and let y be the required angle then setting the proportion, we have

$$x:360::\frac{4}{15}x:y$$

$$\frac{x}{360} = \frac{4x}{15} \qquad \Rightarrow xy = \frac{4x}{15} \times 360$$
$$\Rightarrow y = 4 \times 24 = 96^{\circ}$$

Hence the correct answer is choice C.

Q13.(B) OB = OC 
$$\Rightarrow$$
  $\angle$ OCB =  $\angle$ OBC = 25°  
So,  $\angle$ BOC = [180 - (25 + 25)] = 130°  
 $\therefore$   $\angle$ BAC =  $\frac{1}{2}\angle$ BOC  
= 65°

Hence the correct answer is choice B.

Q14.(B) 
$$x: y = 7: 6$$
  $\Rightarrow \frac{x}{y} = \frac{7}{6} \dots (i)$   
also  $3y: 2z = 2: 3 \Rightarrow \frac{3y}{2z} = \frac{2}{3}$   
 $\Rightarrow \frac{y}{z} = \frac{4}{9} \dots (ii)$   
 $\Rightarrow \frac{z}{v} = \frac{9}{4} \dots (iii)$ 

dividing equation (iii) by (i), we get

$$\frac{\frac{z}{y}}{\frac{x}{y}} = \frac{\frac{9}{4}}{\frac{7}{6}}$$

$$\Rightarrow \frac{z}{y} \times \frac{y}{x} = \frac{9}{4} \times \frac{6}{7}$$

$$\Rightarrow \boxed{\frac{z}{x} = \frac{27}{14}}$$

Hence the correct answer is choice B.

Q15.(B) Guests will arrive according to the following schedule:

	=	·
7:15		8
7:30		8
7:45		8
8:00		8
8:15		8
8:30		8
8:45		. 8
9:00		8
Total gues	ts	64

Hence the correct answer is choice B.

Q16.(B) 
$$x^2 + 2y^2 = 41$$
 ...(i)  
 $2x^2 + y^2 = 34$  ...(ii)

Subtracting equation (i) from (ii), we get

$$2x^2 + y^2 = 34$$



$$\frac{x^2 + 2y^2 = 41}{x^2 - y^2 = -7} \dots (iii)$$

adding (ii) and (iii), we get

$$2x^2 + y^2 = 34$$

$$x^2 - y^2 = -7$$

$$3x^2 = 27$$

$$x^2 = \frac{27}{3}$$

$$\Rightarrow x^2 = 9$$

Hence the correct answer is choice B.

Q17.(C) Given that, Let a = .05, b = 0.41 and c = .073

$$= \frac{a^2 + b^2 + c^2}{\left(\frac{a}{10}\right)^2 + \left(\frac{b}{10}\right)^2 + \left(\frac{c}{10}\right)^2}$$
$$= \frac{100(a^2 + b^2 + c^2)}{(a^2 + b^2 + c^2)} = 100$$

-Hence the correct answer is choice C.

Q18.(B) Let C.P = Rs. 100. Then, first S.P = Rs. 107.50

New C.P = Rs. 87.50 and gain on it = 30%

 $\therefore$  Second S.P = 130% of 87.50 = 113.75

Difference in two selling prices = Rs. (113.75 - 107.50)

$$=$$
 Rs. 6.23

$$\therefore \text{ Actual S.P} = \text{Rs.} \left[ \frac{100}{6.25} \times 5 \right]$$

Hence the correct answer is choice B.

Q19.(D) Service fee = \$6

Charges of 30 pictures @, \$0.16 per picture =  $30 \times 0.16 = 4.8$ 

Total charges = (6 + 4.8) = 10.8

Cost per picture =  $\frac{10.8}{30}$  = \$0.36

Hence the correct answer is choice D.

 $=\frac{360}{n}$ , and Q20.(C) Each exterior angle

> $= \left[ 180 - \frac{360}{n} \right]$ Each interior angle

$$\therefore 180 - \frac{360}{n} = 11 \times \frac{360}{n}$$

$$\Rightarrow \frac{180n - 360}{n} = \frac{11 \times 360}{n}$$

$$\Rightarrow 180n - 360 = 3960$$

$$\Rightarrow 180n = 3960 + 380 \Rightarrow n = \frac{4340}{180}$$

$$\Rightarrow$$
  $n=2$ 

# NTS TEST NO. 2

- ◆ Select the correct answer for each question and blacken the corresponding circle in the answer sheet.
- Q1. The sum of the lengths of all the edges of a cube is 4 centimeters. What is the volume in cubic centimeters of the cube?
  - $(\mathbf{A}) = \frac{1}{8}$

 $(\mathbf{B}) \qquad \frac{1}{27}$ 

(C) 64

- **(D)** 27
- Q2. A 6-foot long cylindrical pipe has an inner diameter of 8 feet and outer diameter of 10 feet. If the total surface area (including inside, outside and ends) is  $x\pi$ , what is the value of x?
  - (A) 20

**(B)** 118

(C) 100

- (D) 109
- Q3. November is the busiest month at Panorama centre, Lahore, where sale in November is 40 percent higher than the average. If sale in March is typically 20 percent lower than the average, what is the ratio of the March sale to November sale?
  - (A) 2:3

**(B)** 2:1

(C) 3:2

- **(D)** 4:7
- Q4. How many 3-digit numbers are there that consist of only odd digits?
  - (A) 125

(B) 625

(C) 12500

- **(D)** 225
- Q5. If (x+y): (x-y)=1:5, then  $(x^2-y^2): (x^2+y^2)$  equals:
  - (A) 2:3

(B) 1:2

(C) 5:13

- (D) 1:10
- Q6. What annual payment will discharge a debt of Rs. 580 due in 5 years, the rate being 8% per annum?
  - (A) Rs. 120

(B) Rs. 100

(C) Rs. 65.60

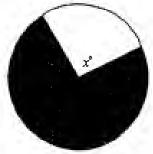
39

- (D) Rs. 166.40
- Q7. Amina found an easy way to add up a sequence of positive even integers with an even number of terms. She forms pairs of equal sums hy adding the first integer to the last, the second integer to the next-to-last, and so on. She then computed the total by adding these equal sums. If the total that Amina obtained was 930, how many terms were there in the sequence of positive even integers if the sequence started with the number 2?
  - (A)

(B) 24

(C) 30

- (D) 25
- Q8. In the following figure, the area of the shaded sector is 75% of the area of the entire circle, what is the value of x?



(A) 25

(B) 90°

(C) 270 °

**(D)** 45



子子の大大ないますべた いるからをころうに 事業

Q9. Ali goes to a park and runs in the following manner:

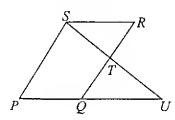
From the starting point, he goes west 25 m, then to north 60 m, then to east 80 m and finally to south 12 m. The distance between the starting point and the finishing point is:

(A) 73 m

**B)** 83 m

(C) 103 m

- **(D)** 177 m
- Q10. PQRS is a parallelogram and T is the midpoint of QR. ST and PQ when produced meet at U. Then



**(A)**  $PU = \frac{3}{2}PQ$ 

(B) PU = 2PQ

(C) PU = 3PQ

- **(D)**  $PU^2 = 2PQ^2$
- Q11. The diameter of a circle is 105 cms less than the circumference. The radius of the circle is:
  - (A) 24.5 cm

(B) 24 cm

(C) 23 cm

- (D) 22 cm
- Q12. The perimeter of a square whose area is equal to that of a circle with perimeter  $2\pi x$  is:
  - (A)  $4\sqrt{\pi} x$

(B)  $4\sqrt{\pi x}$ 

(C)  $\sqrt{\pi} x$ 

- (D)  $2\pi x$
- Q13. A can do a piece of work in 35 days while B can complete it in 45 days. They start the work together, but A drops out after 7 days. In how many days will B take to finish the remaining work?
  - (A) 29

(B) 36

(C) 45

- (D) None of these
- Q14. If  $\frac{3}{5}$  of the employees in Dogar Publishers are not college graduates, what is the ratio of the number of college graduates to those who are not college graduates?
  - (A) 1:3

(B) 3:2

(C) 1:5

- **(D)** 2:5
- Q15. If  $\frac{3a-1}{25} = \frac{a+5}{11}$ , what is the value of a?
  - (A) 13

(B) 136

(C)  $\frac{5}{4}$ 

- **(D)** 17
- Q16. The sum of the six consecutive integers is T, what is the largest of those integers in terms of T?
  - $(A) \quad \frac{T+10}{5}$

(B)  $\frac{T+6}{5}$ 

(C)  $\frac{T+5}{6}$ 

- (D)  $\frac{T+15}{6}$
- Q17. If  $\frac{1}{2}y$  years ago, Rizwan was 10, and  $\frac{1}{2}y$  years from now he will be 2y years old, how old will he be 3y years from now?
  - (A) 54

(B) 60

(C) 34

- If xyz = 1, then  $\left(\frac{1}{1 + x + y^{-1}} + \frac{1}{1 + y + z^{-1}} + \frac{1}{1 + z + x^{-1}}\right)$  is equal to: Q18.
  - (A)

(C) ху

- **(D)**
- A man spends 75% of his income. His income is increased by 20% and he increased his Q19. expenditure by 10%. His savings are increased by:
  - (A) 10%

**(B)** 25%

(C) 37.5%

- **(D)** 50%
- Electricity tax is increased by 20% and its consumption is decreased by 20%. The change in the Q20. expenditure is:
  - (A) nil

**(B)** 5% decrease Q

Q

Q7

**(C)** 4% increase

(D) 4% decrease



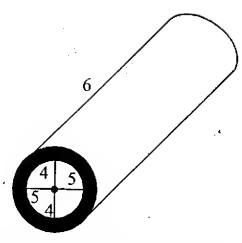
Q1. (B) Since a cube has 12 edges, therefore

$$12e = 4 \implies e = \frac{1}{3}$$

As 
$$v = e^3 \Rightarrow v = \left(\frac{1}{3}\right)^3$$

$$\Rightarrow v = \frac{1}{27}$$

Q2. (B)



According to above diagram, surface area of the cylinder is,  $A = 2\pi rh$ . Thus the area of the outer edge is =  $2\pi(5)(6) = 60\pi$ , and the surface area of the inner side =  $2\pi(4)(5) = 40\pi$ . Now

Area of the shaded end = Area of the outer circle - the area of the inner circle

$$= \pi r^2 - \pi r^2 = \pi (5)^2 - \pi (4)^2$$

$$=25\pi-16\pi=9\pi$$

Now the total surface area  $= 60\pi + 40\pi + 9\pi + 9\pi$ 

$$= 118\pi = x\pi$$

$$\Rightarrow x = 118$$



Hence the correct answer is choice B.

- Q3. (D) Let the average sale be 100, then sale in November = 100 + 40 = 140 and the sale in March = 100 20 = 80. Then ratio between the sale of March to November is  $80 : 140 \Rightarrow 4 : 7$
- Q4. (A) At unit place, there could be only 5 odd digits, i.e., 1, 3, 5, 7 and 9.

Also, at tenth place there could be only 5 odd numbers and at last, at 100th place, there could be 5 odd integers. Then by-product rule

$$5 \times 5 \times 5 = 125$$

Hence the correct answer is choice A.

**Q5.** (C) 
$$\frac{x+y}{x-y} = \frac{1}{5} \Leftrightarrow \frac{x+y+x-y}{x+y-x+y} = \frac{1+5}{1-5}$$

(By Commend & Divendo)

$$\Rightarrow \frac{x}{y} = \frac{6}{-4} \qquad \Rightarrow \frac{x}{y} = \frac{-3}{2}$$

$$\Rightarrow \frac{x^2}{y^2} = \frac{9}{4} \Rightarrow \frac{x^2 - y^2}{x^2 + y^2} = \frac{9 - 4}{9 + 4}$$

$$\Rightarrow \frac{x^2 - y^2}{x^2 + y^2} = \frac{5}{17}$$

Hence the correct answer is choice C.

Q6. (B) Let the annual payment be Rs. x. Then (Amount of x for 4 years) + (Amount of x for 3 years) + (Amount of x for 2 years) + (Amount of x for 1 year) + x = 580

$$\Rightarrow \left(x + \frac{x \times 4 \times 8}{100}\right) + \left(x + \frac{x \times 3 \times 8}{100}\right) + \left(x + \frac{x \times 2 \times 8}{100}\right) + \left(x + \frac{x \times 1 \times 8}{100}\right) + x = 580$$

$$\Rightarrow 5x + \frac{32x + 24x + 16x + 8x}{100} = 580$$

$$\Rightarrow \frac{500x + 80x}{100} = 580$$

$$\Rightarrow \frac{580x}{100} = 580$$

$$\Rightarrow x = 100$$

Hence the correct answer is choice B.

Q7. (C) The sequence of the even numbers are in the form of

Using the formula for sum of integers

$$Sn = \frac{n}{2} \{ 2a + (n-1)d \}$$

Here n = ?, Sn = 930, d = 4 - 2 = 2

and a = 2 *i.e.*, first term. Now

$$930 = \frac{n}{2} \{2 \times 2 + (n-1)2\}$$

$$\Rightarrow 930 \times 2 = n\{4 + 2n - 2\}$$

$$\Rightarrow 1860 = 2n^2 + 2n$$

$$\Rightarrow \qquad \qquad 930 = n^2 + n$$

$$\Rightarrow n^2 + n - 930 = 0$$

$$\Rightarrow$$
  $n^2 + 31n - 30n - 930 = 0$  (Factorizing)

$$\Rightarrow n(n+31)-30(n+31) = 0$$

$$\Rightarrow (n-30)(n+31) = 0$$

$$\Rightarrow$$
  $n = 30 \text{ or } -31$ 

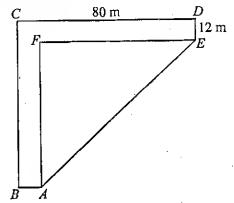
Since n is always positive so the correct answer is choice C.

Q8. (B) Since the shaded area of the given circle is 75% of the entire circle, thus the white area is 25% (100 -75) of the circle. Now x is the 25% of 360°.

$$\Rightarrow x = 360 \times \frac{25}{100} = 90^{\circ}$$

Hence, the correct answer is choice B.

Q9. (A) Here, we draw the following diagram:



AE = 
$$\sqrt{\text{FE}^2 + \text{AF}^2}$$
  
=  $\sqrt{(80 - 25)^2 + (60 - 12)^2}$   
=  $\sqrt{(55)^2 + (48)^2}$   
= 73m

Hence the correct answer is choice A.

Q10.(B) In  $\Delta$ TRS and  $\Delta$ TUQ, we have

$$\angle SRT \cong \angle TQU$$
 ('.' alternative angles)

and 
$$\angle STR \cong \angle UTQ$$
 (vertical opposite angles)

and 
$$TR = QT$$

$$\therefore$$
  $\triangle TRS \cong TUQ$ , so  $SR = QU$ 

$$\therefore PU = PQ + QU$$

$$= PQ + SR$$

$$\Rightarrow$$
 PU = 2PQ (: in | | gram PQ = RS)

Hence the correct answer is choice B.

Q11.(A) Here,

$$2\pi r - 2r = 105$$

$$\Rightarrow 2r(\pi - 1) = 105$$



$$\Rightarrow r = 105 \times \frac{7}{15} \times \frac{1}{2}$$
$$= 24.5 \text{ cm}$$

Hence the correct choice is choice A.

Q12.(A) Since, given area =  $2\pi x$ 

But, the area of a circle =  $2\pi r$ 

 $\Rightarrow$  radius, r =  $2\pi$ 

 $\therefore$  Area of square = Area of circle =  $\pi x^2$ 

 $\therefore \text{ Perimeter} = 4 \times \text{side}$   $= 4\sqrt{\pi x^2}$   $= 4x\sqrt{\pi}$ 

Hence, the correct answer is choice A.

Q13.(A) (A + B)'s 7 days work = 
$$7 \times \left(\frac{1}{35} + \frac{1}{45}\right)$$
  
=  $\frac{16}{45}$ 

Remaining work =  $1 - \frac{16}{45} = \frac{29}{45}$ 

B will finish  $\frac{29}{45}$  of the work in  $\frac{29}{45} \times 45$  days *i.e.*, in 29 days.

Q14.(B) Since for every 5 employees, three are not college graduates, and (5-3) = 2 are college graduates. So the ratio of the graduates to non-graduates is 2:3.

Hence the correct answer is choice B.

Q15.(D) 
$$\frac{3a-1}{25} = \frac{a+5}{11}$$

$$11(3a-1) = 25(a+5)$$

$$33a-11 = 25a+125$$

$$33a-25a = 125+11$$

$$\Rightarrow 8a = 136$$

$$\Rightarrow 8a = 136$$

$$\Rightarrow a = 17$$

Q16.(D) Let the six consecutive integers be n, n+1, n+2, n+3, n+4, n+5. Then

T = n + (n + 1) + (n + 2) + (n + 3) + (n + 4) + (n + 5)

 $T = 6n + 15 \implies 6n = T - 15$ 

$$\Rightarrow n = \frac{T - 15}{6}$$

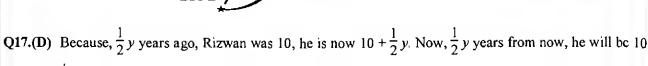
Since n is the smallest of the integers, the largest is

$$n+5 = \frac{T-15}{6} + 5$$

$$= \frac{T-15+30}{6}$$

$$\Rightarrow n+5 = \frac{T+15}{6}$$

Hence the correct answer is choice D.



 $\frac{1}{2}y + \frac{1}{2}y = 10 + y$ . But given that at that time he will be 2y years old. Thus,  $10 + x = 2x \Rightarrow x = 5$ Thus he is now, 10 + 5 = 15, and 3y or 15 years from now he will be 15 + 15 = 30 years. Hence the correct answer is choice D.

Q18.(D) Given that, 
$$\frac{y}{y + xy + 1} + \frac{1}{1 + y + xy} + \frac{xy}{xy + 1 + y}$$
 ( :  $z = \frac{1}{xy}$ )
$$= \left(\frac{y + 1 + xy}{y + 1 + xy}\right) = 1$$

Hence the correct answer is choice D.

New income = 120, new expenditure = 110% of 75

$$= 82.5$$

New saving 
$$= (120 - 82.5) = 37.5$$

Increase in saving = 
$$\left(\frac{12.5}{25} \times 100\right)\%$$

=50%

Original Expenditure = Rs.  $(100 \times 100)$  = Rs. 10000

New Tax = Rs. 120 per unit and New consumption = 80 units

$$\therefore$$
 New expenditure = Rs.  $(120 \times 80)$  = Rs. 9600

∴ Decrease in expenditure 
$$= \left(\frac{400}{10000} \times 100\right)\%$$
  
= 4%

# NTS TEST NO. 3

#### błacken the Select the correct answer for each question and corresponding circle in the answer sheet.

Instructions (1-10): In this part of test, you have 10 MCQs about English. Each sentence below has one or two blanks, each blank shows that something has been omitted. Choose the correct answer from the four answer choices given with each question, numbered (A), (B), (C), (D)

1.	He laboured	the hill; sat watching the	the hill.			
	(A)	Along, Towards	(B)	Down; Up		
	(C)	Up; Down	(D)	Towards; From		
2.	Put the milk	the table and cover it	a cloth.			
	(A)	On; With	(B)	Near; By		
	(C)	On; By	(D)	In, With		
3.	Consumers refused to buy meat products from the company because of rumors th					
-	the meat processing plant was; the rumors, however, were quite,					

- at the water supply at with no hard evidence to back them up.
  - Un-inspected, reckless
  - **(B)** Contaminated, unsubstantiated
  - (C) Impure, damaging
  - **(D)** Misdirected, scandalous
- 4. Consumption of red meat has \_\_\_\_\_ because its fat content has become a worrisome and \_ matter.
  - Abated, Dubious (A)

Skyrocketed, Stressful

_	(C)	Abounded, Divisive	<b>(D)</b>	Declined, Controver	sial
5.	Florence 1	Nightingale was in the a		odern medicine.	Such practices a
	sanitizatio	n of hospital wards and isolation	of actively infected	l patients.	_ onen praenees u
	(A)	A collaborator, Rejecting		•	
	(B)	A maverick, Protesting			
	(C)	, .			
	<b>(D)</b>				
ô.	Sofia		s other interests.		
	(A)	Used to	(B)	Was used to	
	(C)		<b>(D)</b>	Using to	
7.	Salman fin	iishedtwo of his publishe	d compositions be	fore his twelfth birthday	
	(A)	Written	(B)	Writing	
	(C)	To write	<b>(D)</b>	Wrote	
١.	Throughou	ut the animal kingdom, bi	gger than the elep	hant.	
	(A)	Whale is only the		Only the whale is	
	(C)	Is the whale only	( <b>D</b> )	Only whale is the	
	Linda Gree	enhouse's articles for the New Yo	, ,	•	, cansulizine
	prose into	a necessarily limited space.			, · · · P · · · · · a
	(A)	Callousness	(B)	Brevity	
	(C)	Intuition	(D)	Propriety	
0.	One of the	least effective ways of sorting info	, ,		
	(A)	Repeat	(B)	Repeating	
	(C)	To repeat	(D)	How repeat	
	• •	11-20): Each question below con-			Callaginal by Cain
etter	ed pairs of we	ords or phrases numbered (A), (A	R(C) $(C)$	ose the lettered pair tha	t haet evereeeee
elati	onship similar	or branche similario (37); (3	$\omega_{j}$ , $(\omega_{j})$ , $(\omega_{j})$ . $\omega_{110}$	and the testing has into	it best expresses a
	mittine director	to that expressed in the pair given	in the question.	•	
1.	ELM: TRE	to that expressed in the pair given	in the question.	•	
1.	ELM: TRE	to that expressed in the pair given E::	in the question.		
1.	ELM: TRE	to that expressed in the pair given E:: Whale: Mammal	in the question. (B)	Cart: Horse	
1.	ELM: TRE (A) (C)	to that expressed in the pair given  E::  Whale: Mammal  Cloud: Rain	in the question.		
1.	ELM: TRE (A) (C) GULLIBLE	to that expressed in the pair given  E::  Whale: Mammal  Cloud: Rain  E: DUPED::	in the question. (B) (D)	Cart: Horse Painting: Artist	
1.	ELM: TRE (A) (C) GULLIBLE (A)	to that expressed in the pair given  E::  Whale: Mammal  Cloud: Rain  E: DUPED::  Myopic: Misled	in the question.  (B) (D)  (B)	Cart: Horse Painting: Artist Careful: Cautioned	
1. 2.	ELM: TRE (A) (C) GULLIBLE (A) (C)	to that expressed in the pair given  E::  Whale: Mammal  Cloud: Rain  E: DUPED::  Myopic: Misled  Malleable: Molded	in the question. (B) (D)	Cart: Horse Painting: Artist	
1. 2.	ELM: TRE (A) (C) GULLIBLE (A) (C) IMPLICATE	to that expressed in the pair given  E::  Whale: Mammal Cloud: Rain  E: DUPED::  Myopic: Misled Malleable: Molded  TE: COMPLICATE::	in the question.  (B) (D)  (B) (D)	Cart: Horse Painting: Artist  Careful: Cautioned Credible: Cheated	
1. 2.	ELM: TRE (A) (C) GULLIBLE (A) (C) IMPLICAT	to that expressed in the pair given  E::  Whale: Mammal Cloud; Rain  E: DUPED::  Myopic: Misled Malleable: Molded  TE: COMPLICATE::  Vitality: Inevitable	in the question.  (B) (D)  (B) (D)	Cart: Horse Painting: Artist  Careful: Cautioned Credible: Cheated  Empathy: Sympathy	
1. 2. 3.	ELM: TRE (A) (C) GULLIBLE (A) (C) IMPLICAT (A) (C)	to that expressed in the pair given  E::  Whale: Mammal Cloud; Rain  E: DUPED::  Myopic: Misled Malleable: Molded  TE: COMPLICATE::  Vitality: Inevitable Importune: Construct	in the question.  (B) (D)  (B) (D)	Cart: Horse Painting: Artist  Careful: Cautioned Credible: Cheated	
1. 2. 3.	ELM: TRE  (A)  (C)  GULLIBLE  (A)  (C)  IMPLICAT  (A)  (C)  AFTERNO	to that expressed in the pair given  E::  Whale: Mammal Cloud: Rain  E: DUPED::  Myopic: Misled Malleable: Molded  TE: COMPLICATE::  Vitality: Inevitable Importune: Construct  ON: DUSK::	in the question.  (B) (D)  (B) (D)	Cart: Horse Painting: Artist  Careful: Cautioned Credible: Cheated  Empathy: Sympathy	
1. 2. 3.	ELM: TRE  (A)  (C)  GULLIBLE  (A)  (C)  IMPLICAT  (A)  (C)  AFTERNO  (A)	to that expressed in the pair given  E::  Whale: Mammal Cloud; Rain  E: DUPED::  Myopic: Misled Malleable: Molded  TE: COMPLICATE::  Vitality: Inevitable Importune: Construct  ON: DUSK::  Breakfast: Dinner	in the question.  (B) (D)  (B) (D)	Cart: Horse Painting: Artist  Careful: Cautioned Credible: Cheated  Empathy: Sympathy	
1. 2. 3.	ELM: TRE  (A) (C) GULLIBLE  (A) (C) IMPLICATE  (A) (C) AFTERNO (A) (C)	to that expressed in the pair given E::  Whale: Mammal Cloud; Rain E: DUPED::  Myopic: Misled Malleable: Molded TE: COMPLICATE::  Vitality: Inevitable Importune: Construct ON: DUSK::  Breakfast: Dinner Sunday: Saturday	in the question.  (B) (D)  (B) (D)  (B) (D)	Cart: Horse Painting: Artist  Careful: Cautioned Credible: Cheated  Empathy: Sympathy Imply: Simplify	
1. 2. 3.	ELM: TRE  (A) (C) GULLIBLE  (A) (C) IMPLICATE  (A) (C) AFTERNO (A) (C)	to that expressed in the pair given  E::  Whale: Mammal Cloud; Rain  E: DUPED::  Myopic: Misled Malleable: Molded  TE: COMPLICATE::  Vitality: Inevitable Importune: Construct  ON: DUSK::  Breakfast: Dinner	(B) (D) (B) (D) (B) (D) (B) (D)	Cart: Horse Painting: Artist  Careful: Cautioned Credible: Cheated  Empathy: Sympathy Imply: Simplify  Yesterday: Tomorrow	
1. 2. 3.	ELM: TRE  (A) (C) GULLIBLE  (A) (C) IMPLICATE  (A) (C) AFTERNO (A) (C)	to that expressed in the pair given E::  Whale: Mammal Cloud; Rain E: DUPED::  Myopic: Misled Malleable: Molded TE: COMPLICATE::  Vitality: Inevitable Importune: Construct ON: DUSK::  Breakfast: Dinner Sunday: Saturday	(B) (D) (B) (D) (B) (D) (B) (D)	Cart: Horse Painting: Artist  Careful: Cautioned Credible: Cheated  Empathy: Sympathy Imply: Simplify  Yesterday: Tomorrow Night: Dawn	
<ol> <li>3.</li> <li>4.</li> <li>5.</li> </ol>	ELM: TRE  (A)  (C)  GULLIBLE  (A)  (C)  IMPLICAT  (A)  (C)  AFTERNO  (A)  (C)  MINISTER	to that expressed in the pair given  E::  Whale: Mammal Cloud; Rain  E: DUPED::  Myopic: Misled Malleable: Molded  TE: COMPLICATE::  Vitality: Inevitable Importune: Construct  ON: DUSK::  Breakfast: Dinner Sunday: Saturday  R: PULPIT::	(B) (D) (B) (D) (B) (D) (B) (D) (B) (D)	Cart: Horse Painting: Artist  Careful: Cautioned Credible: Cheated  Empathy: Sympathy Imply: Simplify  Yesterday: Tomorrow Night: Dawn  Judge: Bench	
1. 2. 3. 4.	ELM: TRE  (A) (C) GULLIBLE  (A) (C) IMPLICAT  (A) (C) AFTERNO (A) (C) MINISTER (A) (C)	to that expressed in the pair given E::  Whale: Mammal Cloud; Rain  E: DUPED::  Myopic: Misled Malleable: Molded  TE: COMPLICATE::  Vitality: Inevitable Importune: Construct  ON: DUSK::  Breakfast: Dinner Sunday: Saturday  R: PULPIT::  Doctor: Patient Student: Teacher	(B) (D) (B) (D) (B) (D) (B) (D)	Cart: Horse Painting: Artist  Careful: Cautioned Credible: Cheated  Empathy: Sympathy Imply: Simplify  Yesterday: Tomorrow Night: Dawn	
1. 2. 3. 4.	ELM: TRE  (A) (C) GULLIBLE  (A) (C) IMPLICAT  (A) (C) AFTERNO (A) (C) MINISTER (A) (C)	to that expressed in the pair given E::  Whale: Mammal Cloud; Rain E: DUPED::  Myopic: Misled Malleable: Molded TE: COMPLICATE::  Vitality: Inevitable Importune: Construct ON: DUSK::  Breakfast: Dinner Sunday: Saturday R: PULPIT::  Doctor: Patient	(B) (D) (B) (D) (B) (D) (B) (D) (B) (D)	Cart: Horse Painting: Artist  Careful: Cautioned Credible: Cheated  Empathy: Sympathy Imply: Simplify  Yesterday: Tomorrow Night: Dawn  Judge: Bench Programmer: Logic	
1. 2. 3. 4.	ELM: TRE  (A)  (C)  GULLIBLE  (A)  (C)  IMPLICAT  (A)  (C)  AFTERNO  (A)  (C)  MINISTER  (A)  (C)  AUGER: C  (A)	to that expressed in the pair given E::  Whale: Mammal Cloud; Rain  E: DUPED::  Myopic: Misled Malleable: Molded  TE: COMPLICATE::  Vitality: Inevitable Importune: Construct  ON: DUSK::  Breakfast: Dinner Sunday: Saturday  R: PULPIT::  Doctor: Patient Student: Teacher  ARPENTER::  Cement: Mason	(B) (D) (B) (D) (B) (D) (B) (D) (B) (D) (B) (D) (B) (D)	Cart: Horse Painting: Artist  Careful: Cautioned Credible: Cheated  Empathy: Sympathy Imply: Simplify  Yesterday: Tomorrow Night: Dawn  Judge: Bench Programmer: Logic  Apron: Chef	
1. 2. 3. 4.	ELM: TRE  (A) (C) GULLIBLE  (A) (C) IMPLICAT  (A) (C) AFTERNO  (A) (C) MINISTER  (A) (C) AUGER: C  (A) (C)	to that expressed in the pair given E::  Whale: Mammal Cloud; Rain  E: DUPED::  Myopic: Misled Malleable: Molded  TE: COMPLICATE::  Vitality: Inevitable Importune: Construct  ON: DUSK::  Breakfast: Dinner Sunday: Saturday  R: PULPIT::  Doctor: Patient Student: Teacher  ARPENTER::  Cement: Mason Awl: Cobbler	(B) (D) (B) (D) (B) (D) (B) (D) (B) (D)	Cart: Horse Painting: Artist  Careful: Cautioned Credible: Cheated  Empathy: Sympathy Imply: Simplify  Yesterday: Tomorrow Night: Dawn  Judge: Bench Programmer: Logic	
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<ol> <li>2.</li> <li>3.</li> <li>4.</li> <li>7.</li> </ol>	ELM: TRE  (A) (C) GULLIBLE (A) (C) IMPLICAT (A) (C) AFTERNO (A) (C) MINISTER (A) (C) AUGER: C (A) (C) CONTROV (A) (C)	to that expressed in the pair given E::  Whale: Mammal Cloud: Rain E: DUPED::  Myopic: Misled Malleable: Molded TE: COMPLICATE::  Vitality: Inevitable Importune: Construct ON: DUSK::  Breakfast: Dinner Sunday: Saturday R: PULPIT::  Doctor: Patient Student: Teacher ARPENTER:: Cement: Mason Awl: Cobbler TERSY: ARBITRATOR:: Peacemaker: Conflict	(B) (D) (B) (D) (B) (D) (B) (D) (B) (D) (B) (D)	Cart: Horse Painting: Artist  Careful: Cautioned Credible: Cheated  Empathy: Sympathy Imply: Simplify  Yesterday: Tomorrow Night: Dawn  Judge: Bench Programmer: Logic  Apron: Chef Studio: Sculptor	
<ol> <li>2.</li> <li>3.</li> <li>4.</li> <li>7.</li> </ol>	ELM: TRE  (A) (C) GULLIBLE (A) (C) IMPLICAT (A) (C) AFTERNO (A) (C) MINISTER (A) (C) AUGER: C (A) (C) CONTROV (A) (C)	to that expressed in the pair given E::  Whale: Mammal Cloud; Rain E: DUPED::  Myopic: Misled Malleable: Molded TE: COMPLICATE::  Vitality: Inevitable Importune: Construct ON: DUSK::  Breakfast: Dinner Sunday: Saturday PULPIT::  Doctor: Patient Student: Teacher ARPENTER:: Cement: Mason Awl: Cobbler TERSY: ARBITRATOR:: Peacemaker: Conflict Game: Referee	(B) (D) (B) (D) (B) (D) (B) (D) (B) (D) (B) (D) (B) (D) (B) (D)	Cart: Horse Painting: Artist  Careful: Cautioned Credible: Cheated  Empathy: Sympathy Imply: Simplify  Yesterday: Tomorrow Night: Dawn  Judge: Bench Programmer: Logic  Apron: Chef Studio: Sculptor  Artifact: Anthropolog	
1. 2. 3. 4. 5.	ELM: TRE  (A)  (C)  GULLIBLE  (A)  (C)  IMPLICATE  (A)  (C)  AFTERNO  (A)  (C)  MINISTER  (A)  (C)  AUGER: C  (A)  (C)  CONTROV  (A)  (C)  Condemnate	to that expressed in the pair given E::  Whale: Mammal Cloud; Rain  E: DUPED::  Myopic: Misled Malleable: Molded  TE: COMPLICATE::  Vitality: Inevitable Importune: Construct  ON: DUSK::  Breakfast: Dinner Sunday: Saturday  R: PULPIT::  Doctor: Patient Student: Teacher  ARPENTER::  Cement: Mason Awl: Cobbler  TERSY: ARBITRATOR::  Peacemaker: Conflict Game: Referee	(B) (D) (B) (D) (B) (D) (B) (D) (B) (D) (B) (D) (B) (D) (B) (D) (B) (D) (B) (D) (B) (D)	Cart: Horse Painting: Artist  Careful: Cautioned Credible: Cheated  Empathy: Sympathy Imply: Simplify  Yesterday: Tomorrow Night: Dawn  Judge: Bench Programmer: Logic  Apron: Chef Studio: Sculptor  Artifact: Anthropolog Dispute: Mediator  Sorrow: Intention	ist
1. 2. 3.	ELM: TRE  (A)  (C)  GULLIBLE  (A)  (C)  IMPLICATE  (A)  (C)  AFTERNO  (A)  (C)  MINISTER  (A)  (C)  AUGER: C  (A)  (C)  CONTROV  (A)  (C)  Condemnate  (A)	to that expressed in the pair given E::  Whale: Mammal Cloud: Rain  E: DUPED::  Myopic: Misled Malleable: Molded  TE: COMPLICATE::  Vitality: Inevitable Importune: Construct  ON: DUSK::  Breakfast: Dinner Sunday: Saturday  R: PULPIT::  Doctor: Patient Student: Teacher  ARPENTER::  Cement: Mason Awl: Cobbler  TERSY: ARBITRATOR::  Peacemaker: Conflict Game: Referee  Tion: Disapproval:: Ignorance: Patience Optimism: Insight	(B) (D) (B) (D) (B) (D) (B) (D) (B) (D) (B) (D) (B) (D) (B) (D)	Cart: Horse Painting: Artist  Careful: Cautioned Credible: Cheated  Empathy: Sympathy Imply: Simplify  Yesterday: Tomorrow Night: Dawn  Judge: Bench Programmer: Logic  Apron: Chef Studio: Sculptor  Artifact: Anthropolog Dispute: Mediator	ist

**(B)** 

Palisade Display



(C) Stronghold: Defense

(D) Cloister: Storage

20. CAPTAIN: SHOAL::

(A) Soldier: Ambush

(B) Lawyer: Litigation

(C) Corporal: Sergeant

(D) Pilot: Radar

Read the following passages carefully and answer the questions given at its end:

Passage: The purpose of education is to make the student an expert in his subject. This must be clearly understood, and mere muddling through lessons and lectures and books and passing examinations are relegated to secondary importance as means to end-which is excellence in the field chosen.

But there are so many fields, and no man can become an expert in all the fields. It is necessary to decide which fields are the important ones that a man should know well.

It is clear that one's own work is the most important. This has been realised and modern civilization has accordingly provided vocational education. It is now possible to acquire high professional skill in the various fields, medicine, engineering production, commerce and so on-but with good and bad mixed together, and no standard for guidance.

## 21. The purpose of education is to make the student:

- (A) An expert in all fields
- (B) An expert in his subject
- (C) Only capable of earning
- (D) Confident only

# 22. What, according to the writer, is the end?

- (A) Excellence in the field chosen
- (B) Passing the examination
- (C) Earning more and more money
- (D) Cramming lectures and books

#### 23. The modern civilization has provided:

- (A) Vocational education
- (B) Art of conversation

(C) Adult education

(D) Higher education

Passage: According to Aristotle, the most important question in the physical world was the search for happiness. He was not an idealist preaching impossible ideals and counsels of perfection. His scientific training made him a realist who believed that happiness was the aim of life and every activity, even ethics, was subordinate to it. He tries to explore the nature of happiness and explains it by differentiating man from other animals in that he possesses the thinking faculty by which he masters the earth and surpasses all living beings and its development will give him fulfilment and happiness.

#### 24. In the given paragraph:

- (A) Aristotle surpasses the earth and all living beings
- (B) Aristotle tries to explore the nature of physical world
- (C) Aristotle speaks about all living beings
- (D) Aristotle tries to explore the nature of happiness

### 25. Man differs from other animals in having:

(A) A brain

(B) Speaking faculty

(C) Thinking faculty

Eating faculty

#### **ANSWERS**

**(D)** 

1.	(C)	2.	(A)	3.	(B)	3.	(D)	5.	(C)
6.	(A)	7.	(B)	8.	(B)	9.	(B)	10.	(C)
11.	(A)	12.	(C)	13.	(B)	13.	(D)	15.	(B)
16.	(C)	17.	(D)	18.	(D)	19.	(C)	20.	(A)
21.	(B)	22.	(A)	23.	(A)	24.	(D)	25.	(C)

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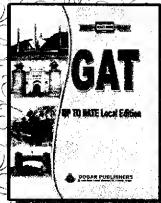
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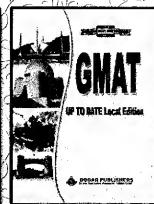
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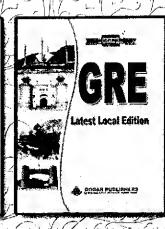
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